Fast and Quasideterministic Single Ion Source from a Dipole-Blockaded Atomic Ensemble

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We present a fast and quasideterministic protocol for the production of single ions and electrons from a cloud of laser-cooled atoms. The approach is based on a two-step process where first a single Rydberg atom is photoexcited from a dipole-blockade configuration and subsequently ionized by an electric field pulse. We theoretically describe these excitation-ionization cycles via dynamical quantum maps and observe a rich behavior of the ionization dynamics as a function of laser Rabi frequency, pulse duration, and particle number. Our results show that a fast sequential heralded production of single charged particles is achievable even from an unstructured and fluctuating atomic ensemble.

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The ability to place single ions into a medium or onto a surface with high precision opens up exciting possibilities for new types of nanofabricated devices and processes in materials science [1–5]. Techniques such as scanning tunneling microscopy [6] and focused ion beam single ion implantation [7] have been very successful in accurate placement of single ions. However, scanning tunneling microscopy is relatively slow, and focused ion beam single ion implantation is stochastic and therefore governed by Poisson statistics. Ideally, one would like fast, precise, and fully deterministic single ion delivery. A promising route towards this goal is to use laser cooling and trapping techniques [8], which allow exquisite control over neutral atoms, therefore enabling “atom optics” to become a realistic prospect for nanotechnology applications [9]. By photoionizing ultracold atoms, one can then transfer the precision control of neutral atoms onto charged particle sources. This approach has sparked research into the development of a new generation of monochromatic ion and electron beams [10–12]. Because these “cold” beams originate from an extended source and are demagnified by a factor of many thousand, the ions can be delivered with nanoscale precision and are less sensitive to vibrations and instabilities than pointlike ion sources [13].

Thus far, there have been two main approaches to making single ion sources based upon laser cooling. First, laser-cooled ions held in a trap can be ejected on demand. For example, linear Paul traps can hold strings of ions which can be emitted deterministically [14,15]. Another approach is to trap a single atom, for example, in a magneto-optical trap (MOT) [16] or optical trap [17], and then photoionize it. While these approaches show great promise, the trap loading remains random and at present the repetition rate is slow (of the order of hertz).

In this Letter, we propose an approach that bypasses the relatively slow process of carefully preparing an initial state. This enables the fast and quasideterministic sequential production of ions out of a standard sample of laser-cooled neutral atoms. By analyzing in detail the quantum dynamics of the ion source, we identify various dynamical regimes and discuss the temporal ion emission statistics as a function of experimental parameters and atom diffusion. We show that the system not only is suited for technological applications but also provides an interesting platform for the study of nonequilibrium dynamics.

The protocol underlying the envisioned ion source is based on a two-step process: At first, a tightly focused laser beam that is resonant with the transition to a high-lying Rydberg state ionizes the Rydberg atom. The ion is subsequently accelerated and extracted from the MOT. The second step involves photoionizing the Rydberg atom. Because of strong interactions between Rydberg atoms, the pair state \(|r, r\rangle\) experiences a distance-dependent energy shift. Below a critical distance \(R_b\) — the blockade radius — this shift becomes larger than the Rabi frequency \(\Omega\). Here \(|r, r\rangle\) becomes energetically inaccessible, and only a single Rydberg atom is excited. (b) Schematic of the ion source. Ultracold atoms are excited within the shaded volume through appropriately focused laser beams. The extension of the excitation volume is smaller than the blockade radius \(R_b\). Atoms can diffuse in and out of the region with rate \(\Gamma_{in}\) and \(\Gamma_{out}\), respectively. An electric field is applied, ionizing the Rydberg atom, and a single ion and electron are emitted in opposite directions. The field-generating electrodes (carrying charges \(\pm ve\)) are indicated at the right- and left-hand sides of the atomic cloud.

FIG. 1 (color online). (a) Dipole blockade. Energy level scheme of a pair of atoms that are resonantly laser-excited from the ground state \(|g\rangle\) to a Rydberg state \(|r\rangle\) with Rabi frequency \(\Omega\). Because of strong interactions between Rydberg atoms, the pair state \(|r, r\rangle\) experiences a distance-dependent energy shift. Below a critical distance \(R_b\) — the blockade radius — this shift becomes larger than the Rabi frequency. Here \(|r, r\rangle\) becomes energetically inaccessible, and only a single Rydberg atom is excited.
Rydberg state is irradiated onto an ensemble of ground state atoms. The use of Rydberg states ensures that at most one ion is created in the subsequent step, which consists of an electric field pulse ionizing the Rydberg atom. The reason for the excitation of only a single atom is the dipole blockade [18–23], which is a consequence of strong and long-range dispersive forces acting among atoms in Rydberg states. These lead to energy level shifts that prevent the laser excitation of many-body states containing more than one Rydberg excitation; cf. Fig. 1(a). An experimental setup depicting the above scheme is sketched in Fig. 1(b). Here, an ensemble of ultracold atoms is prepared between two electrodes. The excitation lasers are focused with a characteristic size that is smaller than the trap volume which is much smaller than the blockade radius R_b. In a steady state MOT, this can, for instance, be achieved by using a three-step excitation scheme [24,25], thereby avoiding avalanche ionization resulting from excitation over an extended region [26]. We assume that the Rabi frequency is uniform over the excitation region, which can be achieved by using flattop beams [27]. The application of a small electric field results in the field ionization of the excited atom, and the resulting ion and its concomitant electron are ejected from the ensemble in opposite directions as shown in Fig. 1(b). The lighter electron can then be detected to “herald” the creation of the ion.

In what follows, we describe a simple model that captures the essential dynamical processes of such an ion source and which permits a detailed study of the statistics of the ion emission. An excitation-ionization cycle consists of a resonant laser pulse of duration τ_ex followed by an electric field pulse of duration τ_ion. The Hamiltonian describing the excitation step is given by $H = \Omega/2 (a†b + b†a)$, where Ω denotes the single-atom Rabi frequency, $a†$ (a) a bosonic operator that creates (annihilates) a particle in the electronic ground state, and $b†$ (b) an operator that creates (annihilates) a Rydberg atom. In order to take the Rydberg blockade into account in a simple way, we impose fermionic anticommutator relations $\{b, b†\} = 1$ and $\{b†, b\} = 0$ on the $b$ operators, so that $b^2 = 0$. This accounts for the fact that a double Rydberg excitation within the blockade volume is highly suppressed [28].

The dynamics of the incoherent ionization step is governed by a Markovian master equation for the density matrix $\rho$ of the (un-ionized) atoms contained in the excitation volume. In order to explicitly resolve the number of ions, we project $\rho$ onto the subspace in which $m \geq 0$ ions have already been created. If $\rho^{(m)}$ denotes the projected density matrix, then $\rho = \sum_m \rho^{(m)}$, and the master equation governing its dynamics is [29]

$$i\partial_t \rho^{(m)} = \gamma \left[ b \rho^{(m-1)} b† (1 - \delta_{m,0}) - \frac{1}{2} (b†b, \rho^{(m)}) \right]$$

with ionization rate $\gamma$.

Since coherent laser excitation and incoherent ionization happen in sequence, we can efficiently describe the dynamics of a whole excitation-ionization cycle within the framework of dynamical quantum maps [30]. The time evolution during the $k$th excitation-ionization cycle is given as follows: Starting at time $t_k-1$, the laser pulse coherently excites an atom in the excitation volume; i.e., the density matrix $\rho_k$ undergoes a unitary evolution $\rho' = U \rho_k U†$ with $U(\tau_{ex}) = \text{exp}(-iH\tau_{ex})$. Since the laser excitation does not change the number of particles in the volume, $U$ is block diagonal in particle number space, and the coherent dynamics for an ensemble of $n$ atoms takes place in the subspace spanned by the states $|g⟩^⊗n$ and $S[|g⟩^⊗n⟨r|]$. The subsequent ionization pulse maps the density matrix $\rho'$ to $\rho_k = M_1 \rho'M_1† + M_2 \rho'M_2†$, where

$$M_1 = \begin{pmatrix} 1 & 0 \\ 0 & e^{-\gamma_{ion}/2} \end{pmatrix}, \quad M_2 = \begin{pmatrix} 0 & \sqrt{1 - e^{-\gamma_{ion}}} \\ 0 & 0 \end{pmatrix}$$

are Kraus operators. $M_1$ describes the dynamics induced by the anticommutator term of the master equation (1), while $M_2$ captures the quantum jump processes induced by the first term on the right-hand side of Eq. (1).

The density matrix of the subspace, where exactly $m$ ions have been produced after the $k$th excitation-ionization cycle, can now be obtained iteratively:

$$\rho^{(m)}_k = \mathcal{K}_1^{(m)} \rho^{(m-1)}_k$$

$$\rho^{(0)}_k = \mathcal{K}_1^{(0)} \rho^{(0)}_k$$

$$\rho^{(m)}_k = [\mathcal{K}_1^{(m)} ρ^{(m-1)}_k (1 - \delta_{km}) + \mathcal{K}_2^{(m)} ρ^{(m-1)}_{k-1}] Θ(k - m)$$

with

$$\mathcal{K}_1^{(m)} ρ^{(m)}_{k-1} = M_1 U_{N + m} \rho^{(m)}_{k-1} U_{N + m}†$$

and

$$\mathcal{K}_2^{(m)} ρ^{(m-1)}_{k-1} = M_2 U_{N - m} \rho^{(m-1)}_{k-1} U_{N - m}† M_2†.$$ Here, $N$ denotes the number of atoms in the focal volume at $t = 0$, and $Θ(x)$ is the Heaviside step function.

Let us now apply this theoretical framework to analyze the dynamics of the ion source in different operational regimes.

(i) Quasideterministic regime in a microtrap.—Here we consider an atomic ensemble which is confined within a trap volume which is much smaller than the blockade radius. We start initially from a fixed number of trapped atoms $N$, and the successive application of the excitation-ionization cycle will lead eventually to a depletion of the trap. For our numerical example, we consider an initial
atom number of $N = 500$—a situation which can be achieved, for example, in the case of an atomic Bose-Einstein condensate held in a tight optical trap. The Rydberg excitation is carried out with a $\pi$ pulse, with respect to the collective Rabi frequency $\sqrt{N} \Omega$ [23,31]. In the regime of a relatively large initial number of atoms, i.e., $N \gg 1$, this collective Rabi frequency changes negligibly with the emission of each ion. Thus, each excitation cycle of length $\tau_{\text{ex}} = \pi/\sqrt{N} \Omega$ will—with probability close to unity—excite a single Rydberg atom, and this excitation process will remain efficient even after many ions have been emitted. This is indeed illustrated in Fig. 2, which shows the probability of having ionized exactly $k$ atoms after $k$ excitation-ionization cycles. In addition, the inset shows the probability distribution $p_k^{(m)}$ of having ionized $m$ atoms after $k$ cycles. Hence, for a fully deterministic single ion source, this quantity is 1 for $m = k$ and 0 elsewhere. The data indeed reflect that a single ion is produced in each cycle until the depletion of the trap begins to alter the collective Rabi frequency significantly. In principle, the Rabi frequency could be adapted dynamically in order to account for atom loss. However, we can see that, even in the static case, many atoms can be rapidly extracted from the sample with high probability. By using typical experimental parameters, i.e., an excitation time $\tau_{\text{ex}} \sim 10$ ns and an ionization rate $\gamma \sim 100$ kHz, an ion production rate up to 100 kHz appears feasible.

(ii) **Trapped states in a microtrap.**—We are now interested in the ion emission dynamics for the case when the excitation pulse length is chosen independent of the particle number in the excitation volume, i.e., without taking the collective laser coupling induced by the dipole blockade into account. Let us first consider the situation in which Rydberg atoms are excited with a single-atom $\pi$ pulse, i.e.,

$$\tau_{\text{ex}} = \pi \Omega^{-1}. $$

The evolution of the corresponding probability density is shown in Fig. 3(a). We find that initially the mean number of emitted ions $m$ grows with the number of cycles $k$. However, in this example with 50 initial atoms, the probability of emitting ions beyond the 250th cycle is strongly suppressed. In fact, the data show that no more than 16 ions will be emitted in total even if the number of cycles is increased. The reason for that is the emergence of trapped states which occur when $\sqrt{N - m \Omega \tau_{\text{ex}}}/2$ becomes an integer multiple of $\pi$. Here the time evolution operator (2) becomes the identity (up to a phase factor of $\pm 1$), and consequently the excitation step does not generate Rydberg atoms. This effect is analogous to the occurrence of trapped states in micromasers. These are photonic number states such that atoms transiting the cavity undergo a $2\pi$ pulse (or an integer multiple of it) [32,33]. A further interesting dynamical regime is reached when the Rydberg excitation pulse is close to a $\nu \pi$ pulse with $\nu = 1, 3, 5, \ldots$. In this case, quasi-trapped states can occur that have a striking effect on the ionization dynamics. The corresponding probability distribution for an excitation pulse length of $\tau_{\text{ex}} = 7.1 \pi/\Omega$ is depicted in Fig. 3(b). As in the previous example, a trapped state is reached after a few initial cycles. However, since $\sqrt{\eta \Omega \tau_{\text{ex}}}/2$ can never be a strict multiple of $\pi$, the trapping is not perfect and we observe a slow leakage into other quasi-trapped states. Eventually, this leads to a multimodal ion distribution that peaks at ion numbers $m$ where $\sqrt{N - m \Omega \tau_{\text{ex}}}/2$ is close to a multiple integer of $\pi$. This shows that, in order to avoid trapping effects and to use the proposed device as a single-ion source, the excitation pulse should be chosen to be a $\pi$ pulse with respect to the collective Rabi frequency.

(iii) **Excitation from an extended atomic cloud.**—So far, we have considered a fully blockaded dense atomic sample in a microtrap with a radius much smaller than $R_b$. Let us now discuss the situation usually encountered in extended systems like standard MOTs. Here the atom density is relatively small, and, moreover, atoms can diffuse in and out of the excitation volume as depicted in Fig. 1(b). In

FIG. 2 (color online). Quasideterministic ion production. Probability $p_{k}^{(m)}$ of having produced $k$ ions after $k$ cycles for initial particle number $N = 500$ and excitation time $\tau_{\text{ex}} = \pi/(\sqrt{N} \Omega)$ (the other parameters are Rabi frequency $\Omega = 4\gamma$ and ionization pulse length $\tau_{\text{ion}} = 16 \gamma^{-1}$). Inset: Probability distribution $p_k^{(m)}$ of having produced $m$ ions after $k$ cycles. The color map is chosen such that white (black) corresponds to 0 (1). The data show that a single ion is created with nearly unit probability after each excitation-ionization cycle.

FIG. 3. Trapped states. Probability distribution $p_k^{(m)}$ of having produced $m$ ions after $k$ excitation-ionization cycles for a fully blockaded sample initially prepared with $N = 500$ atoms. (a) The Rydberg excitation is performed by using a single-atom $\pi$ pulse, i.e., $\tau_{\text{ex}} = \pi/\Omega$. (b) The Rydberg excitation pulse length is $\tau_{\text{ex}} = 7.1 \pi/\Omega$. The values of the other parameters are $\gamma = 4\Omega$ and $\tau_{\text{ion}} = 4\Omega^{-1}$. The color map is chosen such that white (black) corresponds to 0 (1).
order to account for the effects of diffusion, we use a simple rate model: Atoms can enter the excitation volume at a constant rate $\Gamma_{in}$ and leave it at a rate $\Gamma_{out} = \kappa n$, where $n$ is the number of atoms in the volume and $\kappa$ is the diffusion rate. In an equilibrium gas cloud we have $\Gamma_{in} = \Gamma_{out}$ and hence $\Gamma_{in} = \kappa \bar{n}$, where $\bar{n}$ is the mean number of atoms in the excitation volume. This simple model yields a Poissonian atom distribution with mean $\kappa \bar{n}$, where $\bar{n}$ is the number of atoms in the excitation region. To describe the influence of diffusion on the ion source dynamics, we exploit the fact that the excitation cycle ($\tau_{ex} \approx 10$ ns) is much shorter than the ionization step ($\tau_{ion} \approx 10 \mu$s). Thus we assume that diffusion is relevant only during the latter. This is consistent with the frozen gas approximation [34] usually employed in the description of the laser excitation of cold Rydberg gases. Moreover, we consider the limit of slow diffusion; i.e., we assume $\kappa \tau_{ion} \gg 1/(2 \bar{n})$, which means that during the ionization cycle only one atom will enter or leave the excitation volume at a time. Effectively, this amounts to solving the diffusion equation up to first order. Within these approximations we can again use the above-mentioned theoretical framework of dynamical quantum maps and arrive at dynamical equations analogous to (4) (see Supplemental Material [35]).

Let us now investigate the excitation dynamics. We assume that the initial mean number of atoms in the excitation volume is $\bar{n} = 10.2$. With a realistic blockade radius of 5 $\mu$m, this would correspond to typical MOT densities of $10^{10}$ atoms/cm$^3$. In Figs. 4(a) and 4(b), we show the corresponding probability distributions $p_{k}^{(m)}$ for the case without diffusion and for a diffusion rate of $\kappa = 10^{-3} \gamma$, respectively. The data are averaged over the distribution of the initial number of particles in the volume, and the excitation pulse length is fixed at $\tau_{ex} = \pi/\sqrt{n}\Omega$. This choice therefore corresponds to a $\pi$ pulse with respect to the collective Rabi frequency $\sqrt{n}\Omega$. Comparing Figs. 4(a) and 4(b), we see that diffusion leads to a slow drift of the ion number distribution to larger mean values with an increasing number of excitation-ionization cycles. This drift stems from the fact that the excitation volume is quickly depleted due to the ionization process, which is much faster than the diffusion. At long times (large $k$), further ions can be produced only when particles diffuse into the empty excitation volume leading to a slow increase of the total number of emitted ions.

More interestingly, however, for the first few cycles the ion source produces one ion per cycle with a high probability and is therefore quasideterministic. Note that this is despite averaging over the initial atom number distribution. Therefore, even when operated in an extended atomic cloud, the behavior of the ion source is very similar to that in a fully blockaded sample discussed in (i). This is further corroborated by Fig. 4(c), where we show the probability of having emitted $k$ ions after $k$ excitation-ionization cycles. For comparison we also show the probability for the case in which the Rydberg excitation is performed with a $\pi$ pulse with respect to the single-atom Rabi frequency $\Omega$. The data show that the performance of the ion source is indeed significantly improved when the excitation pulse is chosen as a $\pi$ pulse with respect to the collective Rabi frequency $\sqrt{n}\Omega$. Note that the performance of the ion source can be enhanced further by resetting the ion source after the few cycles during which quasideterministic ion emission is taking place. This could be done by refocusing the excitation laser to a different part of the gas cloud, thereby avoiding the depletion of the excitation volume and the broadening of the ion distribution visible in Figs. 4(a) and 4(b). The movement of the source can easily be compensated by ion optics to ensure that the ion is imaged onto the correct position. The fidelity of the single ion emission can be tested by performing number-resolved coincidence measurements [36].

In conclusion, we have presented and analyzed theoretically a fast and heralded single ion source based on a dipole-blockaded atomic ensemble. The source can be operated in a variety of dynamical regimes and permits the quasicontinuous and quasideterministic production of single ions even from an extended gas cloud. The statistics of the ion emission shows some interesting dynamical features such as the emergence of "trapped" states, reminiscent of micromaser physics. We expect that the presented scheme can be of practical relevance for applications in materials science.

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[28] The probability $p_2(t)$ of having excited two Rydberg atoms after a time $t$ in the excitation volume can be estimated by using the time-dependent perturbation theory, $p_2(t) = n(n-1)\Omega^2\sin^2(\sqrt{n}\Omega t)/(2V)$, where $n$ is the number of atoms and $V$ the minimal possible interaction strength of two Rydberg atoms within the excitation volume.