The evolution of galaxy metallicity scaling relations in cosmological hydrodynamical simulations

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ABSTRACT
The evolution of the metal content of galaxies and its relations to other global properties [such as total stellar mass (M∗), circular velocity, star formation rate (SFR), halo mass, etc.] provides important constraints on models of galaxy formation. Here we examine the evolution of metallicity scaling relations of simulated galaxies in the Galaxies-Intergalactic Medium Interaction Calculation suite of cosmological simulations. We make comparisons to observations of the correlation of gas-phase abundances with M∗ (the mass–metallicity relation, MZR), as well as with both M∗ and SFR or gas mass fraction (the so-called 3D fundamental metallicity relations, FMRs). The simulated galaxies follow the observed local MZR and FMRs over an order of magnitude in M∗, but overpredict the metallicity of massive galaxies (log M∗ ≳ 10.5), plausibly due to inefficient feedback in this regime. We discuss the origin of the MZR and FMRs in the context of galactic outflows and gas accretion.

We examine the evolution of MZRs defined using different elements that probe the three enrichment channels [SNII, SNIa, and asymptotic giant branch (AGB) stars]. Relations based on elements produced mainly by SNII evolve weakly, whereas those based on elements produced preferentially in SNIa/AGB exhibit stronger evolution, due to the longer time-scales associated with these channels. Finally, we compare the relations of central and satellite galaxies, finding systematically higher metallicities for satellites, as observed. We show that this is due to the removal of the metal-poor gas reservoir that normally surrounds galaxies and acts to dilute their gas-phase metallicity (via cooling/accretion on to the disc), but is lost due to ram-pressure stripping for satellites.

Key words: methods: numerical – galaxies: abundances – galaxies: evolution – galaxies: haloes – galaxies: high-redshift – galaxies: star formation.

1 INTRODUCTION
The study of elemental abundances in galaxies (‘metallicities’) can provide important information about their star formation histories as well as the different processes affecting gas evolution such as the balance between gas infall and outflows (e.g. Davé, Finlator & Oppenheimer 2011; Dayal, Ferrara & Dunlop 2013; Lilly et al. 2013). Moreover, the determination of correlations between the metal content of these systems and other properties such as their stellar masses (M∗) or gas fractions (f gas) is crucial for reconstructing the formation history of galaxy populations and for constraining galaxy formation models.

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Galaxies in the local Universe, z ≈ 0, exhibit a clear correlation between stellar mass and metallicity, such that systems with higher M∗ are more metal-enriched. This relationship between M∗ and metallicity (the ‘mass–metallicity’ relation, MZR) was first reported by Lequeux et al. (1979) for star-forming galaxies, with subsequent observational studies typically using luminosity as a surrogate (e.g. Garnett & Shields 1987; Zaritsky, Kennicutt & Huchra 1994; Lamareille et al. 2004). Over the last decade or so, improved data quality and larger statistical samples of galaxies have allowed for the determination of the MZR not only in the local Universe (e.g. Tremonti et al. 2004; Lee et al. 2006; Kewley & Ellison 2008) but also at higher redshifts up to z ≈ 3.5 (e.g. Savaglio et al. 2005; Erb et al. 2006; Maiolino et al. 2008; Hayashi et al. 2009; Lamareille et al. 2009; Mannucci et al. 2009; Lara-López et al. 2010; Moustakas et al. 2011; Cresci et al. 2012; Yabe et al. 2012; Yuan, Kewley &
Richard 2013; Zahid et al. 2014). Qualitatively speaking, these studies have typically found declining metallicities (at fixed stellar mass) with increasing redshift, although there are quantitative differences in the reported evolution rates.

The scatter in the observed MZR has also been extensively studied recently (e.g. Ellison et al. 2009; Yates, Kauffmann & Guo 2012; Zahid et al. 2012; Hughes et al. 2013) as it encodes information about the dependence of metallicity on secondary physical parameters. For example, Cooper et al. (2008) and Ellison et al. (2009) have shown that, at fixed stellar mass, galaxies inhabiting denser environments tend to have higher metallicities. Furthermore, higher gas-phase metallicities have been associated with lower star formation rates (SFRs; e.g. Ellison et al. 2008; Andrews & Martini 2013) and specific SFRs (e.g. Ellison et al. 2008), lower gas fractions (e.g. Zhang et al. 2009; Hughes et al. 2013), smaller sizes (e.g. Ellison et al. 2008; Yabe et al. 2014), higher dust fractions (e.g. Zahid et al. 2014) and larger $B-R$ and $R-H$ colours (e.g. Yabe et al. 2014).

The correlation of the scatter in the MZR with other physical quantities suggests that the MZR is a 2D projection of a more fundamental 3D (at least) relation. For example, Lara-López et al. (2010) and Mannucci et al. (2010) have suggested the 3D relation between $M_*$, SFR and gas-phase metallicity is more fundamental. Mannucci et al. (2010) in particular analysed the metallicity as a function of $M_*$ and SFR defining what they called the ‘Fundamental Metallicity Relation’ (FMR), in analogy with the Fundamental Plane of elliptical galaxies introduced by Dressler et al. (1987).

Since this 2D plane in 3D space is not parallel to the $M_*$–$Z$ plane, projecting the FMR on to the $M_*$–$Z$ plane introduces scatter.

Mannucci et al. (2010) defined a new quantity $\mu_\alpha = \log(M_*) - \alpha \log(\text{SFR})$ with the aim of obtaining the projection of the MZR with the minimum scatter, finding the tightest relation at $\alpha \sim 0.32$. The FMR does not appear to evolve significantly up until $z \sim 2.5$, after which the metallicity of galaxies of fixed $M_*$ and SFR starts to decline with increasing $z$ (e.g. Troncoso et al. 2014). Since the FMR consists of a positive correlation between $M_*$ and metallicity at a given SFR and a negative correlation between SFR and metallicity at a given $M_*$, part of the observed evolution of the MZR at $z < 2.5$ might be an artefact because galaxy populations that inhabit different regions of the FMR are sampled at different cosmic epochs. For example, many high-$z$ surveys are magnitude-limited in the UV, tending to select high-SFR systems. As the metal content of galaxies decreases with SFR at a given $M_*$, at least part of the observed evolution of the MZR may be a consequence of the higher SFRs of galaxies observed at high $z$. This is consistent with the recent findings of Stott et al. (2013), who select systems with similar $M_*$ and SFR to local samples and find no significant evolution out of the MZR out to $z \sim 1.5$.

While the existence of a 3D relation between $M_*$, SFR and metallicity has been verified in recent years by many groups, who have explored different redshifts and mass ranges, there is still some debate about the detailed features of the relation (e.g. Mannucci, Salvaterra & Campisi 2011; Cresci et al. 2012; Yabe et al. 2012; Henry et al. 2013; Lara-López, López-Sánchez & Hopkins 2013c; Lara-López et al. 2013b; Pilyugin et al. 2013; Stott et al. 2013; Cullen et al. 2014; Yabe et al. 2014). These discrepancies are generally related to different kinds of systematic uncertainties and selection biases that affect the observational studies and make the comparison between them non-trivial. For example, the use of different metallicity calibrations, methods for stellar mass determination and the aperture size may significantly influence the shape and zero-point of the MZR. Moreover, at high $z$, the exploration of a wide parameter space is more challenging because of the limited sample sizes. The evolution of the physical conditions of star-forming regions with cosmic time should also be taken into account as they can produce a differential evolution of metallicity indicators and locally calibrated metallicity relations may not be valid at high $z$ (Cullen et al. 2014).

There is also still some debate about whether the $M_*$–SFR–metallicity relation is truly fundamental. For example, Bothwell et al. (2013) (see also Lara-López et al. 2013a) proposed that the FMR can be considered a manifestation of a more fundamental relation between $M_{\ast}$, $\text{H I}$ mass and metallicity (the HI-FMR). These authors defined a new parametrization for projecting the MZR in this 3D space: $n_H = \log(M_{\ast}) - \beta \log(M(\text{HI}) - 9.80)$, obtaining the lowest scatter at $\beta = 0.35$. While the dependence of the metallicity on SFR saturates at high masses, the anti-correlation with $\text{H I}$ mass persists. Motivated by this work, we explore below 3D trends between $M_{\ast}$, metallicity and both SFR and gas mass fractions.

Various evolutionary scenarios have been proposed to explain the presence and evolution of the MZR (e.g. Tissera, De Rossi & Scannapieco 2005; Brooks et al. 2007; De Rossi, Tissera & Scannapieco 2007; Finlator & Davé 2008; Davé, Finlator & Oppenheimer 2011; Peeples & Shankar 2011; Davé, Finlator & Oppenheimer 2012; Yates, Kauffmann & Guo 2011; Dayal et al. 2013; Romeo Velonà et al. 2013). The lower metallicity of low-mass galaxies is generally thought to be a result of more efficient star formation driven outflows from shallower potential wells (Larson 1974; Tremonti et al. 2004; Dalcanton 2007; Kobayashi, Springel & White 2007). However, a downsizing scenario, with smaller galaxies exhibiting lower star formation efficiencies and consequently lower chemical enrichment, can also potentially lead to a correlation between mass and metallicity (Brooks et al. 2007; Mouhcine et al. 2008; Calura et al. 2009). Moreover, the infall of metal-poor gas from the IGM or through merger events has been frequently invoked as a key ingredient to reproduce the observed trends (e.g. Köppen & Edmunds 1999; Dalcanton, Yoachim & Bernstein 2004; Finlator & Davé 2008; Davé et al. 2011). In this scenario, the SF process is driven mainly by metal-poor inflowing gas, and the dilution of metal abundances by adding gas and the increased SFR resulting from a bigger gas reservoir then naturally leads to an anti-correlation between SFR and metal mass fraction $Z$. It is possible that differences in the morphological mix of galaxies and the associated changes in star formation efficiencies over time affect the evolution of the MZR (see e.g. Calura et al. 2009, for a study in this sense).

Although inflow and outflow of gas are likely to contribute to establishing the MZR, a complication to theoretical modelling is that the mass-loading of a wind, $M_w/M_\ast$, is not necessarily the same as the mass loading of a wind, $M_w/M_*$. The sub-pc wind simulations presented by Creasey, Theuns & Bower (2015) demonstrate that dense galactic discs drive metal-enriched winds, whereas lower density discs drive winds with far lower metallicities. Interestingly, de Rossi et al. (2007) showed that a correlation between metallicity and mass naturally arises in a hierarchical framework as a consequence of the regulation of the SFR by merger events, without the necessity of invoking SN-driven outflows. However, without SN feedback, they were not able to reproduce the observed slope of the relation (and neglect of SN feedback also leads to significant overcooling). Finally, the MZR need not result from the efficiency of winds as a function of stellar mass, but might simply reflect variations in the stellar initial mass function (IMF) (Köppen, Weidner & Kroupa 2007).

Although significant progress has been made in both characterizing and understanding the nature of the MZR and of the FMR, no clear consensus has emerged for either of them. In this paper, we
investigate if current models of galaxy formation and evolution are able to describe the observed trends, and if so, why. To do so we analyse the abundance evolution of star-forming regions in galaxies from the Galaxies-Intergalactic Medium Interaction Calculation (GIMIC; Crain et al. 2009) suite of cosmological hydrodynamical simulations. These simulations provide a very large sample of galaxies allowing extrapolation of statistics to the (500 Mpc h−1)3 Millennium simulation (Springel et al. 2005) volume. They are able to reproduce rare systems such as voids and massive clusters and have been shown to describe well dynamical, kinematical and abundance properties of observed galaxies (e.g. Font et al. 2011; McCarthy et al. 2012; Sales et al. 2012), and are therefore well suited to the problem at hand. We examine galaxy metallicity scaling relations and their evolution in the GIMIC simulations. In particular, we make comparisons between GIMIC and observations of the MZR (and its 3D extensions) of local galaxies, explore the evolution of metallicity scaling relations with stellar mass and circular velocity, and examine the difference between central and satellite galaxies in terms of their enrichment histories. We also analyse the abundance evolution of different elements.

The plan of the paper is as follows. The simulation and sample of galaxies are described in Sections 2.1 and 2.2, respectively. The redshift z = 0 mass–metallicity relation (MZR) is presented in Section 3.1 and compared to observations, while in Section 4, we analyse and discuss its evolution. In Section 5, we compare the metal enrichment of central and satellite galaxies in GIMIC. In Section 6, we examine the dominant processes that determine the main features of the simulated MZR. Finally, our conclusions are summarized in Section 7.

2 THE GIMIC SIMULATIONS

2.1 Cosmological parameters and sub-grid implementation

Crain et al. 2009 provide full details on the GIMIC simulations; here we begin by giving a brief overview. Five nearly spherical regions of radius R ∼ 20 Mpc h−1 were picked at redshift z = 1.5 from the Millennium simulation (Springel et al. 2005), and resimulated using ‘zoomed’ initial conditions and including hydrodynamics. In such zoomed initial conditions, the picked regions are simulated at high resolution, with the rest of the (500 Mpc h−1)3 Millennium volume represented much more coarsely with more massive dark matter particles. The five regions were selected to have mean over-densities that deviate by (−2, −1, 0, +1, +2) σ from the cosmic mean, where σ is the root mean square mass fluctuation on a scale of ∼20 Mpc h−1 at z = 1.5. These five regions sample environmentally diverse cosmological regions, ranging from massive clusters to voids. Such a zoom technique allows us to combine the advantages of having high numerical resolution with sampling a range of cosmological diverse environments.

The simulations assume a cold dark matter universe at present dominated by a cosmological constant, and use the same values for the cosmological parameters as the Millennium simulation, (Ωm, ΩΛ, Ωb, σ8, nS) = (0.25, 0.75, 0.045, 0.9, 1), where the symbols have their usual meaning. The simulations were performed with the code GADGET-3, a modified version of GADGET-2 last described by Springel 2005, and with the sub-grid ingredients for galaxy formation taken from the OverWhelmingly Large Simulations (OWLS) suite (Schaye et al. 2010) as summarized below. Hydrodynamics in GADGET code is based on the smoothed particle hydrodynamics (SPH) scheme of Lucy 1977 and Gingold & Monaghan 1977, with the cosmic gas represented by a set of particles.

Radiative cooling rates for cosmic gas are computed element-by-element in the presence of a Haardt & Madau (2001) ionizing UV/X-Ray background as a function of density, temperature and redshift using CLOUDY (Ferland et al. 1998) as described in Wiersma, Schaye & Smith (2009b). Reionization of hydrogen is assumed to take place at redshift z = 9, and of He II at redshift z = 3.5, motivated by observations of the intergalactic medium (e.g. Theuns et al. 2002).

Star formation is implemented following the prescription of Schaye & Dalla Vecchia (2008). Above a hydrogen number density threshold of ρ > 0.1 cm−3, gas can self-shield from the UV-background (e.g. Altay et al. 2011), and becomes thermally unstable (Schaye 2004). Lack of numerical resolution prevents the GIMIC simulations from following this process in detail, and our sub-grid implementation parametrizes the unresolved physics by increasing the pressure of such star-forming gas to p = p∗(p/ρ0)0.3. Taking the SFR to be the power law

\[ \dot{\rho}_* = \dot{\rho}_{*,0} (p/\rho_0)^{0.3} \] (1)

yields simulated galaxies that follow the Kennicutt–Schmidt law (Kennicutt 1998) when in hydrostatic equilibrium, with the constants \( \dot{\rho}_{*,0} \) and n directly related to the amplitude and slope of the Kennicutt–Schmidt law (Schaye & Dalla Vecchia 2008). Star formation is then implemented stochastically by converting SPH particles to collisionless ‘star’ particles with a probability set by their SFR. Note that in the case of the very recent EAGLE simulations, SFR is implemented in a very similar way but considering a metallicity-dependent SF threshold (see Schaye et al. 2015, for details).

Abundance evolution and enrichment are implemented as described by Wiersma et al. (2009a). The simulation tracks 11 elements (H, He, C, Na, N, O, Ne, Mg, S, Si, Fe)1 produced by three stellar evolutionary channels, (i) core-collapse (Type II) supernovae resulting from massive stars (\( M > 6 M_\odot \)), (ii) Type I supernovae assumed to result from catastrophic mass transfer in close binary stars, and (iii) asymptotic giant branch (AGB) stars. Stellar evolutionary tracks and yields that depend on initial metal abundance are taken from Portinari, Chiosi & Bressan (1998), Marigo 2001 and Thielemann et al. (2003).

Nucleosynthetic yields are uncertain by factors of a few as discussed in Wiersma et al. (2009a) (see also the detailed comparison of yields for a range of elements in published models by Nomoto, Kobayashi & Tomimaga 2013). Apart from uncertainties in the yields of a given element for a given stellar evolutionary channel, there is also discussion in the literature about which channels dominate for a given element. For example, Chiappini et al. (2006) argue that rotation at low metallicity significantly enhances the production of nitrogen and that this is required to solve the primary nitrogen problem for low-metallicity Milky Way stars whereas Kobayashi & Nakasato (2011) argue that AGB stars could be the source of the N at low metallicity as discussed in Nomoto et al. (2013). A detailed investigation of the abundances of different elements in different environments could help to resolve such issues. For example, Pipino et al. (2009) show how the changes in N yields as a function of metallicity that resolve the primary N problem in the Milky Way fail to predict the correct N/Fe ratio in local spheroids. In this paper we use a single set of yield tables and show that abundance patterns of galaxies nevertheless vary significantly between them because

1 Wiersma et al. (2009b) found that these elements contribute significantly to the radiative cooling at \( T > 10^4 \) K.
the extent to which a galaxy can hang-on to its own metals depends on the efficiency of feedback. This clearly complicates matters and illustrates how one cannot simply compare yield tables to observations and judge which table is the more accurate. Changing yield tables in addition to making changes in the efficiency of feedback will of course also impact the abundance evolution.

A star particle in the simulation represents a single stellar population with given age and initial abundance, assuming a Chabrier (2003) IMF. Star particles distribute the synthesized elements and total mass lost during each time-step to neighbouring gas particles according to the SPH interpolation scheme.

Kinetic feedback from SNe is implemented as described by Dalla Vecchia & Schaye (2008). After a time delay of $3 \times 10^7$ yr, the mean lifetime of a core-collapse progenitor, a star particle ‘kicks’ on average $\eta = 4$ gas particles into a wind with launch speed $v_w = 600 \, \text{km} \, \text{s}^{-1}$. The values yield a star formation history that tracks the observations well. The chosen values for the parameters ($\eta$, $v_w$) imply that 80 per cent of the available SN energy is used to drive a wind [for a Chabrier 2003 IMF with stars forming with masses in the range $0.1$–$100 \, M_\odot$, of which those more massive than $6 \, M_\odot$ undergo core collapse]. Energy injected by Type I SNe is also taken into account. It is worth noting that in this scheme the ‘kicked’ particles are not hydrodynamically decoupled at any stage.

The GIMIC simulations have been run at three levels of resolution. The low-resolution version corresponds to the original Millennium simulation (Springel et al. 2005); the intermediate and high resolution correspond to gas particle masses of $1.16 \times 10^7$ and $1.45 \times 10^6 \, h^{-1} \, M_\odot$, respectively, with the dark matter particles a factor of $\Omega_m - \Omega_b/\Omega_c = 4.56$ higher. Gravitational forces are spline-softened with equivalent Plummer-sphere softening length of $\epsilon = 0.5 \, h^{-1} \, \text{comoving kiloparsec}$ for the high-resolution run until redshift $z = 3$, and is kept constant in physical units thereafter. The intermediate-resolution simulation uses $\epsilon = 1 \, h^{-1} \, \text{kpc}$.

For most of the analysis presented below we used the high-resolution GIMIC simulation performed in the $-2$ and $0\sigma$ regions. The Appendix compares these results with those from the intermediate-resolution runs; we find that the main trends and conclusions are robust against a change in numerical resolution of a factor of 8 in mass. Below, and unless otherwise stated, we will refer to the mass fraction of elements heavier than helium as ‘metallicity’.

### 2.2 Identifying galaxies in GIMIC

We identify dark matter haloes by applying a friends-of-friends (FoF) algorithm with linking length $b = 0.2$ times the mean interparticle separation (Davis et al. 1985). We then apply the SUBFIND algorithm described in Springel, Yoshida & White (2001) and modified to include baryons by Dolag et al. (2009) to identify galaxies as self–bound structures. We will refer to the most massive SUBFIND structure of a FoF halo as its ‘central galaxy’, any other galaxy in the same FoF halo as a ‘satellite’. Unless otherwise specified, central substructures of FoF haloes are analysed in this work. To make comparison of simulated galaxies to observations more realistic, we measure properties of simulated galaxies out to a maximum distance of $R_{\text{cut}} = 20 \, \text{kpc}$ to mimic surface brightness limitations in the data.

We limit our analysis to substructures with more than 2000 particles in total, and following McCarthy et al. (2012), also require galaxies to have a stellar mass of at least $M_\ast > 10^9 \, M_\odot$ (approximately 500 star particles). We also require $M_\ast \leq 10^{10.5} \, M_\odot$ because GIMIC does not include AGN feedback and as a consequence these more massive galaxies are overcooled and have too high stellar fractions. These selection cuts result in a final sample of between 450 and 650 simulated galaxies, depending on redshift. We verified by using the five spheres of the intermediate-resolution GIMIC suite that our findings do not depend (strongly) on large-scale environment and hereafter we do not distinguish between the two different high-resolution GIMIC spheres (i.e. the $-2$ and $0\sigma$ GIMIC runs).

Finally, element abundances are stored based on both particle and SPH smoothed quantities as explained in Wiersma et al. (2009a). The SPH algorithm computes the density $\rho(r_i)$ at the location $r_i$ of particle $i$ by summing the kernel $W$ over all particles within a smoothing length $h_i$ of $r_i$.

$$
\rho(r_i) = \sum_j m_j \, W(|r_i - r_j|/h_i),
$$

(2)

where $m_j$ is the mass of particle $j$. If $A_i$ is the mass fraction in a given element for particle $j$ (i.e. its ‘particle metallicity’), then the smoothed metallicity $\tilde{A}_i$ for element $A$ of particle $i$ is calculated as

$$
\tilde{A}_i \rho(r_i) = \sum_j A_i \, m_j \, W(|r_i - r_j|/h_i).
$$

(3)

Our results do not depend on which of the two abundances we use; for simplicity we only show results corresponding to smoothed abundances below.

### 3 COMPARISON TO OBSERVED ABUNDANCE RELATIONS

#### 3.1 The mass–metallicity relation

The $M_\ast$–$Z$ relation (MZR) is a fundamental galaxy scaling relation, linking dynamics in terms of star formation, gas inflow and outflow to abundances. In this section we compare the MZR in GIMIC to the observed relation at redshift $z = 0$, which is typically inferred by measuring abundances in star-forming gas. We will therefore begin by looking at gas-phase abundance in GIMIC weighing each particle with its SFR computed as described in Section 2. The SFR-weighted abundance $\tilde{A}$ of an element $A$ of a galaxy is

$$
\tilde{A} \, M_\ast = \sum_i A_i \, m_{\ast,i},
$$

(4)

where the sum is over all gas particles $i$ in that galaxy, $m_{\ast,i}$ and $A_i$ are the SFR and abundance of element $A$ of gas particle $i$, and $M_\ast = \sum m_{\ast,i}$ is the total SFR. For simulated galaxies we calculate metallicities within the inner 20 kpc, but verified that using 10 kpc instead makes no significant difference.

GIMIC galaxies exhibit a tight correlation between gas-phase oxygen abundance weighted by SFR, and stellar mass, with more massive systems more metal rich (Fig. 1). The ratio $\text{O}/\text{H}$ increases by approximately 1 dex over the mass range $10^9$–$10^{10.5} \, M_\odot$, with approximately 1 dex of scatter at given $M_\ast$.

The observed values of $\text{O}/\text{H}$ quoted by Mannucci et al. (2010) are ~0.4 dex higher than those of Sánchez et al. (2013), but the dependence on $M_\ast$ is very similar, with $\text{O}/\text{H}$ increasing with $M_\ast$ up to $M_\ast \sim 10^{10.5} \, M_\odot$, and becoming approximately constant at higher mass. The $\text{O}/\text{H}$–$M_\ast$ relation reported by Lara-López et al. (2010) is significantly steeper. GIMIC metallicities follow the $\text{O}/\text{H}$–$M_\ast$ from Mannucci et al. (2010) up to $M_\ast \sim 10^{10} \, M_\odot$, but are higher than those data for more massive galaxies. The absence of AGN feedback in GIMIC causes overcooling in more massive objects (McCarthy et al. 2012), and the resulting high stellar fractions and lack of feedback may be responsible for the high $\text{O}/\text{H}$ values.


Downloaded from http://mnras.oxfordjournals.org/ at University of Durham on February 19, 2016
AGN feedback plays a crucial role in quenching star formation in massive galaxies (e.g. Bower et al. 2006) and models that do not consider AGN tend to overpredict stellar mass and SFRs in such galaxies. Schaye et al. (2015) present results from the EAGLE simulations which reproduce the observed galaxy stellar mass function well and show that these simulations agree well with the observed MZR also for more massive galaxies (their fig. 13). We plan to investigate the metal-enrichment history in EAGLE in a future work.

3.2 O/H dependence on SFR and gas fraction

At a given stellar mass, the O/H abundance of GIMIC galaxies decreases with increasing gas fraction, \( f_g \equiv M_g/(M_g + M_\star) \equiv M_g/M_\star \), and increasing SFR (Fig. 1, middle- and right-hand panels, respectively). Here, \( f_g \) refers to the total gas fraction — not just the fraction of star-forming gas — but we verified that similar trends appear when limiting the gas mass to star-forming gas only for lower mass galaxies with \( M_\star < 10^{10.5} M_\odot \). The limited sample size restricts us to using a small number of bins in \( f_g \) and SFR, and each bin contains \( 30-40 \) per cent of the full sample. At the low-mass end of the simulated MZR, the differences in O/H between the highest and lowest \( f_g \) and SFR bins are \( \sim 0.3 \) and \( \sim 0.2 \) dex, respectively.

The decrease in O/H with increasing \( f_g \) and SFR is also seen in the data of Mannucci et al. (2010) and Bothwell et al. (2013). The solid lines in the right-hand panel correspond to the FMR of Mannucci et al. (2010), with red and pink lines corresponding to log (SFR) = -2 and 0, respectively. Encouragingly, we find reasonable agreement in zero-point and slope of the simulated relations compared to data up to \( M_\star \sim 10^{10.5} M_\odot \). At higher \( M_\star \geq 10^{10.5} M_\odot \), GIMIC galaxies are too metal rich as noted previously.

In GIMIC, SFR is related to the gas reservoir through the imposed (subgrid) star formation law of equation (1, see Section 2), which does not simply translate to \( M_\star \propto M_\star \). However \( M_g \) and SFR are correlated in GIMIC galaxies, with galaxies with a larger total gas mass exhibiting higher SFR. By itself, this does not imply a causal connection: the correlation may be a consequence of the same phenomenon, for example an increased gas fraction and enhanced star formation may both result from a recent accretion or merger event that adds gas to the halo. Whatever the origin of the gas, some of it has low elemental abundance and makes it into the galaxy, since the abundance of star-forming gas decreases with increasing SFR. This suggests that at lower stellar mass where these correlations are strongest, accreted low abundance gas causes both the decrease in abundance, and the increase in star formation. The good agreement between the scaling relation in GIMIC and the observations then suggests that the same process may be at work in real galaxies.

Interestingly, the observed relations turn-over for more massive galaxies, \( M \sim 10^{10.5} M_\odot \), in the sense that metallicity no longer increases with \( M_\star \). As gas surely still accretes on to the haloes of these more massive galaxies, the break down of the scaling relation then suggests that the gas no longer accretes on to the galaxy. Contrasting these observed relations to what happens in GIMIC where the scaling relation does hold for these more massive galaxies suggests the cause of this: feedback. In real galaxies some process prevents the gas from accreting on to the galaxies, but not in GIMIC. We suggest it is likely AGN feedback — not included in GIMIC — that causes the turn-over in the observed MZR.

The location of observed galaxies in O/H, \( M_\star \), and SFR space is plotted in Fig. 2 (left panel). The correlations discussed so far cause observed galaxies to scatter around a (curved) 2D plane in this 3D space, and the fit of Mannucci et al. (2010) to this ‘Fundamental Plane’,

\[
12 + \log(O/H) = 8.90 + 0.37m - 0.14s - 0.19m^2 + 0.12ms - 0.054s^2, \tag{5}
\]

is shown in the left panel. Here, \( m \equiv \log(M_\star/10^{10} M_\odot) \) and \( s \equiv \log(SFR/M_\odot \text{ yr}^{-1}) \). Similar to the observed galaxies, GIMIC
compared to (Dressler et al. 1987), it is possible to choose combinations of O/H, galaxies. correlated with those found by Yates et al. (2012) in semi-analytic model in lieu of M. The more massive galaxies. stellar mass, although in detail there are differences, especially for this trend reverses for more massive galaxies (M, ≳ 10^10 M⊙) for which O/H is correlated with SFR. Such trends are consistent with those found by Yates et al. (2012) in semi-analytic model galaxies.

In analogy with the Fundamental Plane of elliptical galaxies (Dressler et al. 1987), it is possible to choose combinations of O/H, SFR and M, that minimize the scatter when seeing the FMR edge on, for example using the combination O/H and μ_m = log(M,)/log(SFR). For GIMIC, scatter is minimized for a value of α = 0.2 as compared to α = 0.32 for the data from Mannucci et al. (2010). Alternatively, in terms of η_g = log(M,)/μ_m − β log(M(H I)) − β log(M(H I)) − 9.80, GIMIC galaxies prefer β ≈ 0.2 when using the mass in star-forming gas in lieu of M(H I), and β = 0.48 when using the total gas mass, as compared to β = 0.35 for observed galaxies according to Bothwell et al. (2013). We conclude that the feedback in GIMIC induces similar correlations between abundance and SFR as a function of galaxy stellar mass, although in detail there are differences, especially for more massive galaxies.

The anti-correlation of the O/H ratio with gas fraction (f_g) and SFR at given galaxy stellar mass can be examined in more detail by analysing the f_g-M,–SFR relationship in GIMIC. To compare with observations we follow De Rossi et al. (2013) and select ‘warm’ gas with temperature^3 T ≤ 15 000 K, but note that the trends we find remain almost the same if we use the total gas component. For ~85 percent of our sample, this ‘warm’ gas component represents more than ~75 percent of the total gas content. Gas with T > 15 000 K dominates in mass in only ~7 percent of GIMIC galaxies.

The fraction of warm gas in the simulations falls with increasing stellar mass, and follows the observed relation of Stewart et al. (2009) very closely (Fig. 3). At given M, the simulated f_g increases with increasing SFR, and galaxies with little or no star formation have very little warm gas. Santini et al. (2014) reported the existence of a fundamental f_g–M,–SFR relation in observed galaxies, and the GIMIC galaxies appear to be consistent with this. Nevertheless, in the SFR bin where observations and simulations are both available, GIMIC galaxies tend to overpredict gas fractions for massive galaxies. We discuss stellar metallicities next.

3.4 Stellar metallicities

The dependence of stellar metallicity on stellar mass in GIMIC follows the data from Gallazzi et al. (2005) very closely (Fig. 4, left panel), except for the most massive galaxies (M, ≳ 10^{10.5} M⊙) which are overcooled in the simulation.\footnote{We reiterate that GIMIC imposes a pressure–density relation for dense gas, and hence does not distinguish between the warm and cold neutral medium in the ISM of a galaxy.} Also, the scatter around the median is significantly larger in the observations.

We have verified by measuring GIMIC stellar abundances in apertures (i.e. varying the value of the parameter R_in discussed earlier) that the smaller scatter in GIMIC is not likely a consequence of aperture limits. However, uncertainties in observed measurements of Z_∗ may cause the intrinsic scatter to be overestimated (see Gallazzi et al. 2005). Including satellites in our sample does increase the

\begin{equation}
12 + \log(O/H) = 8.93 + 0.79 m - 0.047 s + 0.0048 m^2 + 0.19ms - 0.015s^2.
\end{equation}

The ratio O/H depends more strongly on mass and less strongly on SFR in the simulations as compared to the data, but the overall similarity is encouraging.

This GIMIC FMR describes well the median M,–O/H relation at different SFRs. For both observed and GIMIC FMRs, O/H is anti-correlated with SFR at the low-mass end (M, ≲ 10^7 M⊙), but this trend reverses for more massive galaxies (M, ≳ 10^10 M⊙) for which O/H is correlated with SFR. Such trends are consistent with those found by Yates et al. (2012) in semi-analytic model galaxies.

In analogy with the Fundamental Plane of elliptical galaxies (MNRAS 452, 486–501 (2015))
Figure 3. Median warm gas fraction, $f_g \equiv M_g(T < 15000\text{K})/M_b$, as a function of $M_*$ at redshift $z = 0$, $M_b$ is the galaxy’s baryon mass (black solid line), with error bars indicating the 25th and 75th percentiles. The trend is in good agreement with the observed fraction from Stewart et al. (2009) (dashed black line). Coloured lines show the median of $f_g$ in the simulation for bins in star formation rate (see legend). At given stellar mass, galaxies with higher gas fractions have higher SFR.

scatter in the $M_*-Z_*$ relation, and we also find that aperture effects do affect satellites’ metallicities. It may be that observational uncertainties, and the inclusion of satellites, would be enough to reconcile observe and simulated scatter, but we have not verified this in detail.

In Fig. 4 (right panel) we explore the relation between stellar metallicity $Z_*$ and gas-phase O/H weighted by SFR. We find reasonable agreement with the data of Gallazzi et al. (2005), with the possible exception of the behaviour at low gas-phase O/H not apparent in the data. This trend in the simulations is consistent with a SF triggered by infall of metal-poor gas: in Fig. 1 we saw that most metal-poor systems have the highest gas fractions, $f_g$, and correspondingly higher SFRs.

4 METALLICITY EVOLUTION

Previously, we demonstrated that $\text{GIMIC}$ galaxies display similar trends in ISM and stellar metallicity at redshift $z = 0$ as observed galaxies. This reasonable agreement encourages us to explore the abundance enrichment history. In previous sections we have analysed only O/H as oxygen is the metal most commonly used in observational studies. In the following, we will take advantage of the enrichment evolution of all elements tracked in the simulation.

We caution the reader that our results of course apply to the particular set of yields discussed in Section 2.

4.1 Abundance evolution for different elements

The abundance evolution of different elements in the simulation is plotted in Fig. 5, depicting gas-phase abundances weighted by SFR. The O/H–$M_*$ relation (upper left panel) – commonly used as a proxy for the ‘MZR’ – does not evolve in $\text{GIMIC}$ either in slope or in normalization, and is in place at least since $z \sim 3$. We verified that this result does not depend on the aperture within which O/H is measured by changing the value of $R_{\text{cut}}$ defined earlier. In addition, we employed the redshifts used in the observational analysis of the evolution of the MZR of Maiolino et al. (2008), estimating O/H inside their observed radii: 3.0 kpc ($z \approx 3.5$), 3.6 kpc ($z \approx 2.25$), 3.725 kpc ($z \approx 0.74$) and 2.0 kpc ($z \approx 0.06$) to enable a fair comparison. Using these apertures has no effect on the slope of the O/H–$M_*$ relation, but the zero-point increases by 0.2–0.3 dex – a consequence of metallicity gradients in the simulated galaxies. Including satellites in the analysis does introduce modest evolution in O/H with $z$, with higher $z$ galaxies having lower O/H at given stellar mass (see also Section 5).

The absence of evolution in the MZR in $\text{GIMIC}$ appears inconsistent with the results of several observational studies which claim significant evolution since $z = 3$, in the sense of higher redshift galaxies having lower O/H at given stellar mass. For example, Maiolino et al. (2008) measure a decrease in O/H for galaxies with $M_* = 10^{10} M_\odot$...
Metallicities of simulated galaxies

Figure 5. Median SFR-weighted gas abundances as a function of \( M_\star \) for different redshifts \( z \) (different line styles) for different elements (different panels); error bars depict the 25th and 75th percentiles of galaxies. To ease comparison between different elements, abundances are off-set by a constant \( Y \) whose value appears in brackets in each panel (\( Y = 12 \) for oxygen, the usual normalization for that element). Top panels are for \( \alpha \)-elements produced in the simulations mainly by Type II SNe, while bottom panels are for N and C, produced by AGB stars, and Fe produced in both Type I and Type II SNe.

of 0.8 dex between redshifts \( z = 0.7 \) and \( z = 3.5 \) (their figs 7 and 8), with lower \( M_\star \) galaxies evolving even faster; at that stellar mass, \( z = 2.2 \) galaxies are less enriched than \( z = 0 \) galaxies by 0.4 dex.

A plausible explanation for the lack of strong evolution in the MZR in the simulations can be found in Weinmann et al. (2012). These authors showed that many current cosmological simulations (including GIMIC), as well as semi-analytic models, form too much stellar mass too early compared to observations. As the simulations have approximately the correct amount of stellar mass (per unit halo mass) at \( z \sim 0.1 \), this implies that the simulations will also underpredict the amount of late-time star formation. A likely consequence of this is that the MZR will be set at higher redshift in the simulations compared to real galaxies.

Alternatively, or perhaps in conjunction with the above, the presence of a strong correlation between \( O/H-M_\star \) and \( M_\star \), in simulated – and observed – \( z \sim 0 \) galaxies suggests a possible bias plausibly present in the observations: if higher \( z \) galaxies had higher \( M_\star \), due to observational selection, then their lower metallicities might be inferred to imply evolution. Indeed, observations by Stott et al. (2013) suggest a negligible evolution of the MZR from \( z = 0 \) to \( z \sim 1-1.5 \), and these authors explain the discrepancy with previous studies due to selection bias. Such an explanation is consistent with GIMIC in which low-mass galaxies follow the FMR at least up to \( z \sim 2 \).

Fig. 5 also displays the evolution of the abundances of other nuclei (X). As expected oxygen is the dominant metal by mass at all \( z \) and as such is a good proxy for metallicity. The shape of the \( X/H-M_\star \) relation and its evolution (or rather lack thereof) is almost identical for oxygen and magnesium, both of which are \( \alpha \)-elements synthesized in massive stars and released by Type II SNe. However, the Si/H relation appears to flatten towards \( z = 0 \), even though Si is yet another \( \alpha \)-element. In the yield tables that GIMIC uses for Type II enrichment (basically the yields from Portinari et al. 1998 with some modifications suggested by L. Portinari in a private communication; see Wiersma et al. 2009a for more details), the metallicity dependence of yields is similar for O and Mg: at higher metallicity, massive stars (\( M > 30 M_\odot \)) produce less O and Mg than at lower metallicity, whereas the behaviour for Si is the opposite (i.e. at higher metallicity stars tend to produce more Si than at lower metallicity). However, in all, there is little if any evolution in the MZR for any of the \( \alpha \)-elements O, Mg, and Si, with scatter in abundance significantly larger than net evolutionary trends.

The bottom left panels of Fig. 5 show evolution of nitrogen and carbon. In our models, AGB stars contribute significantly to C, and they are the dominant source of N. Abundances of N/H and C/H show significant evolution particularly from \( z = 3 \rightarrow 1 \), with an increase in abundance towards lower \( z \), accompanied by a flattening of the C/H–\( M_\star \) relation. In the nucleosynthesis models we employ, the N yield is more sensitive to metallicity than the C yield at higher abundance. This is due to the secondary element nature of N – synthesized from other metals rather just from burning hydrogen. This might cause the N abundance turn-up for more massive – and hence higher \( Z \) – galaxies, with approximately N/H proportional to \( Z^2 \). Recent changes to nitrogen yields at low metallicity discussed...
by e.g. Pipino et al. (2009) could plausibly change the evolution of N and a more detailed comparison of the present models to data could test such a model. This is, however, beyond the scope of this paper.

The strongest evolution is for iron (bottom right panel of Fig. 5), and happens mostly below $z = 2$. Iron has a significant contribution from Type I SNe which release synthesized iron with significant delay of $\sim 1$ Gyr after the formation of the progenitor star. At $M_* = 10^{10} M_\odot$, the Fe abundance increases by almost 0.3 dex between $z = 3$ and $z = 0$, and the increase is even more pronounced at lower $M_*$. Of course, these abundances are not just related to nucleosynthetic yields and how they depend on $Z$, but also to the ages of the population, and to what fraction of the elements synthesized in stars manage to remain in the ISM. GIMIC galaxies have on average similar mass-weighted stellar ages of $\sim 10$ Gyr, therefore comparing galaxies of a given stellar mass, those at lower $z$ had more time to become enriched with elements synthesized in SNIa and AGB stars, driving the observed evolution of non-$\alpha$-elements. The (unrealistically) high ages of simulated galaxies are a consequence of too early star formation in these systems, and leave them with a significant old stellar component. The absence of a $M_*-$age relation in the simulation might artificially enhance the correlations between abundances and redshift, and may also lead to an underestimate of the scatter in simulated abundances.

The metallicity evolution of the gas phase, weighted by SFR, shows only very mild evolution, with $Z$ increasing with time (Fig. 6), with a scatter between galaxies of given $M_*$ at any given time as large as the evolution of the median $Z$ from $z = 3$ to $z = 0$. Similarly to the case of stellar abundances, this is a consequence of the absence of significant evolution of O/H, and other elements may well show evolution. The different behaviour of oxygen compared to several other elements suggests that caution should be exercised when using this element just by itself as a measure of abundance evolution.

4.2 Metallicity as a function of circular velocity

One theory of the origin of the MZR is that systems with lower $M_*$ are more affected by galactic winds (e.g. Finlator & Davé 2008). Such ‘leaky’ galaxies cannot efficiently retain their ISM gas or recently produced metals, with SNe ejecting both gas and metals from the disc or indeed the halo of such galaxies (see discussion in Creasey et al. 2015). Such efficient feedback is a crucial ingredient in models of galaxy evolution (e.g. Schaye et al. 2010), and GIMIC includes a sub-grid model for launching winds. The extent to which gas mass is ejected from a galaxy by winds is thus more likely to depend on the circular velocity of the galaxy – a measure of the depth of the potential well – rather than its stellar mass, although the gas density and hence the fraction of energy in the wind lost through radiative cooling may play a role as well (Creasey et al. 2015).

We plot the dependence of gas-phase metallicity (weighted by SFR), stellar mass, and gas mass as a function of circular velocity in Fig. 7 for various redshifts. As expected, systems residing in shallower potential wells exhibit lower metallicities at all
$z$, which is consistent with these galaxies being less able to retain metals in the presence of the kinetic energy injected by SNe in our model (see also Section 4.3). Interestingly, the gas mass at a given circular velocity does not evolve with $z$. As a consequence, galaxies with given circular velocity have significantly higher specific SFRs, and significantly lower $Z$, with increasing redshift.

We have seen that the value of $Z$ at a given stellar mass does not depend strongly on redshift. On the other hand, at a given $V_{\text{circ}}$, galaxies tend to have significantly higher metallicities at lower $z$. The evolution of the $Z-V_{\text{circ}}$ relation ranges from $\sim-0.3$ dex at low velocities to $0.6$ dex or more at the high-velocity end. At first order, the evolution of the $Z-V_{\text{circ}}$ relation can be understood as a consequence of the absence of significant evolution of the $Z-M_\ast$ relation but the significant evolution of the $M_\ast-V_{\text{circ}}$ relation (middle panel; see also Swinbank et al. 2012). Galaxies with similar $V_{\text{circ}}$ (i.e. similarly deep potential wells) have a more dominant stellar component towards $z \sim 0$ and, as a consequence of the MZR, higher metallicities. Because of the more efficient gas outflows of metals at low masses, the star formation in these systems is from less-chemical enriched material on average. We also showed that at a high $V_{\text{circ}}$, the evolution of $M_\ast$ is stronger than in shallower potential wells. This issue can be probably related to the increase of the merger events for larger galaxies which do not only add the mass of the merging satellites but also contributes to the enhancement of the SF rate.

In the lower panel of Fig. 7, we show the gas-phase mass in simulated galaxies as a function of $V_{\text{circ}}$; interestingly there is almost negligible evolution. The increase of $M_\ast$ at a fixed potential well, with no significant variations of the gas mass, implies that the gas fractions of simulated galaxies decrease towards lower redshifts, consistent with the observed behaviour. This means that if the potential well of an individual galaxy does not change significantly over a given period of time and if this galaxy does not experience mergers over that period, its metallicity will increase as gas is converted into stars which enrich the ISM. In addition, as star formation proceeds consuming the gas phase, gas infall will be required to maintain an almost constant gas component.

### 4.3 Abundance imprints of galactic outflows

As we have seen, our simulations are consistent with a scenario in which galactic outflows play an important role in setting the level of depletion of metals. We further investigate this process here by contrasting the abundances of elements produced by different channels, namely SNII, SNIa and AGB stars. Outflows in GIMIC are driven by SNe explosions, which are assumed to occur $\sim 30$ Myr after star formation. Every star particle that is $30$ Myr old imparts kinetic energy in the form of a randomly directed kick with a launch velocity of $600$ km s$^{-1}$ to, on average, $\eta = 4$ of its neighbouring gas particles. Type II, Type I and AGB nucleosynthetic produce are donated to neighbouring gas particles during each time-step. Since Type II produce is distributed to neighbouring particles just before they are kicked, these elements are more likely to escape a galaxy in a galactic wind than elements produced by Type I SNe and AGB stars, whose metals are released from much older stars and after the initial SNII kick.

Wiersma et al. (2010) discuss the enrichment of cosmic metals in the OWLS suite, which used the same code, has comparable resolution to GIMIC for the high-resolution runs, but were performed in periodic boxes. These authors find that metals residing in lower density gas were typically ejected earlier and by winds driven from lower mass galaxies. Wiersma, Schaye & Theuns (2011) investigate to what extent metal enrichment depends on the relatively poorly constrained sub-grid modelling of feedback. Their fig. 12 shows that in most models stars are the dominant repository of metals at redshift $z = 0$ ($\sim 60-70$ per cent for the OWLS reference and MILL models for which the feedback implementation is most similar to that of GIMIC). However, in the AGN model that includes feedback from accretion black holes, this decreases to 20 per cent. The second main repository of metals in these models is the warm-hot intergalactic medium (WHIM). These results demonstrate that the metallicity of stars or star-forming gas in GIMIC is not just set by the star formation efficiency or yields: metal mass loss resulting from feedback indeed plays an important role. For haloes of mass below $\sim 10^{12} M_\odot$ feedback is regulated mostly by SNe-driven winds, whereas in more massive haloes AGN feedback may be more important. Note that GIMIC does not include AGN.
We plot the SF gas abundance X/Fe (X=N, S, O, Mg, C and Fe from Type I SNe only) as a function of $M_\ast$ and as a function of $V_{\text{circ}}$ at $z=0$ in Fig. 8 (left and right panels, respectively); abundances are off-set vertically so that the lines cross at $M_\ast = 10^{10} M_\odot$ ($V_{\text{circ}} = 150 \text{ km s}^{-1}$ for the right panel). The ratio $\alpha/Fe$ of $\alpha$-elements (\(\alpha= V, \text{Si, Mg which are produced in Type II SNe)}\) compared to (total) Fe increases with increasing mass up to $M \sim 10^{10} M_\odot$, then flattens for O and Mg but keeps rising for Si; a similar trend is seen in $\alpha/Fe$ as a function of $V_{\text{circ}}$. This ratio depends on the star formation time-scale, the delay time distribution of Type I SNe, and whether or not Type II produce is more likely to escape the galaxy in a wind than Type I produce. However it of course also depends on nucleosynthetic yields, which themselves depend on metallicity and hence stellar mass – this is the reason these elements do not track each other in detail in DMNC. The $X/Fe$--$M_\ast$ relations for the stellar component are similar to those of star-forming gas – modulus minor changes in the zero-point.

We mentioned in Section 4.1 that simulated galaxies have around the same mass-weighted stellar age ($\sim$10 Gyr). Given the similar mean ages of our galaxies, the slope of the $X/Fe$--$M_\ast$ relation will be significantly influenced by the effects of galactic winds at different masses. From Fig. 8 (left panel), it is clear that there is a correlation between $M_\ast$ and $X/Fe$ for C, Mg, O, Si and N and an anti-correlation between $M_\ast$ and the fraction of Fe from SNIa ($f_{\text{Fe, SNIa}}$). These results are consistent with what we would expect if low-mass systems were more affected by galactic outflows. The shallower potential wells where low-mass systems reside are less efficient in retaining metals against galactic winds generated by SNIa. On the other hand, due to the longer time-scales for the release of SNIa yields, Fe from SNIa is not directly affected by these winds, generating lower $X/Fe$. It is worth noting that C and N are mainly generated by AGB stars but the contribution from SNIa is also significant (Wiersma et al. 2009a) so that they are also affected by winds. In the right panel of Fig. 8, we can see the dependence of $X/Fe$ on the potential well of simulated galaxies. Median $X/Fe$ ($f_{\text{Fe, SNIa}}$) seem to be constant at log ($V_{\text{circ}}$) < 2.1 and increase (decrease) for larger log ($V_{\text{circ}}$), indicating that galactic winds dominate at low $V_{\text{circ}}$ values, as expected.

We note that the slope of the $X/Fe$--$M_\ast$ relation is shallower for C/Fe, probably caused by the significant contribution of AGB stars to C enrichment. A steeper slope is obtained for Si/Fe and N/Fe. In the case of Si, this may be related to the assumed yields of Portinari et al. (1998) for which Si production decreases with the metallicity of the progenitor star.

The interpretation of the trends is more convoluted for the case of N which has characteristics of both a primary and a secondary elements. At low $Z$, N production results mainly from burning the C and O generated during the star’s evolution. Consequently, its yield tracks the yields of C and O, and behaves as a primary element. However at higher $Z$, N production results increasing from burning the C and O that was already in the star from birth and N behaves more as a secondary element – the N yield no longer tracks the C/O yield but depends on $Z$. Therefore, for galaxies with low metallicity, N is expected to behave as a primary element showing no important variations in N/O while for more metal-enriched galaxies, N/O should increase with O/H as N behaves as a secondary element. Because of the tightness of the MZR (Fig. 4), the abundance of O/H is almost a proxy for $M_\ast$. This reasoning explains why the dependence of N abundance on $M_\ast$ steepens increasingly with increasing $M_\ast$, as seen in Fig. 8. The behaviour of O/H with stellar mass may be different if nitrogen were produced abundantly in low-$Z$ fast-rotating stars, as in the models of Pipino et al. (2009).

The study of the stellar $X/Fe$ as a function of $M_\ast$ for elliptical galaxies is discussed extensively in the literature (see e.g. Conroy, Graves & van Dokkum 2014). Although a detailed analysis is beyond the scope of the present paper, we did perform a preliminary analysis of the stellar $X/Fe$--$M_\ast$ relation using a subsample of galaxies with large velocity dispersion, typical of elliptical systems. We find larger average values of [Mg/Fe], [Si/Fe] and [N/Fe] than reported by Conroy et al. (2014) by $\sim0.1$ dex, $\sim0.3$ dex and $\sim0.15$ dex, respectively. Observational uncertainties are of the order of 0.05 dex (Conroy et al. 2014) and differences with other observational works are of the order of $\sim0.1$ dex. Uncertainties in yields, and in the rates of SNIa, may be enough to explain the remaining differences.

Finally, we compare the abundance evolution of yields from SNIa and SNIa as a function of $M_\ast$ and $V_{\text{circ}}$ (Fig. 9) by plotting the fraction of Fe produced by SNIa. We see a significant trend of increasing SNIa Fe/total Fe with decreasing $z$, and decreasing $M_\ast$ (or $V_{\text{circ}}$). The evolution with $z$ is stronger for lower mass galaxies. These trends are consistent with our findings that Type II products escape more easily from lower mass galaxies, and with the delay of SNIa enrichment. We reiterate that we may be overestimating the SNIa

![Figure 9](http://mnras.oxfordjournals.org/)

Figure 9. Median mass fraction of Fe from SNIa in star-forming gas as a function of $M_\ast$ (left panel) and $V_{\text{circ}}$ (right panel) for various redshifts (different curves); error bars denote 25th and 75th percentiles. The contribution to total Fe from Type I SNe increases with time as expected from the delayed production of Type I Fe in the model. The dependence with $M_\ast$ (or $V_{\text{circ}}$) due to more significant loss of SNI products from shallower potentials also becomes more pronounced at later times.
contributions especially for lower mass galaxies, because the stars in our low-mass galaxies tend to be too old on average.

5 SATELLITE GALAXIES

In Section 2, we defined a central galaxy as the most massive SUBFIND structure in a given FoF halo – all other galaxies in that halo are satellites. Here we investigate abundance trends in satellites using the same criteria as for centrals regarding number of particles and mass range (see Section 2.2). Consequently, our sample will only include the most massive satellites; typically only 20–30 per cent of the total depending on redshift.

The MZR of satellites and central galaxies at $z = 0$ are compared in Fig. 10. At given $M_*$, satellites are on average more metal rich than centrals by $\sim 0.1–0.2$ dex, and their metallicity scatter is higher than for centrals ($\sim 0.5$ dex for satellites compared to $\sim 0.1–0.2$ dex for centrals), mainly at intermediate masses $M_* \sim 10^{10} M_\odot$. As we noted in Section 3.4, the inclusion of satellites in the analysis of the MZR based on stellar abundances tends to increase the scatter. Our findings indicate that this is also true for gas abundances; their inclusion also results in an offset to higher $Z$.

Pasquali, Gallazzi & van den Bosch (2012) compare the MZR of satellite and central galaxies inferred from Sloan Digital Sky Survey data, finding that satellites tend to have higher metallicities than central systems at a given $M_*$ by $\sim 0.06$ dex, with the offset increasing with decreasing $M_*$. We find a slightly larger offset, and no obvious trend with $M_*$ except at the very massive end. Previously we explained why varying the size of the aperture within which $Z$ is measured affects the zero-point of the MZR because of abundance gradients; we find the same to be true for satellites. It is possible that this affects the interpretation of the data from Sloan Digital Sky Survey due to the size of the fibres.

What is the origin of the differences in $Z$ between satellites and centrals? At a given $M_*$, satellites reside in shallower potential wells than central galaxies as expected: their $V_{\text{circ}}$ are lower by $\sim 0.05$ dex than those of central galaxies of similar masses. Moreover, the $f_\text{esc} - M_*$ relation of satellite galaxies is offset by $\sim 0.2$ when compared to centrals, mainly due to the loss of non-star-forming gas. This lower gas fraction of satellites is consistent with these systems being subject to strangulation and ram-pressure stripping. We also find that the scatter in $f_\text{esc} - M_*$ (and $f_\text{esc} - V_{\text{circ}}$) is larger for satellites than for centrals. These findings are consistent with a scenario in which satellite galaxies lose the metal-poor gas in their outskirts due to ram-pressure stripping. This gas is then no longer available to dilute the ISM of the satellite, which leads to them having a higher $Z$. The larger scatter in $f_\text{esc}$ is also consistent with the larger scatter in $Z$ at given $M_*$ in satellites compared to centrals. Such a scenario can potentially explain both the offset and increase in scatter in $Z$, but we postpone a more detailed investigation to future work.

The evolution of the MZR for satellites is shown in Fig. 11, which can be compared to the evolution for centrals in Fig. 5. We recall that the ratio $O/H$ – a good proxy for $Z$ – does not show any appreciable evolution for centrals. In contrast, $Z$ does evolve for satellites, increasing from $z = 3$ to $z = 0$ by $\sim 0.2$–0.4 dex, depending on $M_*$. Interestingly at $z \sim 3$, satellites and centrals have MZRs with similar amplitude and slope. We have verified that simulated satellites inhabit haloes typically 10 times more massive than centrals at a given $M_*$, which contributes to the higher metallicity of satellites.

6 DISCUSSION

Galaxies in the GIMIC simulation follow a MZR consistent with that observed, although the evolution of the MZR may be less than that observed. We argued this may be at least partly a consequence of bias in the observations. As shown in Sections 4.2 and 4.3, the slope of the MZR is to the first order set by the efficiency with which galactic winds can escape the potential well. In particular, Type II SN products such as oxygen escape more readily from shallower potential wells. Since oxygen is often used as a proxy for metallicity $Z$, ‘metals’ also escape more easily from shallower ISM may play an important role as well (Creasey et al. 2015). We
also noted in Section 3.1 that the simulated MZR does not exhibit the observed flattening at the high mass end, which we counted on the absence of AGN feedback in GIMIC. We conclude that feedback from SNe modulates the slope of the MZR at low and intermediate masses while the flattening at higher masses is increasingly affected by AGN.

While galactic winds appear to be the main process for setting the slope of the MZR, its zero-point is also affected by the SF timescales. The zero-point of the X/H–\(M_\ast\) relation for the \(\alpha\)-elements produced by short-lived stars does not exhibit significant evolution since \(z \approx 3\). We may have underestimated the level of evolution in \(\alpha\)-elements because our galaxies tend to be too old. However, the ratio X/H–\(M_\ast\) at given \(M_\ast\) does evolve for elements produced by SNeIs and AGB stars, and the level of enrichment is connected to the SF time-scale.

Applying observed aperture corrections and including satellites in our analysis increase the level of evolution by up to \(~0.4\) dex; however it is still not as strong as many observers infer. We believe this is at least partly due to the fact that stellar populations in the simulation are typically older than in the real Universe, plausibly because feedback in the simulation is not sufficiently effective at early times (see also Weinmann et al. 2012; De Rossi et al. 2013). In addition we find that typical specific SFRs in GIMIC are too low at redshift \(z = 0\), in particular for low-mass galaxies, as also found by McCarthy et al. (2012) who blamed this partly on lack of numerical resolution. We note, however, that the overall MZR is not strongly affected by resolution, as demonstrated in the Appendix. In the recent EAGLE simulations (Schaye et al. 2015), feedback becomes more efficient at higher density which suppresses star formation at early times and increases the specific star formation at later times. This may help to increase the level of evolution in the simulations.

With respect to the scatter in the MZR, our findings indicate that at a given \(M_\ast\), metallicities show a secondary dependence on \(f_\text{gas}\), where galaxies with lower metallicities tend to have higher \(f_\text{gas}\) and higher SFRs, consistent with the observed trends. Therefore, the SF process in these systems is driven mainly by accretion of metal-poor gas.

Interestingly, we find that, at a given \(M_\ast\), systems with lower gas-phase metallicities tend to exhibit higher \(V_\text{circ}\). Therefore, at a given \(M_\ast\), systems with deeper potential wells have larger fractions of gas which is also more metal-poor. Such a correlation suggests that the depth of the potential well at a fixed \(M_\ast\) is regulating the infall of metal-poor gas and, hence, the scatter in the MZR. In addition, at a fixed \(M_\ast\), the radius which encloses 50 per cent of the stellar component (\(R_\text{50}\)) tends to be larger for systems with lower metallicities, evidencing again the more significant influence of gas infall in these galaxies.

In summary, the zero-point of the MZR in the GIMIC simulations is at first order set by the star formation time-scale, and the efficiency of galactic winds, respectively. The scatter around the relation is affected by the gas fraction, itself correlated with the depth of the potential of a galaxy of given mass. The MZR of satellites is offset to higher \(Z\) compared to centrals of the same mass, and its scatter and level of evolution are significantly higher. We verified that ram-pressure stripping and the metal pollution of the host haloes in which satellites live seem to play a key role on modulating their metal enrichment.

7 CONCLUSIONS

We have analysed the GIMIC hydrodynamical simulations of structure formation to study the abundances of different elements in star-forming gas in galaxies as a function of galaxy stellar mass and redshift. We focused mainly on the analysis of central substructures of dark matter haloes (‘central galaxies’) but we also looked at satellite systems. Our main conclusions can be summarized as follows.

(i) GIMIC galaxies exhibit a well-defined correlation between O/H and \(M_\ast\) at \(z = 0\) in the sense that more massive galaxies are more metal-enriched, in agreement with observations (Fig. 1). However, at the high-mass end (\(M_\ast \gtrsim 10^{10.5} M_\odot\)) simulations predict higher abundances than observations. We suggest that the inclusion of AGN feedback in the model would help to overcome this problem by preventing overcooling in massive galaxies.

(ii) Consistent with observations, the scatter of the O/H–\(M_\ast\) relation is driven by a secondary dependence of metallicity on the gas fraction (\(f_\text{gas}\); Fig. 2). At given \(M_\ast\), galaxies with lower metallicities tend to have higher \(f_\text{gas}\), higher SFRs, inhabit deeper potential wells and have larger half-mass radii. Such correlations are expected if star formation in galaxies is self-regulating (Schaye et al. 2010) with feedback regulating inflow of more metal-poor gas.

(iii) The simulations are able to reproduce the correlation between O/H, \(M_\ast\), and SFR of the fundamental mass–metallicity relation (FMR) of observed galaxies of Mannucci et al. (2010). Our results are also consistent with the existence of a correlation between O/H, \(M_\ast\), and f\text{gas}. Following observational parametrizations of the FMR, we analysed the parameters \(\mu_\text{g}\) and \(\eta_\text{g}\). We found that \(\beta \approx 0.48\) leads to the tightest relation with O/H, reducing the scatter by \(~0.03\) dex with respect to the O/H–\(M_\ast\) relationship. Our findings show also evidence for a correlation between \(f_\text{gas}\), \(M_\ast\), and SFR, consistent with the observations by Santini et al. (2014). At a given \(M_\ast\), simulated systems with higher \(f_\text{gas}\) tend to have higher SFRs. The simulated \(f_\text{gas}–M_\ast\) relation for the cold gas is in remarkably good agreement with observations.

(iv) The Z–\(M_\ast\) relation in GIMIC agrees well with observations in both slope and zero-point (Fig. 4); however the scatter in the simulations is lower. Including satellites in the analysis, and taking into account aperture effects increases the scatter in the simulation considerably.

(v) There is negligible evolution of the O/H–\(M_\ast\) relation between \(z = 3\) and \(z = 0\) (Fig. 5), in apparent disagreement with observations. Taking into account satellite galaxies – that do evolve – and aperture effects leads combined to a small evolution of \(~0.4\) dex from \(z = 3\) to \(z = 0\), still considerably less than the claimed 1 dex evolution in the data. In GIMIC, galaxy stellar ages tend to be uniformly old, \(~10\) Gyr which contributes to the disagreement – modifying the stellar feedback efficiency as in the recent EAGLE simulations (Schaye et al. 2015) might resolve some of the discrepancy. However, we suggest that observational bias in the data may be the main culprit.

(vi) The evolution of the abundance ratios (X/H) as a function of galaxy stellar mass, for various other elements X tracked in the simulation, depends strongly on the stellar evolutionary channel that produces X (Fig. 5). \(\alpha\)-elements produced by massive stars show very little evolution, whereas elements with significant SNI or AGB contributions show stronger evolution. Therefore, the total metallicity \((Z)\) of the gas evolves in the sense that at a given mass, systems were less enriched in the past. The different behaviour of these elements can be understood in terms of (i) the ejection of SNI produce in galactic winds, and (ii) the stellar evolutionary time-scale for SNI and AGB stars. Galactic winds are driven by the same Type II SNe that also release \(\alpha\)-elements, and such metal-enriched winds escape easily from small galaxies living in a shallow potential well.
If the stars in these galaxies are old enough to produce SNI and AGB stars, then elements produced predominantly by SNI and AGB stars dominate the abundance pattern. More massive galaxies from which winds cannot escape easily are then relatively more abundant in $\alpha$-elements. We focused mainly on the comparison of the slope of the different abundance ratios as the theoretical yields are uncertain by a factor of a few. A comparison between results presented here and those derived from other yields models available in the literature would be very interesting.

(vii) Satellites are more metal rich than centrals at given $M_*$ in agreement with observations, and the scatter around the mean relation is significantly larger for satellites (Fig. 10). The inclusion of satellites in the analysis of the MZR could increase the scatter of the relation, leads to an offset, and introduces evolution.

Satellites have similar amounts of star-forming gas, and similar SFRs as central galaxies at a given $M_*$. However, they have less gas in total, probably because of strangulation and ram-pressure stripping (see also Bahé et al. 2013; Bahé & McCarthy 2015, for a more extensive study of the satellite galaxy population in GIMIC). Their depletion in gas contributes to their higher metallicities.

The MZR in GIMIC is mostly determined by the star formation time-scales and the efficiency of SN feedback as a function of galaxy stellar mass. SN feedback is efficient in shaping the relation at low and intermediate masses, $M_* \lesssim 10^{10.5} \, M_\odot$, but at higher masses the absence of AGN feedback in the simulation leads to unrealistically massive galaxies. The evolution of the zero-point of the MZR seems to be directly related to the SF time-scales. Since GIMIC galaxies have a dominant older stellar component, the MZR based on $\alpha$-elements alone does not evolve significantly. We suggest that an improvement of the feedback prescription as implemented in EAGLE (Schaye et al. 2015) might affect this. At second order, the simulated MZR shows dependencies on the infall of metal-poor gas. At a given $M_*$, systems with deeper potential wells seem to accrete more metal-poor gas increasing their SFRs. These findings are consistent with previous proposed scenarios in the literature.

Finally, although there are still important discrepancies between observational studies with respect to the shape, zero-point and evolution of the MZR and its 3D extensions, the advances of the observational techniques are shedding more light on the abundance evolution of galaxies over cosmic time. The continued comparison between these observations with theoretical models of galaxy formation not only offers a fruitful means for testing/constraining the models, but also helps to guide those studies and provide plausible formation scenarios. A significant combined effort will be required from the theoretical and observational sides in order to converge to a complete understanding of the abundance enrichment history of galaxies.

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APPENDIX A: RESOLUTION STUDY

The analysis presented in this paper has been done by using the high resolution version of GIMIC simulations (see Section 2).
Figure A2. Stellar metallicity as a function of stellar mass at $z \geq 0$ for central galaxies in the high-resolution run (black) and intermediate-resolution run (red). The different curves with error bars depict the median relation with the 15th and 85th percentiles. Convergence is good, with a small tendency for higher values of $Z$ at higher resolution.

In order to assess the numerical convergence of our results, we have also performed a similar analysis by using the intermediate-resolution runs, which has eight times coarser mass resolution. Our results are robust to a factor of 8 change in mass resolution.

As an example, we compare the MZR based on SF-weighted gas and stellar metallicities at two resolutions in Figs A1 and A2, respectively. We see that the main features of the relations seem to be robust against resolution. There is only a very small trend in the case of the intermediate-resolution run to have lower abundances at the high-mass end towards higher redshifts.

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