A Froude-scaled model of a bedrock-alluvial channel reach: 1. Hydraulics

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\section*{Abstract}
The controls on hydraulics in bedrock-alluvial rivers are relatively poorly understood, despite the importance of the flow in determining rates and patterns of sediment transport and consequent erosion. To measure hydraulics within a bedrock-alluvial channel, we developed a 1:10 Froude-scaled laboratory model of an 18 × 9 m bedrock-alluvial river reach using terrestrial laser scanning and 3-D printing. In the reported experiments, water depth and velocity were recorded at 18 locations within the channel at each of five different discharges. Additional data from runs with sediment cover in the flume were used to evaluate the hydraulic impact of sediment cover; the deposition and erosion of sediment patches in these runs are analyzed in the companion paper. In our data (1) spatial variation in both flow velocity and Froude number increases with discharge; (2) bulk flow resistance and Froude number become independent of discharge at higher discharges; (3) local flow velocity and Reynolds stress are correlated to the range of local bed topography at some, but not most, discharges; (4) at lower discharges, local topography induces vertical flow structures and slower velocities, but these effects decrease at higher discharges; and (5) there is a relationship between the linear combination of bed and sediment roughness and local flow velocity. These results demonstrate the control that bedrock topography exerts over both local and reach-scale flow conditions, but spatially distributed hydraulic data from bedrock-alluvial channels with different topographies are needed to generalize these findings.

\section*{1. Introduction}
The reach-scale form and function of river channels is determined by interactions between channel topography, flow, and sediment transport. Although these relationships are increasingly well understood in self-formed alluvial channels, they remain poorly defined in bedrock-alluvial channels (bedrock-alluvial encompasses all channels with a predominantly bedrock boundary and any amount of sediment cover, sensu Turowski \textit{et al.} [2008]). Bedrock channels typically erode slowly, so their topography evolves in response to multiple large flow events [Whipple, 2004; \textit{Wohl and David}, 2008]; in contrast, alluvial channels can be reconfigured during a small number of events and within a single event in some cases [\textit{Gupta and Fox}, 1974; \textit{Wells and Harvey}, 1987; Milan, 2012]. Consequently, in the context of the relationships between topography, flow, and sediment transport, the morphology of bedrock channel boundaries is largely imposed by past conditions and geology, rather than being internally generated in response to the current flow regime. Our aim is to demonstrate how flow and sediment dynamics are controlled by the morphology of the bedrock channel bed, which is static over the timescales of interest and potentially out of equilibrium with the flow regime.

This aim is addressed using a Froude-scaled physical model of a bedrock reach, in which key hydraulic and sediment properties are scaled. Channel topography measured in the field using Terrestrial Laser Scanning (TLS) was reproduced at 1:10 scale in a flume using 3-D printing. In the flume experiments hydraulics and sediment dynamics were measured across a range of discharges and in runs with sediment supply volumes in a range upward from zero. This physical model overcomes many of the limitations of field data, such as measuring the spatial pattern of hydraulics and sediment cover under high discharges, and quantifying discharge and sediment supply. This paper focuses on the impact of channel topography on hydraulics, where channel topography encompasses both bedrock topography and surficial sediment cover. The companion paper addresses the impact of bedrock topography on the formation and stability of sediment cover.
2. Background and Research Questions

2.1. Feedbacks Between Morphology, Flow, and Sediment Cover

The formative relationships between flow, channel morphology, and sediment transport are different between alluvial and bedrock-alluvial systems. In alluvial systems at up to reach scale, adjustments to the channel boundary and bedforms within the timescale of a single event enable the system to respond relatively quickly to changes in external forcing. However, in bedrock-alluvial systems, channel morphology is composed of both bedrock morphology and sediment cover. These two phases have very different timescales of response; substantial changes in sediment cover can occur during a single event, whereas bedrock erosion typically occurs over far longer timescales and can be considered to be a fixed, independent variable over timescales that is relevant for many geomorphological studies [Schumm and Lichty, 1965; Tinkler and Wohl, 1998].

The extent to which bedrock morphology is in equilibrium with the current hydrological regime is a function of the erodibility of the bedrock and the frequency of erosion-causing events. Although there are documented examples of significant bedrock incision within individual events [e.g., Cook et al., 2013; Baynes et al., 2015], calculation of a response timescale also needs to account for all the events where erosion does not occur. Consequently, the morphology of a bedrock-alluvial channel reflects the cumulative effect of flow and sediment supply over decades to millennia or longer [Wohl and David, 2008]. The current morphology may even reflect a regime that no longer exists, for example, a period of enhanced incision has been identified during postglacial periods of high sediment supply in Scottish rivers [Jansen et al., 2011; Whitbread et al., 2015]. Wohl and David [2008] found that bedrock-alluvial rivers exhibit a similar hydraulic scaling between discharge and channel geometry to alluvial rivers, but with the difference that discharge was defined as the largest identifiable event rather than a higher-frequency flow, such as mean annual or bankfull discharge, as used in alluvial channels [e.g., Leopold and Maddock, 1953]. The recurrence interval of the largest identified discharge is subject to considerable uncertainty but was estimated as ranging from a few decades to a few centuries. Consequently, bedrock-alluvial channel morphology is likely to be out-of-equilibrium with the more frequent, smaller flow events which are responsible for the majority of sediment transport, and so the relationships between channel morphology and other components of the fluvial system (hydraulics, sediment transport and cover) are likely to be different to those in alluvial systems.

2.2. Hydraulic Processes in Bedrock-Alluvial Systems

The interactions between flow and channel morphology in bedrock-alluvial systems reflect the same physical processes as occur in alluvial channels [Richardson and Carling, 2006], but there are reasons to expect significant differences in the nature of these interactions between river types. Bedrock-alluvial channels tend to be steeper [Montgomery et al., 1996], are more likely to have morphological discontinuities such as knickpoints at a range of scales, often have resistant bedrock walls rather than erodible banks, and are morphologically adjusted to low-frequency flow events [Wohl and David, 2008]. It has been suggested that bedrock-alluvial channels commonly have flow close to or at critical, with Froude (Fr) numbers near or equal to 1 [Tinkler and Wohl, 1998], although supercritical flows have been identified under high discharges [Turowski and Rickenmann, 2009] and in steep reaches. Clustering around Fr = 1 suggests a form of internal hydraulic regulation associated with energy dissipation, consistent with suggestions that critical flow can become a controlling factor in streams where width is constrained [Huang et al., 2004].

Field observations in bedrock-alluvial channels indicate that flow resistance initially decreases with increasing discharge, before stabilizing at higher discharges [e.g., Richardson and Carling, 2006; Heritage et al., 2004; Van et al., 2012]. Very low discharges are characterized by nonuniform flow, with alternating pools and supercritical flow over bedrock steps [Richardson and Carling, 2006]. Energy is dissipated by hydraulic jumps, internal distortion in the flow, and the physical roughness of bedrock outcrops [Heritage et al., 2004; Van et al., 2012]. As discharge increases, flow becomes more uniform, with few dead zones and a progressive increase in Fr and decrease in flow resistance. Richardson and Carling [2006] termed this state the macroturbulent mixing state (MMS), which is characterized by frequent eddy shedding from irregularities in the channel bed and high turbulent intensities as the area of the bed wetted by the flow progressively expands. The MMS is fully established at a threshold discharge above which there is no further decrease in flow resistance.
At higher discharges, Richardson and Carling [2006] identified a second state, where the flow separated into a central core of critical flow with marginal slack water zones, termed the decoupled dead zone state (DDZS). The switch occurred concurrently with the flow asymptotically approaching $Fr = 1$, suggesting that the development of a shear layer provides internal regulation that prevents the flow from becoming supercritical [Tinkler, 1997]. Venditti et al. [2014] identify similar 3-D turbulent structures related to longitudinal discontinuities in the beds of bedrock canyons. Another possible mechanism, hypothesized by Grant [1997], is that flows asymptotically approach $Fr = 1$ because of interactions between the free surface and channel bed; small irregularities in the bed surface produce hydraulic jumps and surface waves, which rapidly dissipate energy. Wall undulations may play a similar role [Wohl et al., 1999], with Richardson and Carling [2006] suggesting the decoupling they observed could be caused by the relatively rougher channel side walls starting to become submerged. One apparent contradiction is that these energy dissipation mechanisms are equivalent to a progressive increase in flow resistance with stage, yet field measurements suggest that this is more than compensated by drowning out of bed roughness as flow stage rises. The extent to which these different states are generally found in bedrock-alluvial channels remains to be assessed.

2.3. Hydraulic Data From Bedrock-Alluvial Systems

The ability to address questions around channel hydraulics and changing flow resistance is limited by the availability of hydraulic data from bedrock-alluvial channels. Since Tinkler’s [1997] velocity data from a single cross section at different discharges, very few comparable data sets have been collected. Venditti et al. [2014] present high-resolution hydraulic data from a series of bedrock canyons to analyze the flow structures induced by the lateral constriction of the canyons, giving specific findings that are not applicable to a broader range of bedrock-alluvial channels. Similar limited generality applies to hydraulic data from flume experiments. For example, the experiments of Johnson and Whipple [2010] and Finnegan et al. [2007] were based on a self-formed channel that tended to evolve into a tortuous slot canyon, with the shallow flows making hydraulic measurements difficult. Other flume experiments have only recorded reach-average conditions [Chatanantavet and Parker, 2008; Inoue et al., 2014]. Finally, flume experiments tend to have far higher $Fr$ numbers than are hypothesized to occur in natural bedrock-alluvial channels; for example, reported flume $Fr$ numbers are 2.4 to 3.5 [Johnson and Whipple, 2010], ~1.4 [Finnegan et al., 2007], and up to 2.4 [Chatanantavet and Parker, 2008]. These limitations mean that there is, therefore, a need for spatially distributed data sets of hydraulic measurements from bedrock-alluvial channels with which to assess their behavior.

2.4. Hydraulic Processes, Bedrock Roughness, and Sediment Cover

The previous work discussed above addressed changes to reach-scale hydraulics as a function of discharge but did not try to quantify the impact that a particular channel topography has on the hydraulics. Even at the reach scale, it is still unclear how the roughness (a measure of the bed topography) and flow resistance (calculated from hydraulic data) of a bedrock-alluvial channel should be quantified, and how these properties change as sediment patches develop. Different methods have been proposed for quantifying channel topographic roughness. In flume experiments, Johnson and Whipple [2007, 2010] and Finnegan et al. [2007] used the standard deviation of elevations relative to a plane fitted to the surface. This physically meaningful property [Coleman et al., 2011] appeared to correlate with the development of sediment cover and channel incision. An alternative flow resistance approach back-calculates a roughness length from hydraulic data (typically average depth and velocity) and a relationship such as the Manning-Strickler formula [Chatanantavet and Parker, 2008; Johnson, 2014]. However, Chatanantavet and Parker [2008] and Inoue et al. [2014] found that there was not a good correlation between the roughnesses obtained from topographic and flow resistance methods for different surfaces. These data, therefore, question the extent to which a single topographic index records the influence of the bed morphology on the flow.

Attempts to quantify bed roughness and flow resistance are further complicated by the development of sediment cover. Johnson [2014] and Inoue et al. [2014] both developed approaches for calculating the roughness of a bedrock-alluvial surface. Johnson [2014] calculated total roughness as an area-weighted mean of the roughness of the alluvial component, determined from grain size, and the bedrock component, estimated as the standard deviation of surface elevations. Inoue et al. [2014] used a similar approach, although they assumed a linear transition between bedrock and alluvial roughness as the sediment cover infills the bed topography. Despite the importance of this issue for predicting sediment cover dynamics, these estimates
have not been robustly tested using topographic and hydraulic data. Such testing again requires a spatially distributed data set of hydraulic properties from a bedrock-alluvial channel with known topography.

2.5. Research Questions

This research begins to address some of the gaps in current knowledge identified above using flow data from a 1:10 scaled model of a bedrock-alluvial reach. The specific questions that the data are used to answer are: (1) How do the spatial patterns of hydraulic properties change with discharge? (2) To what extent does local bed topography affect velocity? (3) How do sediment patches affect local hydraulics?

These experiments are the first example of which we are aware of a Froude-scaled model of a prototype bedrock-alluvial channel. As the prototype site has Fr close to 1 at high flows, these experiments thus provide a data set for addressing competing ideas on the development of reach-scale hydraulics that is complementary to the supercritical Fr numbers of previous flume models [e.g., Chatanantavet and Parker, 2008; Johnson and Whipple, 2010]. The spatially distributed nature of the velocity measurements across a range of discharges begins to overcome the limitations of reach-averaged approaches used previously.

3. Methods

3.1. Field Methods

The prototype is an 18 m long reach of Trout Beck, North Pennines, UK (54°41′35″N 2°23′18″W), which has an average width of 9 m, gradient of 0.02, and 22% sediment cover. The bedrock is Alston Formation Limestone, and the channel bed has a blocky topography with approximately horizontal bedding ~0.5 m thick, preferential erosion along vertical joints, and vertical relief of up to 1 m (Figure 1). Unlike some bedrock channels, there is no inner channel (Figure 1). The sediment $D_{16}, D_{50},$ and $D_{84}$ are 23, 70, and 146 mm, respectively (where $D_s$ is the grain size for which $x\%$ is finer). Although the study reach does not have the extreme topography of some bedrock-alluvial channels, its topography is representative of many other channels (e.g., images in Tinkler and Wohl [1998], Inoue et al. [2014], and Whitbread et al. [2015]).

Flow data were measured at low to moderate flows and extrapolated to discharges equivalent to those used in the flume. Discharge ($Q$) was measured using dilution gauging [Elder et al., 1990] and mean depth ($\bar{h}$) by measuring the water surface level at eight surveyed cross sections within the reach. Reach-averaged mean velocity ($\bar{U}$) was obtained from $\bar{U} = Q/\bar{A}$ and $\bar{A} = \bar{h} w$, where $A$ is wetted cross-section area and $w$ is flow width. Depth and velocity at higher discharges were estimated in the same way but using water levels determined from stage-discharge rating curves at two pressure transducers, one 58 m upstream of the reach and one at the downstream end of the reach.

The bed topography of Trout Beck was surveyed using TLS under very low flow conditions. Scan data were collected from four different positions at a point spacing of down to 5 mm at the center of the channel. The combined TLS data were trimmed to the area of interest, and obviously erroneous points were removed manually. The resulting TLS data had an average density of 33,000 points m$^{-2}$. Differential GPS (dGPS) was used to survey the 29% of the bed that was underwater and therefore not represented in the TLS data, with an average point density of 43 points m$^{-2}$. Existing sediment cover was left within the reach during the survey. TLS and dGPS data were processed to produce 3-D tiles suitable for printing. See Text S1 for further details of the methods. The banks of Trout Beck are close to vertical; the banks in the flume were vertical glass walls.

3.2. Flume Methods

Experiments were conducted in the 0.9 m wide flume at the University of Glasgow, UK. This has a working length of 8 m and maximum discharge of 75 L s$^{-1}$. In order to replicate field processes in the flume, the experiments were Froude scaled with a length scale of 1:10. Following Froude scaling convention, the flume slope is the same as the field (0.02); the length scale $\lambda_x$ applies to width, depth, and sediment size; velocity scales as $\lambda_x^{0.5}$; and discharge scales as $\lambda_x^{2.5}$ [Young and Warburton, 1996; Thompson and Wohl, 1998].

Tiles were fixed to the bed of the flume 3.5 m from the upstream end. The root-mean-square (RMS) of the differences between measured and expected elevation at 30 locations across the tiles was 3.6 mm, with a range of 10.8 to 0 mm, indicating limited tile warping during printing and installation. At the upstream edge of the tiles, the space between their irregular surface and the flume bed was filled with a vertical acrylic sheet.
cut to shape, to prevent flow from getting under the tiles and generating lift. Coarse uniform sediment ($D_{50} \sim 16$ mm) was used to fill the rest of the flume to a level equal to the top of the tiles to ensure development of a turbulent flow profile before flow reached the tiles and to inhibit scour downstream of the tiles. There was little movement of this sediment during the experiments. This sediment size is comparable to the standard deviation of elevations of the modeled section (12 mm), and so on entering the tiles the flow is already adjusted to a surface of a comparable roughness, albeit with less large-scale structure.

Flow was smoothed by a baffle plate in the header area, and depth was controlled by a tailgate set to avoid backwater development at low flow. Flow depth profiles measured along the side of the flume indicated that flow became uniform at short distance ($<2$ m) downstream of the entrance and was maintained until the top of the tiles, at which point it became strongly nonuniform. As our field conditions had $Fr$ close to one, we avoided many of the problems associated with strongly subcritical or supercritical flow. Backwater effects from the flume tailgate did not propagate as far upstream as the tiles.

Two main sets of experiments were undertaken: the first used clear water conditions to measure the variable impact of the topography on the flow; in the second, different volumes of sediment were supplied to measure the impact of the topography on sediment patch dynamics and any consequent impacts on the flow. The second set is primarily reported in the companion paper [Hodge and Hoey, 2016]. In the first set,
discharge was set to one of a series of constant values between 20 and 60 L s$^{-1}$. 20 L s$^{-1}$ is equivalent to just below bankfull in the field setting. For each run, flow depths were measured along the smooth glass side of the flume. Width-to-depth ratios are greater than 12, indicating that wall induced circulation will be minimized [Colombini, 1993]; these low friction walls are expected to increase velocities close to the channel margins compared to the field situation. A Sontek 10 MHz micro-Acoustic Doppler Velocimeter (ADV) was used to record 3-D flow velocities at 25 Hz for 3 min at each of 18 locations across the tiled section. The instrument measurement volume is 4 mm in diameter with a height of 4.5 mm. Local flow depth was measured at each location using a point gauge. Flow velocities were measured at a constant height to record near bed flow conditions, which are important for sediment dynamics as discussed in the companion paper. To ensure that the ADV did not come into contact with the bed at any of the measurement locations, this height was 15 mm above the bed. At two locations downstream bed topography prevented the ADV from being placed so close to the bed, so flow here was measured at heights of 19 and 23 mm (second from right in top transect and third from right on middle transect, respectively).

In the second set of experiments (described in detail in Hodge and Hoey [2016]), fixed masses of sediment were introduced into the flume under constant flow conditions, including a control run with zero sediment input. After 5 min during which sediment formed stable configurations on the bed, the discharge was gradually increased at 0.7 L min$^{-1}$ up to a maximum value of ~70 L s$^{-1}$ to determine erosion thresholds for sediment in different locations. ADV data were collected at 25 Hz for the duration of the experiment at a fixed location (Figure 1). These time series were split into 3 min intervals for analysis. Vertical photographs centered on the midpoint of the tiles, from which sediment cover was quantified, were taken every 5 s throughout the experiment. The extent of sediment cover around the ADV measurement volume was calculated for each run, where the analyzed area extends 20 mm either side of the center of the ADV and 50 mm upstream. The lateral distance is $\sim 1.4 \, D_{90}$ and the upstream distance is $\sim 3.5 \, D_{90}$; for comparison, research on the influence of pebble clusters on flow suggests little lateral influence beyond the extent of the grain but a downstream influence of up to 3.5 times obstacle height [Brayshaw et al., 1983; Lawless and Robert, 2001; Lacey and Roy, 2008]. Sediment cover developed in the analyzed area of the bed in 7 out of the 13 experiments with sediment.

### 3.3. Velocity Data

The shallow, turbulent flows meant that standard filtering thresholds for processing ADV data [Lane et al., 1998] were not applicable because the data displayed relatively low correlation values [Strom and Papanicolaou, 2007]. In turbulent flows, Wahl [2000] suggests that points with a correlation of $<0.7$ can still provide good data if the signal-to-noise ratio (SNR) is high. The ADV data were initially filtered using a correlation threshold of 0.4 [Martin et al., 2002; Strom and Papanicolaou, 2007], a signal-to-noise (SNR) ratio of 10 [Wahl, 2000; Strom and Papanicolaou, 2007], and the expected measurement range. Further removal of spikes caused by aliasing was achieved by removing all velocity measurements that fell outside 3 standard deviations of the mean and then recalculating and repeating this step once [Buffin-Bélanger et al., 2006; Doroudian et al., 2010].

All data were initially inspected by plotting the time series and by plotting the different velocity components against each other. Of the 90 time series from the first set of experiments (5 discharges by 18 positions), 13 were rejected on the basis of the proportion of points that were removed and/or the presence of aliasing or spikes in the filtered data. For the second set of experiments, one of the 14 runs was removed after processing because aliasing still appeared to be present in the data. The retained time series were used to calculate the mean velocity and RMS of velocity fluctuations, Reynolds stress, and turbulent kinetic energy per unit mass (TKE). We use the labeling convention $U$ (downstream), $V$ (vertical), and $W$ (cross stream). To normalize the velocity data, we use the shear velocity, $U^* = (gS) \frac{1}{2}$, where $g$ is gravitational acceleration, $S$ is flume slope (0.02), and $\overline{H}$ is the average flow depth at the 18 locations [Babaeyan-Kooopaei et al., 2002; Legleiter et al., 2007].

For the first set of experiments, the 13 rejected time series had poor quality vertical velocity data. However, mean velocities were calculated using the downstream and cross-stream components of these data series. Analysis of the downstream and cross-stream components for these 13 series used the same filtering process as outlined above, but only removed identified points from one, rather than all three, directions. Comparison
of mean velocities from data filtered using the two different approaches had a RMS error of 0.015 and 0.006 m s\(^{-1}\) in the downstream and cross-stream directions, respectively.

4. Results

We start by demonstrating that the flume is a scaled representation of the field conditions. We then present the hydraulics of the flume at the 18 measurement locations and consider how they vary with discharge. The spatial distribution of hydraulic properties is then presented, followed by an analysis of the relationships between different topographic indices and local flow conditions. We end by assessing the impact that sediment patches have on local hydraulics.

4.1. Model Froude Scaling

Reach-averaged field data are used for direct comparison of hydraulic variables from the field and the flume, as no point measurements are available from the field site. Hydraulic scaling relationships are used to test the consistency of reach-averaged Froude number, water depth, velocity, and flow resistance (Darcy-Weisbach friction factor, \(f\)) between the model and field across the range of modeled discharges. Figure 2 demonstrates that the field and flume data fall along power law regressions to the flume and TB field data. All regression \(R^2\) values are > 0.99, and 95% confidence intervals on all coefficients and exponents show that they are significantly different to zero. Inset in Figure 2d shows just the relationship for flume data using the original flume dimensions.

Figure 2. Comparison of calculated reach-averaged (a) depth (\(h\)), (b) velocity (\(U\)), (c) Froude number (\(Fr\)), and (d) Darcy-Weisbach friction factor (\(f\)) from the field site Trout Beck and from these flume experiments. Flume data are scaled to field dimensions. Two sets of field data are presented. TB field are data collected during low flow conditions using salt dilution gauging. Field data from higher discharges are unavailable due to the difficulty of measuring in high flow. TB extrapolated are values extrapolated from the low flow conditions to higher discharges. Flume data are from the range of discharges used in this study; data from lower discharges are unavailable due to the difficulty of measuring very shallow flows. Flume flow depths are the average from the 18 positions where ADV data were collected. Average velocity is calculated from the bulk discharge and this average flow depth. Dashed lines show power law regressions to the flume and TB field data. All regression \(R^2\) values are > 0.99, and 95% confidence intervals on all coefficients and exponents show that they are significantly different to zero. Inset in Figure 2d shows just the relationship for flume data using the original flume dimensions.
extrapolated from the field measurements to high discharges show good agreement with the scaled flume data, particularly for velocity and flow resistance. The small offset for depth is consistent with the effect of the flume having a fixed width, whereas the prototype width changes by approximately 10% with discharge. Reynolds numbers averaged across the flume and at each of the 18 measurement locations are all $\gg 2000$, indicating fully turbulent flow. Particle Reynolds numbers ($Re^* = U^* D_x / \nu$ where $D_x$ is a length scale based on the $x$th percentile of the grain size distribution and $\nu$ is the kinematic viscosity of water at the laboratory temperature) for $D_{50}$ are $> 70$ at all discharges. Using $D_{16}$ as a much more conservative estimate of roughness, $Re^*$ is also $> 70$ at all discharges. Furthermore, with much finer sediment, a lower threshold $Re^*$ of 15

**Figure 3.** Increase in (a) flow depth, (b) downstream velocity, (c) point Froude number, and (d) point Reynolds stress with increasing discharge in clear water runs. In Figure 3a black points are the mean flow depth. Measurement errors are ± 2 mm. In Figure 3b velocity is measured at an elevation of 15 mm for most locations. Black points are the mean downstream velocity. Error bars are 1 standard deviation of the ADV measured velocities; error bars of 1 standard error of the mean plot within the circular markers. In Figure 3c black dots are average Froude numbers. Error bars are calculated using ± 1 standard deviation of the velocity measurements. In Figure 3d black dots are average Reynolds stresses. Error bars are 1 standard error of the mean. (e) The proportion of turbulent flow events in quadrants 2 and 4 (ejections and inrush events). Point colors indicate mean downstream velocity. In all plots apart from Figure 3e, points are jittered about the x-axis value for clarity.
has been proposed [e.g., Peakall et al., 1996]. Consequently, nearly all grains are experiencing rough turbulent flow, and sediment transport processes can be considered to be dynamically similar to the prototype [Young and Warburton, 1996].

### 4.2. Changes in Hydraulics as a Function of Discharge

As discharge rises from 20 to 60 L s\(^{-1}\) water depth increases linearly (Figure 3a), whereas mean downstream velocity increases more rapidly at lower discharges than at higher discharges (Figure 3b). There is considerable spatial variation in depth and velocity across the channel bed. The range of depths is approximately constant at all discharges (43 mm at 20 L s\(^{-1}\) to 49 mm at 60 L s\(^{-1}\)), whereas the range of downstream velocity increases with increasing discharge (range of 0.53 m s\(^{-1}\) at 20 L s\(^{-1}\) to 0.77 m s\(^{-1}\) at 60 L s\(^{-1}\)). Data from individual locations can vary from the overall trend, with up to 28% of the locations showing decreases in depth or velocity as discharge increases. Decreases are slightly more likely for velocity rather than depth. Flow resistance (Darcy-Weisbach friction factor) decreases with increasing discharge up to \(Q=40\) L s\(^{-1}\) and then remains fairly constant up to \(Q=60\) L s\(^{-1}\) (Figure 2d, inset).

At all discharges, there are some locations with supercritical flow (Figure 3c), the proportion of which increases from 8 to 12 (of 18 locations) as discharge increases from 20 to 60 L s\(^{-1}\). The mean value of \(Fr\) increases from 0.88 ± 0.07 (1 standard error) at 20 L s\(^{-1}\) to 1.05 ± 0.08 at 30 L s\(^{-1}\) before stabilizing at 1.09 ± 0.08 or 1.10 ± 0.08 at 40 to 60 L s\(^{-1}\). As with depth and velocity, \(Fr\) number at a location can decrease, as well as increase, with increasing discharge.

Reynolds stress (Figure 3d) shows a similar pattern to the other properties, increasing from a mean of 1.0 to 3.1 N m\(^{-2}\). There is less variation in TKE, the average of which increases by about 30% from 16.0 J kg\(^{-1}\) at 20 L s\(^{-1}\) to 21.4 J kg\(^{-1}\) at 60 L s\(^{-1}\). In contrast, quadrant analysis of the velocity data indicates some change in the flow structures with changing discharge. The mean proportion of the time that the ADV data are in quadrants 2 and 4 (ejections and inrush events) is fairly constant (52% at \(Q=20\) L s\(^{-1}\) to 55% at...
but the range increases with increasing $Q$ (Figure 3e), indicating that the flow appears to be becoming more spatially variable. As with previous flow properties, at each location the proportion of $Q_2$ and $Q_4$ events can increase or decrease at a higher discharge.

To aid comparison between the different discharges, mean flow velocities and RMS values were normalized by $U^*$ at each discharge (Figure 4). For most components of the velocity the normalized data from different discharges collapse onto the same trend, showing that there is a consistent structure to the flow across the discharges. The main exceptions to this pattern are for $U/U^*$ and $\text{RMS}_V/U^*$. At 20 L s$^{-1}$, the values of $U/U^*$ are significantly lower than at the other four discharges (Kruskal-Wallis test, $p = 0.063$). For $\text{RMS}_V/U^*$ there is a systematic decrease in range and values as discharge increases (Kruskal-Wallis test, $p < 0.001$). In summary, downstream velocities are lower than expected at 20 L s$^{-1}$, and the vertical mixing in the flow decreases with increasing discharge. Legleiter et al. (2007) report similar data from an alluvial channel ($D_{50} = 124$ mm) under low flow conditions. Comparing the range of their results to those in Figure 4, we find that our results typically have a larger range for all components, with the exception of $W/U^*$.

### 4.3. Spatial Patterns of Hydraulics

Vectors of planform velocity (Figure 5) are predominantly downstream at all discharges, with small cross-stream components suggesting limited transverse topographic steering. The range of velocities is always greatest in the upstream transect, which has the most topographic variation (Figure 1e). At $Q=20$ L s$^{-1}$, higher flow velocities occur in the center of the upstream and downstream transects, with lower than average velocities across the middle transect. As discharge increase, velocities increase fastest in the middle transect, linking together high-velocity areas in the upstream and downstream transects and creating a high-
velocity pathway through the model reach. Consequent on the velocity changes, areas of supercritical flow become connected as discharge increases.

Reynolds stress is more varied than velocity across the model (Figure 6) and shows a similar spatial pattern at all discharges, although the range of values increases with discharge. Consequently, areas of high Reynolds stress do not become connected. As with velocity, Reynolds stress is more variable in the upstream transect with the greatest relief. Higher values of Reynolds stress are typically, but not always, associated with higher values of $\text{RMS}_U$.

4.4. Relationships Between Bed Topography and Local Hydraulics

Figure 7 shows the extent to which the local bed elevation accounts for the variation in flow depth and velocity. Unsurprisingly, flow depth shows an inverse relationship with bed elevation; this relationship is fairly consistent across all discharges suggesting that there are not large changes in the water surface slope over the range of imposed discharges (Figure 7a). Because of the momentum of the flow, velocity is not expected to show a strong correlation with either local elevation or flow depth, as seen in Figures 7b and 7c.

To determine the length scales over which bed topography does affect the flow velocity, we regress measures of the bed topography against velocity and Reynolds stress from the 18 measurement locations. We use two different indexes of bed topography: first, the maximum difference in elevation between the measurement point and the upstream bed over a given distance ($\Delta z$). For this calculation we consider the bed elevations over a lateral width of ± 30 mm to account for possible lateral deflection of the flow. This lateral width value produced relationships with the highest $R^2$, but its exact value does not make a significant difference to the overall findings. Second, we calculate the standard deviation of elevations of the local bed topography ($\sigma_z$) [Inoue et al., 2014; Johnson, 2014], calculated over a square area centered on the
measurement location. Both $\Delta_z$ and $\sigma_z$ require a length scale over which the index is calculated. One approach would be to identify the smallest scale at which these indexes reach a constant value. However, because of the irregular bed topography, the value of $\sigma_z$ depends on the size of the area of bed elevations. Figure 8 shows that the distribution of $\sigma_z$ does not stabilize as the window size increases up to the width of the flume, suggesting that there is not a geometrically optimum window size to apply. Consequently, we use a range of sizes.

For each discharge, linear regression was used to analyze the relationship between (1) $U$ and $\Delta_z$; (2) Reynolds stress and $\Delta_z$, with $\Delta_z$ calculated over a range of upstream distances in both cases; and (3) $U$ and $\sigma_z$ calculated using a range of window sizes. For each of these combinations multiple regression was also conducted, including the measurement point elevation ($z$) in addition to the topographic index ($\Delta_z$ or $\sigma_z$). Linear regressions between the hydraulic parameters and the measurement point elevation ($z$) were also undertaken.

Regressing velocity against these topographic indices is supported through analysis of flow resistance equations. A linear relationship between $\sigma_z$ and velocity would result from Manning’s $n$ being proportional to topographic roughness. In the case of the Darcy-Weisbach equation, standard hydraulic relationships are

$$\tau = \rho ghS$$  \hspace{1cm} (1)

$$U^2 = 8ghS/f$$  \hspace{1cm} (2)

$$f = \frac{8}{a_0^2 \left( \frac{h}{k} \right)^{1/3}}$$  \hspace{1cm} (3)

where $a_0^2$ is a coefficient with a value of 8 [Ferguson, 2012], $k$ is a representative roughness length, and $\rho$ is the density of water. Rearranging equations 1–3 gives $U \propto k^{-1/6}$. We therefore show both linear and power law fits to the strongest relationship between the hydraulic and topographic parameters in Figure 9.

**Figure 7.** Relationships between downstream velocity, bed elevation, and water depth across all five discharges at each of the 18 measurement locations.
4.5. Impact of Sediment on Flow Velocities

Flume runs where sediment was introduced and the ADV was in a single location (Figure 1d) illustrate the impact of sediment cover on downstream and vertical velocities (Figure 10). High sediment cover in the area upstream of the ADV (areal coverage proportion > 0.4) leads to a significant reduction in the mean downstream velocity (Figure 10a) and a less pronounced trend of reduction in vertical velocities (Figure 10b) and cross-stream velocities. With smaller amounts of sediment cover, velocities tend to plot below the trend of data with no sediment cover (control run). In the absence of sediment some variation in the proportion of quadrant 2 and quadrant 4 events with changing discharge was reported above, but the amount of sediment cover seems to have little impact on this aspect of flow structure (Figure 10c).

The impact of sediment cover was evaluated using the difference between the velocity in each run with sediment cover and the control run with no sediment input. This difference was calculated for each of the points in Figure 10a, with velocities from the control series being interpolated at the appropriate discharge. Stepwise regression of this difference in velocity against discharge and proportion of sediment cover was performed for all three flow velocity components. In all three cases sediment cover contributed significantly
Figure 9. (a) $R^2$ values for relationships between the upstream difference in surface elevations ($\Delta z$) and mean downstream velocity ($U$), using $\Delta z$ calculated over a range of upstream distances. (c) The same analysis but for Reynolds stress (RS) instead of $U$. (e) The same analysis as Figure 9a but characterizing topography using the standard deviation of elevations ($\sigma_z$) within a square window centered on the velocity measurement location. In all of Figures 9a, 9c, and 9e, thin lines are $R^2$ for the regression between the topographic index and the hydraulic data for each discharge; thick lines are $R^2$ for a regression that also incorporates the elevation of the measurement location (using the same color scheme for $Q$), and dashed lines are for the regression between the point elevation and the hydraulic data. Circles indicate statistically significant relationships ($p < 0.05$). (b, d, and f) The relationships between the topographic index and the hydraulic data for the highest $R^2$ in the previous panel. Dashed lines are power functions (top equation shown on each panel), and solid lines are linear relationships (bottom equation on each panel). In Figures 9b and 9f, $Q = 20\text{ L s}^{-1}$, and in Figures 9d $Q = 30\text{ L s}^{-1}$. 

$U = 0.95\Delta z^{-0.27}$

$U = 0.68 - 0.012\Delta z$

$RS = 0.27\Delta z^{0.76}$

$RS = 0.46 + 0.13\Delta z$

$U = 1.03\sigma_z^{-0.36}$

$U = 0.71 - 0.025\sigma_z$
to explaining the velocity difference ($p < 0.001$). Discharge was not a significant component ($p > 0.30$), which is not surprising as the changes in velocity with discharge measured in the control run have been removed from these data.

The formation of sediment cover changes the roughness of the upstream bed surrounding the ADV. The impact of this change was estimated by calculating a roughness length for this area of the bed (i.e., the area that sediment cover was calculated for) using the relationship

$$k_{\text{tot}} = k_{B} F_{e} + k_{A} (1 - F_{e})$$

(4)

where $k_{\text{tot}}$ is the total roughness length, $k_{A}$ and $k_{B}$ are the alluvial and bedrock roughness lengths, respectively, and $F_{e}$ is the fractional exposure of the channel bed [Johnson, 2014]. $k_{A}$ is estimated as the standard deviation of surface elevations within this small area, which is 3.4 mm (compared to a channel-wide value of 12 mm). Although earlier analysis showed that $\Delta z$ had a stronger correlation with velocity than $\sigma_{z}$, $\sigma_{z}$ is used here because it is unclear what a comparable value of $\Delta z$ for sediment cover would be, and for consistency with Johnson [2014]. $k_{B}$ is estimated as $2D_{50}$ [Johnson, 2014], which is 14.6 mm. $k_{\text{tot}}$ is plotted against velocity in Figure 10d. In keeping with Figure 9f and previous hydraulic relationships, a power law was fitted. The exponent and coefficient are significantly different to zero ($p = 0.05$).
5. Discussion

In the discussion we address each of our research questions (section 2.5), before considering the broader implications of our findings for bedrock-alluvial channels.

5.1. How Do the Spatial Patterns of Hydraulic Properties Change With Discharge?

The channel topography induces considerable spatial variation in flow depth, velocity, Froude number, and Reynolds stress (Figures 3, 5, and 6). As discharge increases, the range (and thus spatial variation) of flow depths remains approximately constant, whereas the range of velocities increases. At a single point, hydraulic properties can both increase and decrease as discharge increases. The scaled variability in velocities (Figure 4) remains largely unchanged throughout, although at the lowest discharge (20 L s⁻¹) the downstream velocities are significantly lower than at all other discharges. The vertical velocity component (Figure 4) shows a systematic trend of becoming less variable as discharge rises, whereas variability in the other components remains unchanged. When the spatial patterns of these changes are considered, a key result is the development of a core of high-velocity and supercritical flow that links up all three measurement transects.

The development of a high-velocity core is comparable to the hydraulic changes identified by Richardson and Carling [2006] in Birk Beck. They hypothesized that the channel switched from a macroturbulent mixing state (MMS) with complete mixing across the entire channel cross section to a decoupled dead zone state (DDZS), with a decoupled core of faster flow. Aspects of the results presented here suggest that Trout Beck may behave in a similar manner. Between discharges of 20 and 40 L s⁻¹, the channel appears to be in an MMS. This is supported by the smaller variation in flow velocities at these discharges and flow resistance (Darcy-Weisbach f) becoming independent of discharge at Q = 40 L s⁻¹ (Figure 2d, inset). Froude number also stabilizes at just above unity at this discharge (Figure 3c). Between discharges of 40 and 50 L s⁻¹, the channel seems to transition into the DDZS, with the development of a core of supercritical flow and greater variation in velocity (Figure 5). However, even at the highest discharge there is still more lateral and downstream variation in Fr than was observed by Tinkler [1997], indicating that the bed topography is still influencing the flow.

The reason for this transition in our experiments seems to be a function of the differing response of the 3-D flow field to the bed topography and the changing scales of influence of the channel topography (discussed below). As the flume has smooth walls these changes do not result from the flow accessing additional roughness sources as has been postulated in the field [Richardson and Carling, 2006]. Richardson and Carling [2006] also identified two distinct thresholds, with the MMS developing above Q₁ when flow resistance decouples from discharge and the DDZS occurring at the higher Q₂. In our experiments the decoupling of flow resistance occurred at around the same discharge as the development of the high-velocity core, suggesting only a single threshold. However, the use of only five different discharges makes the identification of specific threshold difficult.

5.2. To What Extent Does Local Bed Topography Affect Velocity?

The relatively poor correlation between bed elevation and downstream velocity (Figure 7b) is not surprising. However, analysis of the correlations between downstream velocity (U) and Reynolds stress and indices of local bed topography (Δz and σz) shows that at some discharges upstream bed elevations do affect downstream velocity. At the lowest discharge, Q = 20 L s⁻¹, there is a significant relationship between both Δz and σz and U, with the strongest relationship when Δz and σz are calculated over a distance of about 300 mm. At other discharges the relationship between Δz or σz and U is at best similar to the weak relationship between the local bed elevation (z) and U, with relationships calculated using σz being worse.

The velocity therefore seems to be conditioned by the upstream bed topography at low discharges, but not at larger discharges. This is consistent with the normalized flow data (Figure 4a), in which values of U/U* are significantly lower at 20 L s⁻¹ than at higher discharges, suggesting an increased flow resistance at the lower discharge. Values of RMS/U* show that there is also more vertical turbulence in the flow at the lowest discharge, suggesting that the higher flow resistance is caused by the development of larger coherent flow structures downstream of topographic steps that increase vertical flow and reduce downstream velocities. Consistent with these data, Hardy et al. [2010] found, over an alluvial bed, that at lower relative roughness (i.e., increased flow depth for a fixed bed topography) flow structures became less defined throughout the
flow depth, and the reduction in downstream velocity was less pronounced. This hydraulic state is also consistent with the MMS of Richardson and Carling [2006].

The identified length scale of 300 mm (3 m in the field) is likely to reflect the length of this detachment zone behind the dominant steps in the bed. Observations suggest that pebble clusters can influence the flow over a downstream distance equivalent to 3.5 times the obstacle height [Brayshaw et al., 1983; Lawless and Robert, 2001; Lacey and Roy, 2008]. Applying the 3.5 scaling factor to our site suggests that a length scale of 300 mm corresponds with an obstacle height of 86 mm (860 mm field), which is comparable to some of the larger steps in the bed topography. The relationship between Reynolds stress and the topographic indices is harder to explain, with significant correlations only at 30 and 60 L s\(^{-1}\). This therefore demonstrates that the different components of velocity do not appear to respond in the same way to the identified topographic indices.

5.3. How Do Sediment Patches Affect Local Hydraulics?

Experiments with sediment demonstrated that sediment cover alters the local hydraulics, decreasing downstream flow velocities. The relationship proposed by Johnson [2014] for estimating the topographic roughness of mixed bedrock-alluvial surfaces was used to predict how roughness in the region affecting the velocity recorded by the ADV changed as sediment cover developed. The resulting relationship between downstream velocity and topographic roughness (Figure 10d) has a very similar form to the relationship derived from clear water flows (Figure 9f), with both power law exponents being about \(-0.35\). This provides support for the relationship proposed by Johnson [2014], albeit maybe as a power function. Both relationships are different to either the linear or \(-1/6\) power suggested by the Manning’s and Darcy-Weisbach relationships; however, concurrent variations in local energy slope and depth were not accounted for. Further analysis of the runs with sediment cover, such as the calculation of flow resistance parameters from the flow data, was not possible because local water depths were not recorded.

The above analysis was limited to a single ADV location and results may vary spatially. The \(\sigma_z\) in the ADV measurement location was 3.4 mm, which is comparatively smooth compared to sediment \(D_{50}\) of 7.3 mm. Mean values of \(\sigma_z\) across the entire channel range from 5 to 6 mm over window sizes of 150 to 300 mm (Figure 8). Thus, there is a significant proportion of the channel where adding sediment could decrease topographic roughness by infilling bedrock depressions, so potentially increasing local flow velocities.

5.4. Implications for Bedrock-Alluvial Channels

These experiments have demonstrated relationships between spatial patterns of flow (velocity, Froude number, and Reynolds stress), bed topography (including the impact of sediment cover), and discharge. However, these experimental results are for one 18 m long section of a particular bedrock-alluvial channel, and so it is necessary to consider possible implications for bedrock-alluvial rivers in general. The topography of this reach of Trout Beck is relatively low relief, with an elevation range of just over 1 m (excluding the net downstream slope), and a blocky topography which becomes less rough toward the downstream end of the reach. Although such topography is not unusual in bedrock-alluvial channels, the value of our results also lies in the validation of concepts that either have only been observed at a single site or have not previously been tested. In particular, we have demonstrated (1) increased spatial variation in flow characteristics with discharge, which is not driven by channel bank roughness, and (2) that at the lowest discharge, velocity is correlated with upstream bed topography.

The changes in spatial flow conditions and relatively poor relationships between topographic roughness and hydraulics at most discharges have implications for predicting hydraulics in bedrock-alluvial rivers. The increased variation and development of a high-velocity core mean that the distribution of shear stress over the bed will be highly spatially variable. Furthermore, Reynolds stress shows different spatial variation to other hydraulic parameters. The location of the high-velocity core will have implications for the pathways that bedload will be transported along, the areas of the bed that will be most subject to erosional processes, and the deposition and erosion of sediment patches (see companion paper [Hodge and Hoey, 2016]).

The analysis comparing topographic indices and velocity suggests that \(\Delta z\) and \(\sigma_z\) can be used to quantify the impact of the topography on the flow at some, but not all, discharges. The analysis supports the use of a mixing model approach for combining sediment and bedrock roughness. There is also the question of the most appropriate window size for calculating \(\Delta z\) and \(\sigma_z\). For any given river, this length scale is likely to be a...
function of the bed topography and may change as a function of discharge. One possible approach is to use a length scale that is a function of the topographic relief, for example, a length of 3.5 times a representative step height as suggested from our data and the effect of particle clusters on hydraulics. The second approach is to look at the changing distribution of $c_v$ with increasing window size and to identify a minimum window size that is needed to capture the topographic variability.

### 6. Conclusions

A Froude-scaled model of a bedrock-alluvial river reach was used to quantify how flow hydraulics changed across a range of discharges, and how they related to the bed topography. The flume experiments demonstrated that (1) spatial variation in flow velocity, Froude number, and Reynolds stress increases with discharge; (2) flow resistance and Froude number become independent of discharge at higher discharges; (3) local flow velocity and Reynolds stress are correlated with the range of local bed topography at some, but not most, discharges; and (4) sediment cover produces changes in flow velocity that are consistent with predicted changes in surface roughness. Although these data are from a single channel, they have wider implications. In particular, the results indicate that there is no single representative roughness length for a bedrock-alluvial channel, with topographic analysis showing that standard deviation of surface elevations does not converge to a single value over length scales up to the width of the flume (channel width at field scale), and that different hydraulic properties correlate with local topography at only some discharges. The results also indicate that the transition from a macroturbulent mixing state to a decoupled dead zone state, as observed by Richardson and Carling [2006], may be a characteristic behavior of bedrock-alluvial channels, and also that bank roughness is not necessary for this transition to occur.

The hydraulics of bedrock-alluvial channels remain little researched, despite their importance for bedload transport, channel incision, and ultimately landscape evolution. The implications of the role of hydraulics for the development and erosion of sediment cover in this reach are addressed in the companion paper [Hodge and Hoey, 2016]. To extend the findings in this paper further, high-resolution data on spatially distributed hydraulics are required (either from scaled models or the field) from bedrock-alluvial channels with a wide range of channel morphologies and extents of sediment cover. Such data sets would enable more robust relationships between hydraulics and bed topography, and the way in which the relationships change with discharge, to be established.

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