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A weak lensing mass reconstruction of the large-scale filament feeding the massive galaxy cluster MACS J0717.5+3745

Mathilde Jauzac,1,2☆ Eric Jullo,1,3 Jean-Paul Kneib,1 Harald Ebeling,4 Alexie Leauthaud,5 Cheng-Jiun Ma,4 Marceau Limousin,1,6 Richard Massey7 and Johan Richard8

1Laboratoire d'Astrophysique de Marseille – LAM, Université d'Aix-Marseille & CNRS, UMR7326, 38 rue F. Joliot-Curie, 13388 Marseille Cedex 13, France
2Astrophysics and Cosmology Research Unit, School of Mathematical Sciences, University of KwaZulu-Natal, Durban 4041, South Africa
3Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA 91109, USA
4Institute for Astronomy, University of Hawaii, 2680 Woodlawn Drive, Honolulu, HI 96822, USA
5Kavli Institute for the Physics and Mathematics of the Universe (Kavli IPMU, WPI), Todai Institutes for Advanced Study, the University of Tokyo, Kashiwa 277-8583, Japan
6Dark Cosmology Centre, Niels Bohr Institute, University of Copenhagen, Juliane Maries Vej 30, DK-2100 Copenhagen, Denmark
7Institute for Computational Cosmology, Durham University, South Road, Durham DH1 3LE
8CRAL, Observatoire de Lyon, Université Lyon 1, 9 Avenue Ch. André, 69561 Saint Genis Laval Cedex, France

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ABSTRACT

We report the first weak lensing detection of a large-scale filament funnelling matter on to the core of the massive galaxy cluster MACS J0717.5+3745.

Our analysis is based on a mosaic of 18 multipassband images obtained with the Advanced Camera for Surveys aboard the Hubble Space Telescope, covering an area of ∼10 × 20 arcmin². We use a weak lensing pipeline developed for the Cosmic Evolution Survey, modified for the analysis of galaxy clusters, to produce a weak lensing catalogue. A mass map is then computed by applying a weak gravitational lensing multiscale reconstruction technique designed to describe irregular mass distributions such as the one investigated here. We test the resulting mass map by comparing the mass distribution inferred for the cluster core with the one derived from strong lensing constraints and find excellent agreement.

Our analysis detects the MACS J0717.5+3745 filament within the 3σ detection contour of the lensing mass reconstruction, and underlines the importance of filaments for theoretical and numerical models of the mass distribution in the cosmic web. We measure the filament’s projected length as ∼4.5 h⁷₄⁻¹ Mpc, and its mean density as (2.92 ± 0.66) × 10⁸ h⁷₄⁻² M⊙ kpc⁻². Combined with the redshift distribution of galaxies obtained after an extensive spectroscopic follow-up in the area, we can rule out any projection effect resulting from the chance alignment on the sky of unrelated galaxy group-scale structures. Assuming plausible constraints concerning the structure’s geometry based on its galaxy velocity field, we construct a three-dimensional (3D) model of the large-scale filament. Within this framework, we derive the 3D length of the filament to be 18 h⁷₄⁻¹ Mpc. The filament’s deprojected density in terms of the critical density of the Universe is measured as (206 ± 46) ρ₉₅₀, a value that lies at the very high end of the range predicted by numerical simulations. Finally, we study the distribution of stellar mass in the field of MACS J0717.5+3749 and, adopting a mean mass-to-light ratio ⟨M*/Lₖ⟩ of 0.73 ± 0.22 and assuming a Chabrier initial mass function, measure a stellar mass fraction along the filament of (0.9 ± 0.2) per cent, consistent with previous measurements in the vicinity of massive clusters.

Key words: gravitational lensing: weak – galaxies: clusters: individual: MACS J0717.5+3745 – cosmology: observations – large-scale structure of Universe.

*E-mail: mathilde.jauzac@gmail.com

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1 INTRODUCTION

In a Universe dominated by cold dark matter (CDM), such as the one parametrized by the ΛCDM concordance cosmology, hierarchical structure formation causes massive galaxy clusters to form through a series of successive mergers of smaller clusters and groups of galaxies, as well as through continuous accretion of surrounding matter. N-body simulations of the dark matter distribution on very large scales (Bond, Kofman & Pogosyan 1996; Yess & Shandarin 1996; Aragón-Calvo et al. 2007; Hahn et al. 2007) predict that these processes of merging and accretion occur along preferred directions, i.e. highly anisotropically. The result is the ‘cosmic web’ (Bond et al. 1996), a spatially highly correlated structure of interconnected filaments and vertices marked by massive galaxy clusters. Abundant observational support for this picture has been provided by large-scale galaxy redshift surveys (e.g. Geller & Huchra 1989; York et al. 2000; Colless et al. 2001) showing voids surrounded and connected by filaments and sheets of galaxies.

A variety of methods have been developed to detect filaments in surveys, among them a ‘friends-of-friends’ algorithm (FOF; Huchra & Geller 1982) combined with ‘shapefinders’ statistics (Sheth & Jain 2003), the ‘skeleton’ algorithm (Novikov, Colombi & Doré 2006; Sousbie et al. 2006), a two-dimensional technique developed by Moody, Turner & Gott (1983) and the Smoothed Hessian Major Axis Filament Finder (SHMAFF; Bond, Strauss & Cen 2010).

Although ubiquitous in large-scale galaxy surveys, filaments have proven hard to characterize physically, owing to their low density and the fact that the best observational candidates often turn out to be not primordial in nature but the result of recent cluster mergers. Specifically, attempts to study the warm-hot intergalactic medium (WHIM; Cen & Ostriker 1999), resulting from the expected gravitational heating of the intergalactic medium in filaments, remain largely inconclusive because it is hard to ascertain for filaments near cluster whether spectral X-ray features originate from the filament or from past or ongoing clusters mergers (Kaarstra et al. 2006; Rasmussen & Ponman 2007; Galeazzi, Gupta & Ursino 2009; Williams et al. 2010). Some detections appear robust as they have been repeatedly confirmed (Fang et al. 2002; Fang, Canizares & Yao 2007; Williams et al. 2007) but are based on just one X-ray line. An alternative observational method is based on a search for filamentary overdensities of galaxies relative to the background (Ebeling, Barrett & Donovan 2004; Pimbblet & Drinkwater 2004). When conducted in 3D, i.e. including spectroscopic galaxy redshifts, this method is well suited to detecting filament candidates. It does, however, not allow the determination of key physical properties unless it is supplemented by follow-up studies targeting the presumed WHIM and dark matter which are expected to constitute the vast majority of the mass of large-scale filaments. By contrast, weak gravitational lensing offers the tantalizing possibility of detecting directly the total mass content of filaments (Mead, King & McCarthy 2010), since the weak lensing (WL) signal arises from luminous and dark matter alike, regardless of its dynamical state.

Previous weak gravitational lensing studies of binary clusters found tentative evidence of filaments, but did not result in clear detections. One of the first efforts was made by Clowe et al. (1998) who reported the detection of a filament apparently extending from the distant cluster RXJ1716+67 ($z = 0.81$), using images obtained with the Keck 10-m telescope and University of Hawaii (UH) 2.2-m telescope. This filamentary structure would relate two distinct subclusters detected on the mass and light maps. The detection was not confirmed though. Almost at the same time Kaiser et al. (1998) conducted a WL study of the supercluster MS 0302+17 with the UH8K CCD camera on the Canada–France–Hawaii Telescope (CFHT). Their claimed detection of a filament in the field was, however, questioned on the grounds that the putative filament overlapped with both a foreground structure as well as with gaps between CCD chips. Indeed, Gavazzi et al. (2004) showed the detection to have been spurious by means of a second study of MS 0302+17 using the CFHT 12K camera. A weak gravitational lensing analysis with MPG/ESO Wide Field Imager conducted by Gray et al. (2002) claimed the detection of a filament in the triple cluster A901/902. The candidate filament appeared to connect two of the clusters and was detected in both the galaxy distribution and in the WL mass map. However, this detection too was of low significance and coincided partly with a gap between the chips of the camera. As in the case of MS 0302+17, a re-analysis of the A901/A902 complex using high-quality HST/ACS images by Heymans et al. (2008) failed to detect the filament and led the authors to conclude that the earlier detection was caused by residual point spread function (PSF) systematics and limitation of the KS 93 mass reconstruction used in the study by Gray et al. (2002). A further detection of a filament candidate was reported by Dietrich et al. (2005) based on a weak gravitational lensing analysis of the close double cluster A222/A223. Initial concerns, as in similar cases, that the putative filament connecting A222 and A223 might be a merger remnant rather than primordial in nature were alleviated by a follow-up X-ray study of Werner et al. (2008) who found the gas between the two clusters to be too cool for it to have experienced merger-induced shock heating. A weak lensing study of this cluster pair by Dietrich et al. (2012) finds further evidence for the presence of a genuine filament.

In this paper we describe the first weak gravitational analysis of the very massive cluster MACS J0717.5+3745 ($z = 0.55$; Edge et al. 2003; Ebeling et al. 2004, 2007; Ma et al. 2008; Ma, Ebeling & Barrett 2009). Optical and X-ray analyses of the system...
(Ebeling et al. 2004; Ma et al. 2008, 2009) find compelling evidence of a filamentary structure extending towards the south-east of the cluster core. Using WL data to reconstruct the mass distribution in and around MACS\,J0717.5$+$3745, we directly detect the reported filamentary structure in the field of MACS\,J0717.5$+$3745.

The paper is organized as follows. After an overview of the observational data in Section 2, we discuss the gravitational lensing data in hand in Section 3. The modelling of the mass using a multiscale approach is described in Section 4. Results are discussed in Section 5, and we present our conclusions in Section 6.

All our results use the ΛCDM concordance cosmology with $\Omega_M = 0.3$, $\Omega_{\Lambda} = 0.7$ and a Hubble constant $H_0 = 74$ km s$^{-1}$ Mpc$^{-1}$, hence 1 arcsec corresponds to 6.065 kpc at the redshift of the cluster. Magnitudes are quoted in the AB system.

## 2 OBSERVATIONS

The Massive Cluster Survey (MACS; Ebeling, Edge & Henry 2001) was the first cluster survey to search exclusively for very massive clusters at moderate to high redshift. Covering over 20,000 deg$^2$ and using dedicated optical follow-up observations to identify faint X-ray sources detected in the ROSAT All-Sky Survey, MACS compiled a sample of over 120 very X-ray luminous clusters at $z > 0.3$, thereby more than tripling the number of such systems previously known. The high-redshift MACS subsample (Ebeling et al. 2007) comprises 12 clusters at $z > 0.5$. MACS\,J0717.5$+$3745 is one of them. All 12 were observed with the Advanced CCD Imaging Spectrometer-I array (ACIS-I) imaging spectrograph onboard the Chandra X-Ray Observatory. Moderately deep optical images covering $30 \times 27$ arcmin$^2$ were obtained in five passbands ($B$, $V$, $R_c$, $I_c$, $z'$) with the Suprime-Cam wide-field imager on the Subaru 8.2-m telescope, and supplemented with $u$-band imaging obtained with MegaCam on the CFHT. Finally, the cores of all clusters in this MACS subsample were observed with the Advanced Camera for Surveys (ACS) onboard HST in two bands, F555W and F814W, for 4.5 ks in both bands, as part of programmes GO-09722 and GO-11560 (PI: Ebeling).

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</table>

$^a$Cluster core; observed through F555W, rather than F606W filter.

### 2.1 HST/ACS wide-field imaging

A mosaic of images of MACS\,J0717.5$+$3745 and the filamentary structure to the south-east was obtained between 2005 January 24 and February 9 with the ACS aboard HST (GO-10420, PI: Ebeling). The 3 × 6 mosaic consists of images in the F606W and F814W filters, observed for roughly 2.0 and 4.0 ks, respectively (1 and 2 HST orbits). Only 17 of the 18 tiles of the mosaic were covered though, since the core of the cluster had been observed already (see Table 1 for more details).

Charge transfer inefficiency (CTI), due to radiation damage of the ACS CCDs above the Earth’s atmosphere, creates spurious trails behind objects in HST/ACS images. Since CTI affects galaxy photometry, astrometry and shape measurements, correcting the effect is critical for WL studies. We apply the algorithm proposed by Massey et al. (2010) which operates on the raw data and returns individual electrons to the pixels from which they were erroneously dragged during readout. Image registration, geometric distortion corrections, sky subtraction, cosmic ray rejection and the final combination of the dithered images are then performed using the standard MULTIDRIZZLE routines (Koekemoer et al. 2002). MULTIDRIZZLE parameters are set to values optimized for precise galaxy shape measurement (Rhodes et al. 2007), and output images created with a 0.03 arcsec pixel grid, compared to the native ACS pixel scale of 0.05 arcsec.

### 2.2 Ground-based imaging

MACS\,J0717.5$+$3745 was observed in the $B$, $V$, $R_c$, $I_c$ and $z'$ bands with the Suprime-Cam wide-field camera on the Subaru 8.2-m telescope (Miyazaki et al. 2002). These observations are supplemented by images in the $u'$ band obtained with the MegaPrime camera on the CFHT 3.6-m telescope, as well as near-infrared imaging in the $J$ and $K_s$ bands obtained with WIRCam on CFHT. Exposure times and seeing conditions for these observations are listed in Table 2 (see also Ma 2010). All data were reduced using standard techniques which were, however, adapted to deal with special characteristics of the Suprime-Cam and MegaPrime data; for more details see Donovan (2007).
with the Low Resolution Imaging Spectrometer (LRIS) and Gemini supplemented by observations of the cluster core region performed (DEIMOS) on the Keck-II 10-m telescope on Mauna Kea, sup-
2008, mainly with the Deep Imaging Multi-Object Spectrograph full length of the filament) were conducted between 2000 and

Spectroscopic observations of MACS J0717.5
3745 (including the

Spectroscopic and photometric redshifts
Ilbert et al. (2006). In addition to employing $\chi^2$ optimization during SED fitting, LE PHARE adaptively adjusts the photometric zero-points by using galaxies with spectroscopic redshifts as a training set. This approach reduces the fraction of catastrophic errors and also mitigates systematic trends in the differences between spectroscopic and photometric redshifts (Ilbert et al. 2006).

Further details, e.g. concerning the selection of targets for spectroscopy or the spectral templates used for the determination of photometric redshifts, are provided by Ma et al. (2008). The full redshift catalogue as well as an analysis of cluster substructure and dynamics as revealed by radial velocities will be presented in Ebeling et al. (in preparation).

2.3 Spectroscopic and photometric redshifts
Spectroscopic observations of MACS J0717.5+3745 (including the full length of the filament) were conducted between 2000 and 2008, mainly with the Deep Imaging Multi-Object Spectrograph (DEIMOS) on the Keck-II 10-m telescope on Mauna Kea, supplemented by observations of the cluster core region performed with the Low Resolution Imaging Spectrometer (LRIS) and Gemini

Table 2. Overview of ground-based imaging observations of MACS J0717.5+3745.

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The ground-based imaging data thus obtained are used primarily to compute photometric redshifts which allow the elimination of cluster members and foreground galaxies that would otherwise dilute the shear signal. To this end we use the object catalogue compiled by Ma et al. (2008) which we describe briefly in the follow-

Figure 2. Colour–colour diagram ($B - R$ versus $R - I$) for objects within the HST/ACS mosaic of MACS J0717.5+3745. Grey dots represent all objects in the study area. Unlensed galaxies diluting the shear signal are marked by different colours: galaxies spectroscopically confirmed as cluster members or foreground galaxies (green); galaxies classified as foreground objects because of their photometric redshifts (red) and galaxies classified as cluster members via photometric redshifts (yellow). The solid black lines delineate the BRI colour cut defined for this work to mitigate shear dilution by unlensed galaxies.

Figure 3. Redshift distribution of all galaxies with $B$, $R_C$ and $I_C$ photometry from Subaru/Suprime-Cam observations that have photometric or spectroscopic redshifts (black histogram). The cyan histogram shows the redshift distribution of galaxies classified as background objects using the BRI criterion illustrated in Fig. 2.

Multi-Object Spectrograph (GMOS) on Keck-I and Gemini-North, respectively. The DEIMOS instrument set-up combined the 600ZD grating with the GC455 order-blocking filter and a central wavelength between 6300 and 7000 Å; the exposure time per multi-object spectroscopy (MOS) mask was typically 3 $\times$ 1800 s. A total of 18 MOS masks were used in our DEIMOS observations; spectra of 1752 unique objects were obtained (65 of them with LRIS and 48 with GMOS), yielding 1079 redshifts, 537 of them of cluster members. Fig. 1 shows the area covered by our spectroscopic survey as well as the loci of the targeted galaxies. The data were reduced with the DEIMOS pipeline developed by the DEEP2 project.

Photometric redshifts for galaxies with $m_{R_C} < 24.0$ were computed using the adaptive SED-fitting code LE PHARE (Arnouts et al. 1999; Ilbert et al. 2006, 2009). In addition to employing $\chi^2$ optimization during SED fitting, LE PHARE adaptively adjusts the photometric zero-points by using galaxies with spectroscopic redshifts as a training set. This approach reduces the fraction of catastrophic errors and also mitigates systematic trends in the differences between spectroscopic and photometric redshifts (Ilbert et al. 2006).

Further details, e.g. concerning the selection of targets for spectroscopy or the spectral templates used for the determination of photometric redshifts, are provided by Ma et al. (2008). The full redshift catalogue as well as an analysis of cluster substructure and dynamics as revealed by radial velocities will be presented in Ebeling et al. (in preparation).

3 WEAK GRAVITATIONAL LENSING ANALYSIS

3.1 The ACS catalogue
Our WL analysis is based on shape measurements in the ACS/F814W band. Following a method developed for the analysis of data obtained for the Cosmic Evolution Survey (COSMOS) and described in Leauthaud et al. (2007, hereafter L07) we use the
3.2 Foreground, cluster and background galaxy identifications

Since only galaxies behind the cluster are gravitationally lensed, the presence of cluster members and foreground galaxies in our ACS catalogue dilutes the observed shear and reduces the significance of all quantities derived from it. Identifying and eliminating as many contaminants as possible is thus critical. The large-scale filament feeding MACS J0717, as shown in Fig. 4, the solid black line delineates the uncontaminated uBV colour cut defined for this work to mitigate shear dilution by unlensed galaxies.

Figure 4. As Fig. 2 but for the $B - V$ and $u - B$ colours. The solid black line delineates the $uBV$ colour cut defined for this work to mitigate shear dilution by unlensed galaxies.

The large-scale filament feeding MACS J0717, as shown in Fig. 4, the solid black line delineates the uncontaminated uBV colour cut defined for this work to mitigate shear dilution by unlensed galaxies.

Figure 5. Redshift distribution of all galaxies with $u$, $b$ and $V$ photometry from CFHT/MegaCam and Subaru/Suprime-Cam observations that have photometric or spectroscopic redshifts (black histogram). The cyan histogram shows the redshift distribution of galaxies classified as background objects using the $uBV$ criterion illustrated in Fig. 4.

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Photometric redshifts derived as described in Section 2.3. Taking into account the statistical uncertainty of $\Delta z = 0.021$ of the photometric redshifts, galaxies are defined as cluster members if their photometric redshift satisfies the criterion:

$$|z_{\text{phot}} - z_{\text{cluster}}| < \sigma_{z_{\text{phot}}},$$

where $z_{\text{phot}}$ and $z_{\text{cluster}}$ are the photometric redshift of the galaxy and the spectroscopic redshift of the galaxy cluster, respectively. Reflecting the need for a balance between completeness and contamination, these redshift limits are much more generous than those used in conjunction with spectroscopic redshifts, which set the redshift range for cluster membership to $3\sigma \sim 0.0122$. For more details, see Ma (2010), as well as Ma et al. (2008) and Ma & Ebeling (2010).

In spite of these cuts according to galaxy redshift, the remaining ACS galaxy sample is most likely still contaminated by foreground and cluster galaxies, the primary reason being the large difference in angular resolution and depth between the ACS and Subaru images. The relatively low resolution of the ground-based data causes the Subaru catalogue to be confusion limited and makes matching galaxies between the two catalogues difficult, especially near the cluster core. As a result, we can assign a redshift to only $\sim 15\%$ of the galaxies in the $HST$/ACS galaxy catalogue.

For galaxies without redshifts, we use colour–colour diagrams ($B - R$ versus $R - I$, Fig. 2, and $B - V$ versus $u - B$, Fig. 4) to identify foreground and cluster members. Using galaxies with spectroscopic or photometric redshifts from the full photometric Subaru catalogue with a magnitude limit of $m_{R_c} = 25$, we identify regions marked dominated by unlensed galaxies (foreground galaxies and cluster members). In the $BRI$ plane we find $B - R < 2.6 (R - I) + 0.05, (R - I) > 1.03$ or $(B - R) < 0.9$ to best isolate unlensed galaxies; in the $UBV$ plane the most efficient criterion is $B - V < -0.5 (u - B) + 0.85$. The large-scale filament feeding MACS J0717, as shown in Fig. 4, the solid black line delineates the uncontaminated uBV colour cut defined for this work to mitigate shear dilution by unlensed galaxies.

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where $z_{\text{phot}}$ and $z_{\text{cluster}}$ are the photometric redshift of the galaxy and the spectroscopic redshift of the galaxy cluster, respectively. Reflecting the need for a balance between completeness and contamination, these redshift limits are much more generous than those used in conjunction with spectroscopic redshifts, which set the redshift range for cluster membership to $3\sigma \sim 0.0122$. For more details, see Ma (2010), as well as Ma et al. (2008) and Ma & Ebeling (2010).

In spite of these cuts according to galaxy redshift, the remaining ACS galaxy sample is most likely still contaminated by foreground and cluster galaxies, the primary reason being the large difference in angular resolution and depth between the ACS and Subaru images. The relatively low resolution of the ground-based data causes the Subaru catalogue to be confusion limited and makes matching galaxies between the two catalogues difficult, especially near the cluster core. As a result, we can assign a redshift to only $\sim 15\%$ of the galaxies in the $HST$/ACS galaxy catalogue.

For galaxies without redshifts, we use colour–colour diagrams ($B - R$ versus $R - I$, Fig. 2, and $B - V$ versus $u - B$, Fig. 4) to identify foreground and cluster members. Using galaxies with spectroscopic or photometric redshifts from the full photometric Subaru catalogue with a magnitude limit of $m_{R_c} = 25$, we identify regions marked dominated by unlensed galaxies (foreground galaxies and cluster members). In the $BRI$ plane we find $B - R < 2.6 (R - I) + 0.05, (R - I) > 1.03$ or $(B - R) < 0.9$ to best isolate unlensed galaxies; in the $UBV$ plane the most efficient criterion is $B - V < -0.5 (u - B) + 0.85$. The large-scale filament feeding MACS J0717, as shown in Fig. 4, the solid black line delineates the uncontaminated uBV colour cut defined for this work to mitigate shear dilution by unlensed galaxies.
Figs 3 and 5 show the galaxy redshift distributions before and after the colour–colour cuts (BRI or uBV) are applied. The results of either kind of filtering are similar. The uBV selection is more efficient at removing cluster members and foreground galaxies at $z \leq 0.6$ (20 per cent remain compared to 30 per cent for the BRI criterion) but also erroneously eliminates part of the background galaxy population. Comparing the convergence maps for both colour–colour selection schemes, we find the uBV selection to yield a better detection of structures in the area surrounding the cluster, indicating that suppressing contamination by unlensed galaxies is more important than a moderate loss of background galaxies from our final catalogue (see Section 5 for more details).

Since the redshift distribution of the background population peaks at $0.61 < z < 0.70$ (cyan curve in Fig. 5) we assign, in the mass modelling phase, a redshift $z = 0.65$ to background galaxies without redshift.

3.3 Shape measurements of galaxies and lensing cuts

3.3.1 Theoretical weak gravitational lensing background

The shear signal contained in the shapes of lensed background galaxies is induced by a given foreground mass distribution. In the WL regime this shear is observed as a statistical deformation of background sources. The observed shape of a source galaxy, $\varepsilon$, is directly related to the lensing-induced shear, $\gamma$, according to the relation:

$$\varepsilon = \varepsilon_{\text{intrinsic}} + \varepsilon_{\text{lensing}},$$

where $\varepsilon_{\text{intrinsic}}$ is the intrinsic shape of the source galaxy (which would be observed in the absence of gravitational lensing), and

$$\varepsilon_{\text{lensing}} = \frac{\gamma}{1 - \kappa}.$$

Here $\kappa$ is the convergence. In the WL regime, $\kappa \ll 1$, which reduces the relation between the intrinsic and the observed shape of a source galaxy to

$$\varepsilon = \varepsilon_{\text{intrinsic}} + \gamma.$$

Assuming galaxies are randomly oriented on the sky, the ellipticity of galaxies is an unbiased estimator of the shear, down to a limit referred to as ‘intrinsic shape noise’, $\sigma_{\gamma,\text{intrinsic}}$ (for more details see L07; Leauthaud et al. 2010, hereafter L10). Unavoidable errors in the galaxy shape measurement are accounted for by adding them in quadrature to the ‘intrinsic shape noise’:

$$\sigma_{\gamma}^2 = \sigma_{\text{measurement}}^2 + \sigma_{\gamma,\text{intrinsic}}^2.$$

The shear signal induced on a background source by a given foreground mass distribution will depend on the configuration of the lens–source system. The convergence $\kappa$ is defined as the dimensionless surface mass density of the lens:

$$\kappa(\theta) = \frac{1}{2} \nabla^2 \phi(\theta) = \frac{\Sigma(D_{\text{OL}}, \theta)}{\Sigma_{\text{crit}},}$$

where $\theta$ is the angular position of the background galaxy, $\phi$ is the deflection potential, $\Sigma(D_{\text{OL}}, \theta)$ is the physical surface mass density of the lens and $\Sigma_{\text{crit}}$ is the critical surface mass density defined as

$$\Sigma_{\text{crit}} = \frac{\epsilon^2 D_{OS}}{4\pi GD_{\text{OL}}D_{LS}G}.$$

Here, $D_{\text{OL}}$, $D_{OS}$ and $D_{LS}$ represent the angular distances from the observer to the lens, from the observer to the source and from the lens to the source, respectively.

Considering the shear $\gamma$ as a complex number, we define

$$\gamma = \gamma_1 + i \gamma_2,$$

where $\gamma_1 = |\gamma| \cos 2\phi$ and $\gamma_2 = |\gamma| \sin 2\phi$ are the two components of the shear, $\gamma$, defined previously, and $\phi$ is the orientation angle. With this definition, the shear is defined in terms of the derivatives of the deflection potential as

$$\gamma_1 = \frac{1}{2} (\varphi_{11} - \varphi_{22}),$$

$$\gamma_2 = \varphi_{12} = \varphi_{21},$$

with

$$\varphi_{ij} = \frac{\partial^2}{\partial \theta_i \partial \theta_j} \phi(\theta), \quad i, j \in (1, 2).$$

Following Kaiser & Squires (1993), the complex shear is related to the convergence by

$$\kappa(\theta) = -\frac{1}{\pi} \int d^2 \theta' \Re \{ \mathcal{D}(\theta - \theta')\gamma^*(\theta') \}.$$

Here $\mathcal{D}(\theta)$ is the complex kernel, defined as

$$\mathcal{D}(\theta) = \frac{\theta_1^2 - \theta_2^2 + 2i\theta_1 \theta_2}{|\theta|^4},$$

and $\Re(x)$ defines the real part of the complex number $x$. The asterisk denotes complex conjugation. The last equation shows that the surface mass density $\kappa(\theta)$ of the lens can be reconstructed straightforwardly if the shear $\gamma(\theta)$ caused by the deflector can be measured locally as a function of the angular position $\theta$.

3.3.2 The RRG method

To measure the shape of galaxies we use the Rhodes–Refregier–Groth (RRG) method (Rhodes, Refregier & Groth 2000) and the pipeline developed by L07. Having been developed for the analysis of data obtained from space, the RRG method is ideally suited for use with a small, diffraction-limited PSF as it decreases the noise on the shear estimators by correcting each moment of the PSF linearly, and only dividing them at the very end to compute an ellipticity.

The ACS PSF is not as stable as one might expect from a space-based camera. Rhodes et al. (2007) showed that both the size and the ellipticity pattern of the PSF vary considerably on time-scales of weeks due to telescope ‘breathing’. The thermal expansion and contraction of the telescope alter the distance between the primary and the secondary mirrors, inducing a deviation of the effective focus which can be repeatedly determined from a random sample of 10 stars brighter than $m_F = 23$ with an rms error of 1 $\mu$m. Once images have been grouped by their effective focus position, the few stars in each image can be combined into one large catalogue. PSF parameters are then interpolated using a polynomial fit in the usual WL fashion (Massey et al. 2002). More details on the PSF modelling scheme are given in Rhodes et al. (2007).

The RRG method returns three parameters: $d$, a measure of the galaxy size, and, the ellipticity represented by the vector $\varepsilon = (\varepsilon_1, \varepsilon_2)$.
defined as follows:
\[ e = \frac{a^2 - b^2}{a^2 + b^2}, \]
\[ e_1 = e \cos(2\phi), \]
\[ e_2 = e \sin(2\phi), \]
where \( a \) and \( b \) are the half-major and half-minor axis of the background galaxy, respectively, and \( \phi \) is the orientation angle of the ellipse defined previously. The ellipticity \( e \) is then calibrated by a factor called shear polarizability, \( G \), to obtain the shear estimator \( \gamma \):
\[ \gamma = C \frac{e}{G}. \] (2)
The shear susceptibility factor \( G \) is measured from moments of the global distribution of \( e \) and other shape parameters of higher order (see Rhodes et al. 2000). The Shear Testing Program (STEP; Massey et al. 2007) for COSMOS images showed that \( G \) is not constant but varies as a function of redshift and signal-to-noise ratio \( (S/N) \). To determine \( G \) for our galaxy sample we use the same definition as the one used for the COSMOS WL catalogue (see L07):
\[ G = 1.125 + 0.04 \arctan \left( \frac{S/N - 17}{4} \right). \]
Finally, \( C \), in equation (2), is the calibration factor. It was determined using a set of simulated images similar to those used by STEP (Heymans et al. 2006; Massey et al. 2006) for COSMOS images, and is given by \( C = (0.86^{+0.07}_{-0.05})^{-1} \) (for more details see L07).

### 3.3.3 Error of the shear estimator

As explained in Section 3.3.1, the uncertainty in our shear estimator is a combination of intrinsic shape noise and shape measurement error:
\[ \sigma^2_e = \sigma^2_{\text{intrinsic}} + \sigma^2_{\text{measurement}}, \]
where \( \sigma^2_e \) is referred to as shape noise. The shape measurement error is determined for each galaxy as a function of size and magnitude. Applying the method implemented in the PHOTO pipeline (Lupton et al. 2001) to analyse data from the Sloan Digital Sky Survey, we assume that the optical moments of each object are the same as the moments computed for a best-fitting Gaussian. Since the ellipticity components (which are uncorrelated) are derived from the moments, the variances of the ellipticity components can be obtained by linearly propagating the covariance matrix of the moments. The value of the intrinsic shape noise, \( \sigma_{\text{intrinsic}} \), is taken to be 0.27 (for more details see L07, L10).

In order to optimize the \( S/N \), we introduce an inverse-variance weighting scheme following L10:
\[ w_\gamma = \frac{1}{\sigma_\gamma^2}. \]
Hence faint small galaxies which have large measurement errors are down-weighted with respect to sources that have well-measured shapes.

### 3.3.4 Lensing cuts

The last step in constructing the WL catalogue for the MACS J0717.5+3745 field consists of applying lensing cuts, i.e. to exclude galaxies whose shape parameters are ill-determined and will increase the noise in the shear measurement more than they add to the shear signal. However, in doing so, we need to take care not to introduce any biases. We use three galaxy properties to establish the following selection criteria.

(i) Their estimated detection significance:
\[ S \frac{\text{FLUX\_AUTO}}{N} > 4.5, \]
where \( \text{FLUX\_AUTO} \) and \( \text{FLUXERR\_AUTO} \) are parameters returned by SEXTRACTOR.

(ii) Their total ellipticity:
\[ e = \sqrt{e_1^2 + e_2^2} < 1. \]

(iii) Their size as defined by the RRG \( d \) parameter:
\[ d > 0.13 \text{ arcsec}. \]

The requirement that the galaxy ellipticity be less than unity may appear trivial and superfluous. In practice it is meaningful though since the RRG method allows measured ellipticity values to be greater than 1 because of noise, although ellipticity is by definition restricted to \( e \leq 1 \). Because LENTOOL prevents ellipticities to be larger than 1, we removed the 251 objects with an ellipticity greater than unity from the RRG catalogue (2 per cent of the catalogue). Servin a similar purpose, the restriction in the RRG size parameter \( d \) aims to eliminate sources with uncertain shapes. PSF corrections become increasingly significant as the size of a galaxy approaches that of the PSF, making the intrinsic shape of a galaxy difficult to measure.

Our final WL catalogue is composed of 10170 background galaxies, corresponding to a density of \( \sim52 \) galaxies arcmin$^{-2}$. In addition to applying the aforementioned cuts, and in order to ensure an unbiased mass reconstruction in the WL regime only, we also remove all background galaxies located in the multiple-image [strong lensing (SL)] region defined by an ellipse aligned with the cluster elongation and with a semimajor axis of 55 arcsec, a semiminor axis of 33 arcsec. From the resulting mass map presented in Section 5, we a posteriori derived a convergence histogram of the pixels outside this region, and found that 90 per cent of them are smaller than \( \kappa = 0.1 \), with a mean value of \( \kappa = 0.03 \). The shear and convergence are so weak because the ratio \( D_{LS}/D_{OS} = 0.14 \) for background galaxies at redshift \( z_{\text{med}} = 0.65 \) and the cluster at \( z = 0.54 \) (see Section 4).

### 4 MASS DISTRIBUTION

The mass modelling for the entire MACS J0717.5+3745 field is performed using the LENTOOL\(^1\) (Jullo et al. 2007) software, using the adaptive-grid technique developed by Jullo & Kneib (2009) and modified by us for WL mass measurements. Because LENTOOL implements a Bayesian sampler, it provides many mass maps fitting the data that can be used to obtain a mean mass map and to determine its error.

#### 4.1 Multiscale grid method

We start with the method proposed by Jullo & Kneib (2009) to model the cluster mass distribution using gravitational lensing. This recipe uses a multiscale grid of radial basis functions (RBFs) with physically motivated profiles and lensing properties. With a minimal number of parameters, the grid of RBFs of different sizes provides higher resolution and sharper contrast in regions of higher density where the number of constraints is generally higher. It is well suited

\[^1\text{LENTOOL is available online: http://lamwws.oamp.fr/lenstool}\]
to describe irregular mass distributions like the one investigated here.

The initial multiscale grid is created from a smoothed map of the cluster $K$-band light and is recursively refined in the densest regions. In the case of MACS J0717.5+3745, this method is fully adaptive as we want to sample a wide range of masses, from the cluster core to the far edge of the $HST$/ACS field where the filamentary structure is least dense. Initially, the field of interest is limited to a hexagon, centred on the cluster core and split into six equilateral triangles (see fig. 1 in Julio & Kneib 2009). This initial grid is subsequently refined by applying a splitting criterion that is based on the surface density of the light map. Hence, a triangle will be split into four smaller triangles if it contains a single pixel that exceeds a predefined light-surface-density threshold.

Once the adaptive grid is set up, RBFs described by truncated isothermal mass distributions (TIMD), circular versions of truncated pseudo-isothermal elliptical mass distributions (PIEMD; see e.g. Kassiola & Kovner 1993; Kneib et al. 1996; Limousin, Kneib & Natarajan 2005; Elia'sdottir et al. 2007) are placed at the grid node locations. The analytical expression of the TIMD mass surface density is given by

$$\Sigma(R) = \sigma_0^2 f(R, r_{\text{core}}, r_{\text{cut}}),$$

with

$$f(R, r_{\text{core}}, r_{\text{cut}}) = \frac{1}{2G} \frac{r_{\text{cut}}}{r_{\text{core}} - r_{\text{cut}}} \left( \frac{1}{\sqrt{r_{\text{core}}^2 + R^2}} - \frac{1}{\sqrt{r_{\text{cut}}^2 + R^2}} \right).$$

Hence, $f$ defines the profile, and $\sigma_0^2$ defines the weight of the RBF. This profile is characterized by two changes in slope at radius values of $r_{\text{core}}$ and $r_{\text{cut}}$. Within $r_{\text{core}}$, the surface density is approximately constant, between $r_{\text{core}}$ and $r_{\text{cut}}$, it is isothermal (i.e. $\Sigma \propto r^{-1}$), and beyond $r_{\text{cut}}$ it falls as $\Sigma \propto r^{-3}$. This profile is physically motivated and meets the three important criteria of (a) featuring a finite total mass, (b) featuring a finite central density and (c) being capable of describing extended flat regions, in particular in the centre of clusters.

The RBFs’ $r_{\text{core}}$ value is set to the size of the smallest nearby triangle, and their $r_{\text{cut}}$ parameter is set to $3r_{\text{core}}$, a scaling that Julio & Kneib (2009) found to yield an optimal compromise between model flexibility and overfitting. We then adapt the technique proposed by Diego et al. (2007) to our multiscale grid model to fit the WL data ($\kappa \ll 1$). Assuming a set of $M$ images and a model composed of $N$ RBFs, the relation between the weights $\sigma_0^2$ and the $2M$ components of the shear is given by

$$\begin{bmatrix} \gamma_1^1 \\
\vdots \\
\gamma_M^1 \\
\gamma_1^2 \\
\vdots \\
\gamma_M^2 \end{bmatrix} = \begin{bmatrix} \Delta_1^{(1)} & \cdots & \Delta_1^{(N)} \\
\vdots & \ddots & \vdots \\
\Delta_M^{(1)} & \cdots & \Delta_M^{(N)} \\
\Delta_1^{(2)} & \cdots & \Delta_1^{(N)} \\
\vdots & \ddots & \vdots \\
\Delta_M^{(2)} & \cdots & \Delta_M^{(N)} \end{bmatrix} \begin{bmatrix} \sigma_0^{i,j} \\
\vdots \\
\sigma_0^{N,j} \end{bmatrix},$$

with

$\Delta_i^{(j)} = \frac{D_{\text{LS}}}{D_{\text{OS}}} \gamma_1^{(j)},$

and

$\Delta_i^{(j)} = \frac{D_{\text{LS}}}{D_{\text{OS}}} \gamma_2^{(j)}.$

Figure 6. Distribution of grid nodes and galaxy-scale potentials, superimposed on the $K$-band light map of MACS J0717.5+3745. Cyan crosses represent the location of 468 RBFs at the nodes of the multiscale grid; magenta circles represent galaxy-scale potentials used to describe the contribution of individual cluster members. The white dashed line defines the $HST$/ACS field of view. The white cross marks the cluster centre at 07:17:30.025, +37:45:18.58 (RA, Dec.).

where

$$\gamma_1^{(j)} = \frac{1}{2} \left( \partial_{11} \Phi_j(R_i) - \partial_{22} \Phi_j(R_i) \right),$$

$$\gamma_2^{(j)} = \partial_{12} \Phi_j(R_i) - \partial_{21} \Phi_j(R_i),$$

and

$$R_i = |\theta_i - \theta_j|.$$

In the above, $D_{\text{LS}}$ and $D_{\text{OS}}$ are the angular distances from the RBF $j$ to the background source $i$ and from the observer to the background source $i$, respectively, and $\Phi$ is the projected gravitational potential. $\gamma_{k=1,2}$ are the two components of the shear, $\Delta_i^{(1)}$ is the value of the RBF normalized with $\sigma_0^2 = 1$, centred on the grid node located at $\theta_j$, and computed at a radius $R = |\theta_i - \theta_j|$. The contribution of this RBF to the predicted shear at location $\theta_i$ is given by the product $\Delta_i^{(1)} \sigma_0^2$ (see equation 1). More details about this method will be provided in a forthcoming paper (Julio et al., in preparation).

Fig. 6 shows the distribution of the 468 RBFs superimposed on the light map used to define the multiscale grid. The smallest RBF has a $r_{\text{core}} = 26$ arcsec. Note that although LENSSTOOL can perform SL, and reduced-shear optimization, here the proposed formalism assumes weak shear with $\kappa \ll 1$. To get an unbiased estimator, we remove the background galaxies near the cluster core from the catalogue, but we keep RBFs in this region as we found it improves the mass reconstruction. In order to check our weak shear assumption, we multiply the resulting convergence map by the factor $1 - \kappa$, and find this minor correction only represents about 5 per cent at 300 kpc and less than 1 per cent at 500 kpc. It confirms that working with a weak shear assumption in this case is not biasing our results. In Fig. 8, the black dashed curve corresponds to the corrected weak shear optimization, while the black curve represents the weak shear optimization profile. Both show a really good agreement with the SL results (magenta curve).

4.2 Cluster member galaxies

Our catalogue of cluster members is compiled from the photometric catalogue of Ma et al. (2008). Within the $HST$/ACS study area we identify as cluster members 1244 galaxies with spectroscopic and/or photometric redshifts within the redshift ranges defined in

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Section 3.2. We use these galaxies’ $K_s$-band luminosities as mass estimators (see below for details).

All cluster members are included in the lens model in the form of truncated PIEMD potentials (see Section 4.1) with characteristic properties scaled according to their $K$-band luminosity:

$\rho_{\text{core}} = \rho_{\text{core}}^*(L/L^*)^{1/2}$,

$\rho_{\text{cut}} = \rho_{\text{cut}}^*(L/L^*)^{1/2}$

and

$\sigma_0 = \sigma_0^*(L/L^*)^{1/4}$.

These scaling relations are found to well describe early-type cluster galaxies (e.g. Wuyts et al. 2004; Fritz et al. 2005) under the assumptions of mass tracing light and the validity of the Faber & Jackson (1976) relation. Since the mass, $M$, is proportional to $r_0^2$, the above relations ensure $M \propto L$, assuming that the mass-to-light ratio is constant for all cluster members.

To find suitable values of $r_{\text{core}}^*$, $r_{\text{cut}}^*$ and $\sigma_0^*$ we take advantage of the results of the SL analysis of MACS J0717.5+3745 recently conducted by Limousin et al. (2012). Their mass model of the cluster also included cluster members, using the scaling relations defined above (see also Limousin et al. 2007). For a given $L^*$ luminosity, given by $m^* = 19.16$, the mean apparent magnitude of a cluster member in $K$ band, Limousin et al. (2012) set all geometrical galaxy parameters (centre, ellipticity, position angle) to the values measured with SExtractor, fixed $r_{\text{core}}^*$ at 0.3 kpc and then searched for the values of $\sigma_0^*$ and $r_{\text{cut}}^*$ that yield the best fit. We here use the same best-fitting values, $r_{\text{cut}}^* = 60$ kpc and $\sigma_0^* = 163$ km s$^{-1}$, to define the potentials of the cluster members. Hence, all parameters describing cluster members are fixed in our model; their positions are marked by the magenta circles in Fig. 6.

4.3 Mass modelling

The mass reconstruction is conducted using LENSTOOL which implements an optimization method based on a Bayesian Markov chain Monte Carlo (MCMC) approach (Jullo et al. 2007). We chose this approach because we want to propagate as transparently as possible errors on the ellipticity into errors on the filament mass measurement. This method provides two levels of inference: parameter space exploration and model comparison, by means of the posterior probability density function (PDF) and the Bayesian evidence, respectively.

All of these quantities are related by the Bayes theorem:

$\Pr(\theta | D, M) \propto \frac{\Pr(D | \theta, M) \Pr(\theta | M)}{\Pr(D | M)}$,

where $\Pr(\theta | D, M)$ is the posterior PDF, $\Pr(D | \theta, M)$ is the likelihood of a realization yielding the observed data $D$ given the parameters $\theta$ of the model $M$ and $\Pr(\theta | M)$ is the prior PDF for the parameters. $\Pr(D | M)$ is the probability of obtaining the observed data given the assumed model $M$, also called the Bayesian evidence. It measures the complexity of the model. The posterior PDF will be the highest for the set of parameters $\theta$ that yields the best fit and is consistent with the prior PDF. Jullo et al. (2007) implemented an annealed Markov chain to converge progressively from the prior PDF to the posterior PDF.

For the WL mass mapping, we implement an additional level of complexity based on the Gibbs sampling technique (see massive inference in the BayeSys manual; Skilling 1998). Basically, only the posterior distribution of the most relevant RBFs is explored. The number of RBFs to explore is an additional free parameter with a Poisson prior. Exploring possible values of this prior in simulations, we find that the input mass is well recovered when the mean of this prior is set to 2 per cent of the total number of RBFs in the model. The weights of the RBFs, $\sigma_{\gamma,j}^2$, are decomposed into the product of a quantum element of weight, $q$, common to all RBF, and a multiplicative factor $\xi_j$. In order to have positive masses, we make $\xi_j$ follow a Poisson prior (case MassInf $= 1$), and $q$ to follow the prior distribution $\pi(q) = q_0^{-2} e^{-q/q_0}$, and we fix the initial guess $q_0 = 10$ km$^2$ s$^{-2}$. The final distribution of $\sigma_{\gamma,j}^2$ is well approximated by a distribution $\pi(q)$ with $q_0 = 12$ km$^2$ s$^{-2}$, and we find that 16.8 ± 4.8 RBFs are necessary on average to reconstruct the mass distribution given our data, i.e. about 3.5 per cent of the total number of RBFs in the model. This new algorithm is fast, as it can deliver a mass map in 20 min for about 10 000 galaxies and 468 RBFs – the previous algorithm used in Jullo & Kneib (2009) was taking more than 4 weeks to converge. The new algorithm has been tested in parallel on five processors clocked at 2 GHz.

We define the likelihood function as (see e.g. Schneider, King & Erben 2000)

$\Pr(D | \theta) = \frac{1}{L_{\chi^2}} \exp \left( -\frac{\chi^2}{2} \right)$,

where $D$ is the vector of ellipticity component values, and $\theta$ is a vector of the free parameters $\gamma_j^2$. $\chi^2$ is the usual goodness-of-fit statistic:

$\chi^2 = \sum_{i=1}^{M} \sum_{j=1}^{2} \left( \gamma_{j,i} - 2 \gamma_{j,i}(\theta_i) \right)^2 / \sigma_{\gamma,j}^2$.

The $2M$ intrinsic ellipticity components ($M$ is the number of background sources) are defined as follows:

$\gamma_{\text{intrinsic},i,j} = \gamma_j(\theta_i) - 2 \gamma_j(\theta_i)$, (4)

and are assumed to have been drawn from a Gaussian distribution with variance defined in Section 3.3.1:

$\sigma_{\gamma,j}^2 = \sigma_{\gamma,j}^2 + \sigma_{\text{measure}}^2$. 

Figure 7. Contours of the convergence $\kappa$ in the MACS J0717.5+3745 field obtained using the inversion method described by Seitz & Schneider (1995), overlaid on the $K$-band light map. Magenta contours represent the 1, 2 and $3\sigma$ contours. Cyan crosses mark the position of two galaxy groups (see text for details). The white cross marks again the cluster centre (cf. Fig. 6).
The normalization factor is given by

$$Z_L = \prod_{i=1}^{M} \sqrt{2\pi \sigma_{\lambda_i}}.$$  

Note the factor of 2 in equations (3) and (4) because of the particular definition of the ellipticity in RRG (see Section 3.3.2). The logarithmic Bayesian evidence is then given by

$$\log(E) = -\frac{1}{2} \int_{0}^{1} \langle \chi^2 \rangle_{\lambda} d\lambda,$$

where the average is computed over a set of 10 MCMC realizations at any given iteration step $\lambda_i$, and the integration is performed over all iterations $\lambda_i$ from the initial model ($\lambda = 0$) to the best-fitting result ($\lambda = 1$). An increment in $d\lambda$ depends on the variance between the 10 likelihoods computed at a given iteration, and a convergence rate that we set equal to 0.1 (see BayeSys manual for details). The increment gets larger as the algorithm converges towards 1.

## 5 Results

### 5.1 Kappa map: standard mass reconstruction

We test our catalogue of background galaxies by mapping the convergence $\kappa$ in the MACS J0717.5+3749 field. We use the method described in Section 3.3.1, which is based on the inversion equation found by Kaiser & Squires (1993) and developed further by Seitz & Schneider (1995). It shows that the best density reconstructions are obtained when the smoothing scale is adapted to the strength of the signal. We find a smoothing scale of 3 arcmin to provide a good compromise between S/N considerations and map resolution. We estimate the noise directly from the measured errors, $\sigma_{\text{measurement}}$, averaged within the grid cells.

The resulting $\kappa$-map is shown in Fig. 7, overlaid on a smoothed image of the $K$-band light from cluster galaxies. We identify two substructures south-east of the cluster core whose locations match the extent of the filamentary structure seen in the galaxy distribution. The first of these, near the cluster core, coincides with the beginning of the optical filament; the second falls close to the apparent end of the filament close to the edge of our study area. A simple inversion technique thus already yields a $2\sigma$ detection of parts of the filament.

The Chandra observation of MACS J0717.5+3749 shows X-ray detections of two satellite groups of galaxies embedded in the filament (Ebeling, private communication, see also fig. 1 of Ma et al. 2009, and Fig. 10 of this paper). Their X-ray coordinates (RA, Dec., J2000) are (i) 07:17:53.618, +37:42:10.46 and (ii) 07:18:19.074, +37:41:13.14 (cyan crosses in Fig. 7). The first of these, close to the filament–cluster interface, is detected by the inversion technique, but not the second. Conversely, the peak in the convergence map in the south-eastern corner of our study area is not detected in X-rays.

### 5.2 Mass map: iterative mass reconstruction

The primary goal of this paper is the detection of the large-scale filament with WL techniques and the characterization of its mass content. To calibrate the mass map of the entire structure (i.e. filament + cluster core) and overcome the mass-sheet degeneracy, we compare the WL mass obtained for the cluster core with the technique described in Section 4, with the SL results from Limousin et al. (2012).

#### 5.2.1 Cluster core

Limousin et al. (2012) inferred a parametric mass model for the core of MACS J0717.5+3745 using SL constraints, specifically 15 multiple-image systems identified from multicolour data within a single HST/ACS tile. Spectroscopic follow up of the lensed features allowed the determination of a well calibrated mass model. The cyan contours in Fig. 9 show the mass distribution obtained from their analysis. Four mass components, associated with the main light components, are needed to satisfy the observational constraints. The cluster mass reported by Limousin et al. (2012) for the region covered by a single ACS field-of-view is $M_{\text{SL}}(R < 500 \text{ kpc}) = (1.06 \pm 0.03) \times 10^{15} h_{70}^{-1} \text{M}_\odot$ where the cluster centre is taken to be at the position quoted before (07:17:30.025, +37:45:18.58). This...
position was adopted as the cluster centre because it marks the barycentre of the Einstein ring measured by Meneghetti et al. (2011). Another SL analysis of MACS J0717.5+3745 was performed by Zitrin et al. (2009) who report a mass of $M_{\text{SL}}(R < 350 \text{kpc}) = (7.0 \pm 0.5) \times 10^{14} M_{\odot}$. This is further confirmed by a test using a low-resolution uniform grid with a pixel size of 21 arcsec.)

In Fig. 8, the SL density profile is extrapolated beyond the multiple-image region (the cluster core), while the WL density profile is extrapolated into the multiple-image region. The WL mass thus obtained for the cluster core is $M_{\text{WL}}(R < 350 \text{kpc}) = (1.04 \pm 0.08) \times 10^{15} h_{75}^{-1} M_{\odot}$ in excellent agreement with the value measured by Limousin et al. (2012). We also measure $M_{\text{WL}}(R < 350 \text{kpc}) = (5.10 \pm 0.54) \times 10^{14} h_{75}^{-1} M_{\odot}$, in slight disagreement with the result reported by Zitrin et al. (2009). But the excellent agreement at larger radii between strong and WL results without any adjustments validates our redshift distribution for the background sources and our new reconstruction method.

Fig. 9 compares the mass contours from the two different gravitational lensing analyses for the core of MACS J0717.5+3745 and illustrates the remarkable agreement between these totally independent measurements. Our WL analysis requires a bi-modal mass concentration which coincides with the two main concentrations inferred by the SL analysis of Limousin et al. (2012). This is further confirmed by a test using a low-resolution uniform grid with a pixel size of $r_{\text{core}} = 43 \text{arcsec}$ comprising 817 RBFs, for which we found a Bayesian evidence of $\log(E) = -6582$. All three grids equivalently reproduce the data. Our multiscale grid model provides an intermediate-resolution map.

Having established that the use of an adaptive grid has no detrimental effect on the Bayesian evidence, the second test consisted in locations where no structures were detected neither in the optical, nor in the mass map produced with the multiscale grid. The Bayesian evidence obtained for the uniform grid (pixel size of $r_{\text{core}} = 21 \text{arcsec}$) is $\log(E) = -6589$, compared to $\log(E) = -6586$ for the multiscale grid (pixel size of $r_{\text{core}} = 26 \text{arcsec}$). The small difference between these two values demonstrates that the reduced number of RBFs in our multiscale grid does not compromise the measurement. This is further confirmed by a test using a low-resolution uniform grid with a pixel size of $r_{\text{core}} = 43 \text{arcsec}$ comprising 817 RBFs, for which we found a Bayesian evidence of $\log(E) = -6582$. All three grids equivalently reproduce the data. Our multiscale grid model provides an intermediate-resolution map.

5.2.2 Detection of a filamentary structure

Fig. 10 shows the mass map obtained for the whole HST/ACS mosaic using the modelling and optimization method described in Section 4. Also shown are the X-ray surface brightness as observed with Chandra/ACIS-I, and the cluster $K$-band light. A filamentary structure extending from the south-eastern edge of the cluster core to the south-eastern edge of the ACS mosaic area is clearly visible in all three data sets. The projected length of the filament is measured as $4.5 h_{74}^{-1} \text{Mpc}$, and the mean density in the region of the filament is found to be $(2.92 \pm 0.66) \times 10^{15} h_{74}^{-1} M_{\odot} \text{kpc}^{-2}$. The mass concentration detected to the south-east of the cluster core corresponds to a low-mass structure comparable to a galaxy group and indeed coincides with a poor satellite cluster of MACS J0717.5+3745 that has been independently identified as an overdensity of galaxies and as a diffuse peak in the X-ray surface brightness. The second, more compact, X-ray emitting galaxy group (almost due east of the cluster core and outside the filament) is also detected.

To assess the validity of this filament detection, we test the robustness of our multiscale grid optimization method. As a first step we create a uniform grid with a RBF of size $r_{\text{core}} = 21 \text{arcsec}$ and 3169 potentials. We found that using this uniform grid added noise in locations where no structures were detected neither in the optical, nor in the mass map produced with the multiscale grid. The Bayesian evidence obtained for the uniform grid (pixel size of $r_{\text{core}} = 21 \text{arcsec}$) is $\log(E) = -6589$, compared to $\log(E) = -6586$ for the multiscale grid (pixel size of $r_{\text{core}} = 26 \text{arcsec}$). The small difference between these two values demonstrates that the reduced number of RBFs in our multiscale grid does not compromise the measurement. This is further confirmed by a test using a low-resolution uniform grid with a pixel size of $r_{\text{core}} = 43 \text{arcsec}$ comprising 817 RBFs, for which we found a Bayesian evidence of $\log(E) = -6582$. All three grids equivalently reproduce the data. Our multiscale grid model provides an intermediate-resolution map.

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Figure 10. Mass map from our weak gravitational lensing analysis overlaid on the light map of the mosaic. The two sets of contours show the X-ray surface brightness (cyan) and WL mass (white). The bold white contour corresponds to a density of $1.84 \times 10^{14} h_{74}^{-1} M_{\odot} \text{kpc}^{-2}$. The orange cross marks the location of the fiducial cluster centre, and the two blue crosses show the positions of the two X-ray detected satellite groups mentioned in Section 5.1. The dashed cyan lines delineate the edges of the Chandra/ACIS-I field of view. The yellow box, finally, marks the cluster core region shown in Fig. 9. The magenta line emphasizes the extent and direction of the large-scale filament.
in increasing the resolution of the multiscale grid to a pixel size of $r_{\text{core}} = 13$ arcsec, resulting in 2058 potentials. We found that the noise increased with the resolution, whereas all real mass concentrations maintained their size. The Bayesian evidence obtained with this high-resolution multiscale grid is $\log(E) = -6608$. A WL mass reconstruction with the high-resolution multiscale grid recovers the density profile obtained with the multiscale grid using $r_{\text{core}} = 26$ arcsec pixels. However, in view of the large difference between these two evidence values, it is clear that such an increase in resolution is not required by the data.

6 PROPERTIES OF THE FILAMENT

In this section, we first summarize briefly the results of previous studies of the MACS J0717.5+3745 filament, and then discuss the filament’s properties as derived from our WL analysis.

The detection of a filamentary structure in the field of the cluster MACS J0717.5+3745 was first reported by Ebeling et al. (2004), who discovered a pronounced overdensity of galaxies with $V - R$ colours close to the cluster redshift, extending over $\sim 4 h^{-1}_74$ Mpc at the cluster redshift. Extensive spectroscopic follow-up of over 300 of these galaxies in a region covering both the cluster and the filament confirmed that the entire structure is located at the cluster redshift, $z = 0.545$. This direct detection of an extended large-scale filament connected to a massive, distant cluster lent strong support to predictions from theoretical models and numerical simulations of structure formation in a hierarchical scenario, according to which large-scale filaments funnel matter towards galaxy clusters inhabiting the nodes of the cosmic web. Taking advantage of the opportunity provided by this special target, Ma et al. (2008) pursued a wide-field spectroscopic analysis of the galaxy population of both the cluster and the filament. Along the filament, they found a significant offset in the average redshift of over 300 of these galaxies in a region covering both the cluster and the filament. Along the filament, they found a significant offset in the average redshift of galaxies, corresponding to $\sim 630 \, \text{km} \, \text{s}^{-1}$ in velocity, as well as a decrease in velocity dispersion from the core of the cluster to the end of the filament. Ma & Ebeling (2010) studied the morphology of cluster members across a 100 $h^{-1}_74$ Mpc$^2$ area to investigate the effect of cluster environment on star formation using HST/ACS data. They explored the relation between galaxy colour and density. They showed that the 1D density profile of MACS J0717.5+3745 cluster members followed the filament from the core to beyond the virial radius falling, then slightly rising and flattening at $\sim 2h^{-1}_74$ Mpc.

To physically characterize the large-scale filament, we (1) analyse its density profile (Fig. 11); (2) study the variation of its diameter as a function of distance to the cluster core (Fig. 12); (3) derive a schematic picture of its geometry and orientation along the line of sight (Figs 13 and 14) and (4) attempt to measure the mass in stars within the entire structure (Fig. 15).

6.1 Density profiles

Fig. 11 shows the density profile across the entire study area as a function of distance from the cluster centre as defined and shown in Figs 6, 7, 9 and 10. Also shown are the profiles of the filament only (obtained by only considering the WL mass along the magenta line and within the bold white contour in Fig. 10) and the cluster. The cluster density profile is cut at $2h^{-1}_74$ Mpc from the cluster core as further, the ACS field is dominated by the filament.

As is apparent from both Figs 10 and 11, the filament connects to the cluster at a distance of about $1.5 h^{-1}_74$ Mpc from the cluster core, causing the density profile to flatten from this distance outward. The mean density in this region is $(2.92 \pm 0.66) \times 10^8 h^{-1}_74 \, \text{M}_\odot \, \text{kpc}^{-2}$. The embedded galaxy group detected also in the cluster light and at X-ray wavelengths is responsible for the peak in the density profile at a distance of about $2h^{-1}_74$ Mpc from the cluster centre. The dip in the filament profile at $\sim 2.8 h^{-1}_74$ Mpc from the cluster centre coincides with a dip visible also in projection in Fig. 10 (see Section 6.3 for more details on the 3D geometry of the large-scale filament). The filament clearly dominates the radial density profile from $\sim 2h^{-1}_74$ Mpc from the cluster centre until the edge of the HST/ACS field.

Fitting any of these profiles with parametric models (NFW, SIS, etc.) is not meaningful in view of the complexity and obvious non-sphericity of these structures. We note, however, that the overall density profile decreases as $R^{-2}$ until about $2 h^{-1}_74$ Mpc, where the beginning of the filament causes a dramatic flattening of the density profile. For illustrative purposes, Fig. 11 shows two different slopes, $R^{-1}$ and $R^{-2}$.

6.2 Filament size

We define the region of the filament on the mass map by a density threshold of $1.84 \times 10^9 h^{-1}_74 \, \text{M}_\odot \, \text{kpc}^{-2}$ which corresponds to the $3\sigma$ detection contour of the lensing mass reconstruction, and then define the central axis of the filament with respect to this contour (magenta line in Fig. 10). Under the simplifying assumption that the filament cross-section is spherical (i.e. the filament resembles a cylinder of variable radius), the filament diameter is given by the perpendicular distance of the contour to this axis. The uncertainty of this measurement is assessed by repeated this procedure for every mass map produced by LENSTOOL, and adopting the standard deviation of the results as the error of the filament diameter.

Fig. 12 shows the results thus obtained as a function of distance from the cluster centre. We find the filament’s diameter to
3D properties of the large-scale filament

In order to derive intrinsic properties of the filament from the observables measured in projection, we need to know the 3D orientation and geometry of the filament and, specifically, its inclination with respect to the plane of the sky. Ebeling et al. (in preparation) derive a model of the entire complex by comparing the measured variation in the mean radial velocity of galaxies along the filament axis to expectations from Hubble flow velocities, as well as with the predictions of peculiar velocities within filaments from numerical simulations (Colberg, Krughoff & Connolly 2005; Cuesta et al. 2008; Ceccarelli et al. 2011). A self-consistent description is obtained for an average inclination angle of the filament with respect to the plane of the sky of about 75° (Fig. 13). At this steep inclination, the 3D length of the filament reaches 18 h⁻¹ Mpc within our study region.

Using the WL mass map and the above model of the 3D geometry and orientation of the filament, we can constrain the filament’s intrinsic density. Adopting again a cylindrical geometry and the average projected values from Figs 11 and 12 we obtain a mass density of ρfilament = (3.13 ± 0.71) × 10¹³ h⁻²₄ M⊙ Mpc⁻³, or ρfilament = (206 ± 46) ρcrit.

in units of the critical density of the Universe.

We stress that this is an average value: a more complex density distribution along the filament is not only possible but also physically plausible. The density of the filament depends strongly on its inclination angle α which is reasonably well constrained on average but is uncertain at large clustercentric distances (see Fig. 13). Fig. 14 shows how sensitively the deduced density of the filament depends on α. In addition, embedded mass concentrations like the X-ray bright group of galaxies highlighted in Fig. 10 and clearly detected also in the mass surface density profile (Fig. 11) will cause local variations in the filament’s density. A more comprehensive discussion of dynamical considerations regarding the 3D geometry of the cluster–filament complex is provided in Ebeling et al. (in preparation).

6.4 Stellar mass fraction

To compute the stellar mass, M∗, across our study region we use the relation log (M∗/Lk) = az + b established by Arnouts et al. (2007) for quiescent (red) galaxies in the VIMOS-VLT Deep Survey (VVDS) sample (Le Fèvre et al. 2005) and adopting a Salpeter initial mass function (IMF). Here Lk is the galaxy’s luminosity in the K band, z is its redshift and the parameters a and b are given by a = −0.18 ± 0.03, b = −0.05 ± 0.03.

Figure 12. Diameter of the filamentary structure as a function of distance from the cluster centre. The regime of the cluster proper and the segment containing the embedded X-ray bright group of galaxies (blue cross in Fig. 10) are marked. The density threshold used to define the filamentary structure is 1.84 × 10⁵ h⁻²₄ M⊙ kpc⁻².

Figure 13. Schematic presentation of the geometry of the large-scale filament along the line of sight, as deduced from radial velocity measurements. Over the first 4 Mpc (in projection) the filament’s average inclination angle is found to be α ~ 75°. Beyond this projected distance, the filament curves increasingly towards the plane of the sky, eventually rendering its projected mass surface density too low to be detectable. In this sketch, radial velocities as observed are split into two components: peculiar velocities and Hubble flow, all expressed relative to the radial velocity of the cluster core. (Adapted from Ebeling et al., in preparation.)

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We apply this relation to the $K$-band magnitudes of all cluster members, defined using the redshift criteria presented in Section 3. The $K$-band magnitude limit of our catalogue is 23.1. The resulting projected mass density in stars is shown in Fig. 15 as a function of distance from the cluster centre. It decreases in proportion to the total projected mass density depicted in Fig. 11, as illustrated by the two different slopes, $\Sigma \sim R^{-1}$ and $\Sigma \sim R^{-2}$, shown in both figures. Hence the measured mass-to-light ratio is approximately constant across the study area, with a mean value of $(M_{\text{gal}}/L_K) = 0.94 \pm 0.41$.

To compare our result with those obtained by Leauthaud et al. (2012) for COSMOS data we need to adjust our measurement to account for the different IMF used by these authors. Applying a shift of 0.25 dex to our masses to convert from a Salpeter IMF to a Chabrier IMF, we find $(M_{\text{gal}}/L_K)_{\text{Chabrier}} = 0.73 \pm 0.22$ for quiescent galaxies at $z \sim 0.5$, in good agreement with Leauthaud et al. (2012).

The fraction of the total mass in stars, $f_\star$, i.e. the ratio between the stellar mass and the total mass of the cluster derived from our WL analysis, is $f_\star = (1.3 \pm 0.4)$ and $(0.9 \pm 0.2)$ per cent for a Salpeter and a Chabrier IMF, respectively. The latter value is slightly lower than that obtained for COSMOS data by Leauthaud et al. (2012), possibly because of different limiting $K$-band magnitudes or differences in the galaxy environments probed (the COSMOS study was conducted for groups with a halo mass comprised between $10^{11}$ and $10^{14} M_\odot$ and extrapolated to haloes of $\sim 10^{15} h^{-1} M_\odot$).

Finally, we compute the total stellar mass within our study area and find $M_{\star} = (8.62 \pm 0.24) \times 10^{13}$ and $(6.71 \pm 0.19) \times 10^{13} M_\odot$ for a Salpeter and a Chabrier IMF, respectively.

7 SUMMARY AND DISCUSSION

We present the results of a weak gravitational lensing analysis of the massive galaxy cluster MACS J0717.5+3745 and its large-scale filament, based on a mosaic of 18 $HST$/ACS images covering an area of approximately $10 \times 20$ arcmin$^2$. Our mass reconstruction method uses RRG shape measurements (Rhodes et al. 2007); a multiscale adaptive grid designed to follow the structures’ $K$-band light and including galaxy-size potentials to account for cluster members and the LENSTOOL software package, improved by the implementation of a Bayesian MCMC optimization method that allows the propagation of measurement uncertainties into errors on the filament mass. As a critical step of the analysis, we use spectroscopic and photometric redshifts, as well as colour–colour cuts, all based on ground-based observations, to eliminate foreground galaxies and cluster members, thereby reducing dilution of the shear signal from unlensed galaxies.

A simple convergence map of the study area, obtained with the inversion method of Seitz & Schneider (1995), already allows the detection of the cluster core (at more than 6σ significance) and of two extended mass concentrations (at 2–3σ significance) near the beginning and (apparent) end of the filament.

The fully optimized WL mass model yields the surface mass density shown in Fig. 10. Its validity is confirmed by the excellent agreement between the mass of the cluster core measured by us, $M_{\text{WL}}(R < 500 \text{kpc}) = (1.04 \pm 0.08) \times 10^{15} h_{70}^{-1} M_\odot$, and the one obtained in a SL analysis by Limousin et al. (2012), $M_{\text{SL}}(R < 500 \text{kpc}) = (1.06 \pm 0.03) \times 10^{15} h_{70}^{-1} M_\odot$.

Based on our WL mass reconstruction, we report the first unambiguous detection of a large-scale filament fuelling the growth of a massive galaxy cluster at a node of the cosmic web. The projected length of the filament is approximately $4.5 h_{70}^{-1}$ Mpc, and its mean mass surface density $(2.92 \pm 0.66) \times 10^8 h_{70}^{-2} M_\odot$ kpc$^{-2}$. We measure the width and mass surface density of the filament as a function of distance from the cluster centre, and find both to decrease, albeit with local variations due to at least four embedded mild mass concentrations. One of these, at a projected distance of $1.85 h_{70}^{-1}$ Mpc from the cluster centre, coincides with an X-ray detected galaxy group. The filament is found to narrow at a clustercentric distance of approximately $3.6 h_{70}^{-1}$ Mpc as it curves south and, most likely,
also recedes from us. We find the cluster’s mass surface density to decrease as $r^{-2}$ until the onset of the filament flattens the profile dramatically.

Following the analysis by Ebeling et al. (in preparation) we adopt an average inclination angle with respect to the plane of the sky of 75° for the majority of the filament’s length. For this scenario and under the simplifying assumption of a cylindrical cross-section we obtain estimates of the filament’s 3D length and average mass density in units of the Universe’s critical density of $18 \, h^{-1}_{70}$ Mpc and $(206 \pm 46) \, \rho_{\text{crit}}$, respectively. However, additional systematic uncertainties enter since either quantity is sensitive to the adopted inclination angle. These values lie at the high end of the range predicted from numerical simulations (e.g. Colberg et al. 2005), which is not unexpected given the extreme mass of MACS J0717.5+3745.

The lensing surface mass density and the spectroscopic redshift distribution suggest the consistent picture of an elongated structure at the redshift of the cluster. The galaxy distribution along the filament appears to be homogeneous, and at the cluster redshift (see Ebeling et al. 2004). This motivates our conclusion of an unambiguous detection of a large-scale filament, and not a superposition of galaxy groups projected on the plane of the sky.

Finally, we measure the stellar mass fraction in the entire MACS J0717.5+3745 field, using as a proxy the $K$-band luminosity of galaxies with redshifts consistent with that of the cluster–filament complex. We find $f_\ast = (1.3 \pm 0.4)$ and $(0.9 \pm 0.2)$ per cent for a Salpeter and Chabrier IMF, respectively, in good agreement with previous results in the fields of massive clusters (Leauthaud et al. 2012).

Our results show that, if shear dilution by un lensed galaxies can be efficiently suppressed, WL studies of massive clusters are capable of detecting and mapping the complex mass distribution at the vertices of the cosmic web. Confirming results of numerical simulations (e.g. Colberg et al. 1999, 2005; Oguri & Hamana 2011), our WL mass reconstruction shows that the contribution from large-scale filaments can be significant and needs to be taken into account in the modelling of mass density profiles. Expanding this kind of investigation to HST/ACS-based WL studies of other MACS clusters will allow us to constrain the properties of large-scale filaments and the dynamics of cluster growth on a sound statistical basis.

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