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Earthquake source properties from pseudotachylite

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Abstract

Earthquake-radiated motions contain information that can be interpreted as source displacement and therefore related to stress drop. Except in a few notable cases, these displacements cannot be easily related to the absolute stress level, the fault strength, or attributed to a particular physical mechanism. In contrast paleo-earthquakes recorded by exhumed pseudotachylite have a known dynamic mechanism whose properties constrain the co-seismic fault strength. Pseudotachylite can be used to directly address a discrepancy between seismologically-measured stress drops, which are typically a few MPa, and much larger dynamic stress drops expected from thermal weakening during slip at seismic speeds in crystalline rock [Sibson, 1973; McKenzie and Brune, 1969; Lachenbruch, 1980; Mase and Smith, 1986; Rice, 2006], and as have been observed in laboratory experiments at high slip rates [Di Toro et al., 2006a]. This note places pseudotachylite-derived estimates of fault strength and inferred crustal stress within the context and bounds of naturally observed earthquake source parameters: apparent stress, stress drop, and overshoot, including consideration of fault surface roughness, off-fault damage, fracture energy, and the 'strength excess'. The analysis, which assumes stress drop is related to corner frequency by the Madariaga [1976] source model, is restricted to earthquakes of the Gole Larghe fault zone in the Italian Alps where the dynamic shear strength is well-constrained by field and laboratory measurements. We find that radiated energy is similar to or exceeds the shear-generated heat and that the maximum strength excess is ~16 MPa. These events have inferred earthquake source parameters that are rare, for instance a few percent of the global earthquake population has stress drops as large, unless: fracture energy is routinely greater than in existing models, pseudotachylite is not representative of the shear strength during the earthquake that generated it, or unless the strength excess is larger than we have allowed.
Introduction

Within the earthquake source region a large number of inelastic processes are thought to operate: frictional sliding, rock fracture, dilatancy, melting, devolatilization, thermal expansion of pore fluid, hydrofracture, and creation of new fracture surface energy are among many known and proposed processes [Andrews, 1976; Scholz, 2002; Rice, 2006]. The processes that actually occur depend on mineralogy, ambient temperature and stress conditions, total slip, the degree of shear localization, the amount of shear dilatancy, and fault zone hydraulic properties. Outside the source, the surrounding rock is assumed predominantly elastic and the motions radiated from the source as elastodynamic waves can be related to the spatial time history of displacement within the source. Accounting for attenuation, scattering, and other path effects, information propagating from the source is interpretable at the surface in terms of, for example, source stress drop, moment, radiated energy, and displacement or velocity spectrum, but only on rare occasions to the absolute level of stress [e.g., Spudich, 1992]. For earthquakes that have source mechanisms that are predominately double couple, to date there is little observational or theoretical research that ties surface recorded motions to a particular physical mechanism within the source. So, with the exception of a very few notable claims [e.g., Kanamori et al., 1998], what source processes actually occur for any particular earthquake is anyone’s guess.

Field observations and melt shear strength.

A well-understood exception are the ancient earthquakes recorded in exhumed pseudotachylites [Sibson, 1975]. Pseudotachylite is thought by most to be the definitive record of an earthquake where dynamic strength was controlled by shear melting [Jeffreys, 1942; McKenzie and Brune, 1972; Sibson, 1975], though there are alternative interpretations [e.g., Pec et al., 2012 and references therein]. In the present study we assume that natural pseudotachylites are generated by coseismic shear heating and take advantage of field and laboratory constraints on the co-seismic properties of the shear zone. Melt layers are viscous and therefore have strengths that are quite strongly slip rate- and thickness-dependent. In addition the viscosity can
depend on the characteristics of the flow regime and melt composition [Spray, 1993; Lavallee et al., 2015]. The field measurements avoid these complexities and produce empirical constraints on the dynamic shear strength during the event [Sibson, 1975]. Specifically, field-measured values of the thickness of a pseudotachylite layer, \( w \), are used to estimate the heat necessary to melt a particular volume of rock of a particular composition using the protolith heat capacity.

Sibson assumed all the shear generated heat remains in the slipping zone and causes melting immediately at the melting temperature \( T_m \) of the constituent minerals. Somewhat more recently Wenk et al., [2000] and Di Toro et al. [2005] repeated the same type of analysis while also allowing for some of the shear heat to be absorbed in the slipping zone as latent heat of fusion.

Accordingly the heat necessary to convert a thickness of rock entirely to melt is

\[
Q = A \ w \left[ (T_m - T_0) c_p + H \right],
\]

(1a)

where \( c_p \) is the heat capacity (energy/mass K), \( H \) is the heat of fusion (in energy/mass), \( A \) is fault area, \( \rho \) is density (mass/volume) and \( T_0 \) is the initial slipping zone temperature. The two terms on the righthand side of (1a) are from left to right, the change in thermal energy within the slipping zone and the energy necessary to drive the endothermic melting reaction, the latent heat stored within the melt. This assumes that significant heat does not diffuse away from the fault coseismically, which is reasonable given the low thermal diffusivity of rocks \( (\kappa \approx 10^{-6} \text{ m}^2 \text{s}^{-1}) \) and the few second duration, \( \Delta t \), of earthquake slip [Lachenbruch, 1980], which results in a heat penetration distance, \( z \approx \sqrt{\kappa \Delta t} < 2-3 \text{ mm} \). An additional requirement of (1a) is that the slipping zone temperature does not exceed the melting temperature (no superheating) which is expected if the phase change buffers the temperature increase. The displacement-averaged shear strength is

\[
\hat{t}_m = \frac{Q}{A},
\]

(1b)

where \( \Delta \delta \) is fault slip as measured in the field using offset markers across the fault [Sibson, 1975]. Combining (1a) and (1b) the displacement-averaged shear strength during seismic slip that produces a shear melt is

\[
\hat{t}_m = \frac{w}{(T_m - T_0) c_p + H}.
\]

(1c)
Note that the heat of fusion is on the order of $10^5$ J/kg while the heat capacity is of order $10^3$ J/kgK for granitic compositions. So long as the temperature difference $T_m - T_0$ is 1000 K or more the change in thermal energy greatly exceeds the heat of fusion and dominates the sum (1c). This is the case for both the natural [Di Toro et al., 2005] and laboratory [Di Toro et al., 2006a] settings of tonalitic psuedotachylite generation that we consider in this study.

Thickness displacement ratios, $w/\Delta \delta$ measured by Di Toro et al. [2005; 2006a] for pseudotachylite in tonalite within the Gole Larghe fault zone in the southern European Alps exhumed from hypocentral depths of 9 to 11 km and $T_0$ of 250°C are between 0.01 and 0.004. The associated calculated shear strengths are between 15 and 48 MPa, as depicted in Figure 1. This technique to estimate melt shear strength, equation (1c), was confirmed for normal stresses $> 20$ MPa in experiments simulating coseismic slip on gabbro [Niemeijer et al., 2011]. In the field the approach also requires some independent measure of the ambient temperature prior to the earthquake. Hypocentral temperature ($T_0 \approx 250$ °C) of the Gole Larghe was estimated from deformation microstructures of quartz in cataclasites associated with the pseudotachylites, and by the mineral assemblage of coeval metamorphic alteration by Di Toro and Pennacchioni [2004].

### Lab observations of melt shear strength.

Meanwhile, advances in experimental design and technique [Tsutsumi and Shimamoto, 1997; Hirose and Shimamoto, 2003, 2005] and related theoretical developments [Nielsen et al., 2008, 2010; Di Toro et al., 2006b] allow determination of the shear strength and constitutive response of friction melts of identical composition to the Gole Larghe fault zone field exposures at a few to a few 10’s of MPa normal stress [Di Toro et al., 2006a]. Laboratory shear melting experiments by Di Toro et al. [2006a] were conducted at normal stresses between 5 and 20 MPa at a sliding velocity of 1.3 m/s for 4 to 8 s on the source tonalite collected from the Adamello batholith in the southern Italian Alps from which the natural pseudotachylites were exhumed. In our study the reported steady-state shear strengths from Di Toro et al. [2006a] are assumed to be analogous to their natural equivalents. The melt steady-state shear strength resembles the
unmelted strength of granitic faults [Byerlee, 1978] at the lowest normal stresses (Figure 1) but is considerably weaker at 10 to 20 MPa normal stress, the highest normal stresses tested. For extrapolation to the conditions of the natural pseudotachylites, the ‘pressure dependence’ of fault strength $d\tau/d\sigma_e$ is the necessary metric; for these faults shear strength increases very weakly with normal stress (0.05 MPa per MPa) and using this extrapolation from Di Toro et al. [2006a], the implied natural strength at 9 to 11 km is less than 20 MPa (Figure 1).

In this study we examine the energy budget of earthquakes that generate shear melts of tonalitic composition. Knowing both the shear generated heat from field observations and the shear strength from laboratory measurements puts constraints on energy partitioning that are lacking for all other earthquakes. Our approach is to use the laboratory and field measurements of co-seismic fault strength along with the known static strength of the granitic host rock as the independent variables and determine the possible range of source parameters for the paleo-earthquakes that generated these melts. Throughout the paper we refer to these prehistoric seismic events as earthquakes for simplicity. Particular goals are to establish whether these events could be consistent with typical earthquake source properties and what seismically observed properties may be diagnostic of melting. We find that earthquakes generating these pseudotachylites have atypical source properties that arise from the very high static frictional strength of granitic rock and the very low strength of shear melts. As in this particular example, and likely in other rocks that have high frictional strengths at low sliding speed and for which shear heating produces a weak melt, the result is a large stress drop and relatively high radiated energy.

**Energy during dynamic slip**

Ignoring gravitational and rotational terms, the total energy of an earthquake $E_T$ can be partitioned between heat $Q_{all}$ and radiated energy $E_s$,

$$E_T = Q_{all} + E_s.$$  \hspace{1cm} (2)
Here, as follows from the analysis of Savage and Wood [1971] [e.g., McGarr, 1999; Beeler 2006], we have included in $Q_{all}$ both the shear generated heat that is available to be conducted away from the fault, and also latent heats that are absorbed during shearing: for example the heat of fusion (as in equation (1) [Di Toro et al., 2005]), heat of reaction during other phase changes [e.g., devolitalization Brantut et al., 2011], and the creation of surface energy that results from wear and comminution [Lachenbruch and Sass, 1980]. The average shear stress on the fault is related to the total work $\bar{\tau} = E_T/A\Delta\delta$. Following the definition of heat above, equation (1b), define a shear ‘strength’ $\hat{\tau} = Q_{all}/A$; $\hat{\tau}$ is the stress measure of energy dissipated and stored in the source, spatially- and slip-averaged over the entire source region [McGarr, 1999; Beeler, 2006]. It is a representative sliding strength of the fault, associated with energy distributed within the source, including heat, latent heat associated with chemical reactions and with the creation of surface energy. Using the standard definition of apparent stress as the stress measure of radiated energy $\tau_a = E_s/A\Delta\delta$, the balance (2) can be rewritten in stress units as

$$\bar{\tau} = \hat{\tau} + \tau_a,$$

(Savage and Wood, 1971; McGarr, 1994). The energy budget can be graphically expressed using a stress versus displacement diagram (Figure 2) [McGarr, 1994]. The figure presents the definitions of stress quantities used throughout this paper. In particular the average stress is the difference between the static stress levels before and after the earthquake, $\bar{\tau} = (\tau_0 + \tau_1)/2$, where $\tau_0$ is the initial stress on the fault prior to the earthquake and $\tau_1$ is the stress after seismic slip.

Equating the shear strength that produces melt, equation (1b), to this stress measure of all the energy that is not radiated, $\hat{\tau} = \hat{\tau}_m$, is the first crucial assumption in our analysis. Making this assumption presumes, for example, that any off-fault damage makes a negligible contribution to the energy budget. This is an assumption that is difficult to verify [Pittarello et al., 2008] and not without associated controversy [e.g., Wilson et al., 2005; Chester et al., 2005; Ma et al., 2006]. Some of the limitations and implications if this assumption is relaxed are detailed in the Discussion section below. Recent field studies of pseudotachylite, e.g., Di Toro et al. [2006a],
have equated the fault shear strength $\hat{t}$ inferred from thickness-displacement ratios (1c) (Figure 1) with the average crustal shear stress $\overline{\tau}$. The average shear strength and the static shear stress are approximately equivalent under special circumstances, as noted by McGarr [1994; 1999]. This analysis to recover shear stress has been repeated elsewhere [e.g., Barker, 2005; Ujiie et al., 2007; Andersen et al., 2008; Billi and Di Toro, 2008]. That relationship is valid only if $\hat{t} = \hat{t}_m$, as we have assumed, and if the apparent stress, $\tau_a$, is relatively small. For shear melting there are no published proportions of radiated energy and heat from laboratory measurements. There is also little knowledge of partitioning between heat and radiated energy from seismology or field relations; however combining lab and field studies for granitic rock and considering the source properties of earthquakes observed seismically, the possible range of energy partitioning for shear melted granitic faults can be addressed as we show next.

Earthquakes show a wide range of relationships between shear strength and shear stress during rupture. The difference can be parameterized to some degree by the slip overshoot [Savage and Wood, 1971; McGarr, 1994],

$$\xi = \frac{\hat{t} - \tau_1}{\Delta \tau_s}$$  \hspace{1cm} (4)

where $\Delta \tau_s$ is the static stress drop, the difference between the initial and final stresses (Figure 2). Throughout the following analysis we take the initial stress to be approximately equal to the static fault strength; this is the second crucial assumption. This is controversial, especially for plate boundary-scale faulting [Lapusta and Rice, 2003; Noda et al., 2009]. The assumption also differs from the general example in Figure 2 where the initial stress is lower than the static fault strength (the peak strength $\tau_p$ in Figure 2). Such differences and the implications when this assumption is relaxed are dealt with in the Discussion section below.

The static strength of the andesitic and granitoid rocks of the motivating studies of Sibson [1975] and Di Toro et al. [2005] follow Byerlee’s law approximately [Byerlee, 1978] (Figure 1). To estimate the stresses at depth we use guidance from the field studies of Di Toro and Pennacchioni [2004] and Di Toro et al. [2006] who used Andersonian assumptions for strike-slip...
faulting [Anderson, 1951]. We use the mean depth of 10 km, a lithostatic stress gradient of 26 MPa/km and assume that the intermediate principal stress is equal to the mean stress and then average the results for hydrostatic pore pressure and dry conditions. The details of the estimate are in the Appendix. The effective normal stress is 122 MPa resulting in an initial stress of $\tau_0 = 104$ MPa for a Byerlee friction of 0.85. According to the regression of Di Toro et al. [2006] at 10 km depth the average dynamic strength is $\hat{\tau} = 10.6$ MPa. This coseismic shear strength is lower than the mean value inferred from the field study, $\hat{\tau} = 26.8$ MPa. Here and throughout we report stress estimates to the tenths of MPa. This choice should not be interpreted as the accuracy of the estimate which is unlikely to exceed a few MPa. However, we are interested in seismologic stress measurements, particularly stress drop, that can often be two to three orders of magnitude smaller than the above quoted initial stress (see the subsequent Figure 3). As a consequence the apparent accuracy of stresses in this report is required to estimate stress drop in our analyses. Typical stress drops are a few MPa and our reported stresses are to the order of 10% of that.

In the following we consider four possible scenario earthquake source parameters for shear melting at this depth. The scenarios are intended to span the range of plausible seismically observed source properties. For all four scenarios we calculate source parameters using the average field measured shear strength of 26.8 MPa. These results are described in the immediately following text and listed in Table 1.

**Scenario 1** is the Orowan condition where the stress drops exactly to the dynamic fault strength $\hat{\tau} = 1$ [Orowan, 1960; Kanamori and Heaton, 2000], then $\Delta \tau_s = 77.2$ MPa, the overshoot (4) is zero, $\tau_a = 65.4$ MPa and $\tau_a = 38.6$ MPa. This would be a case of high seismic efficiency relative to that which has been assumed for pseudotachylyte [Di Toro et al., 2006a], $a/\tau = 0.59$; 59% of the total energy would be radiated. Because the Orowan condition is the most often used assumption in studies of the earthquake energy budget, such as in a number of seminal contributions, compilations and reviews [e.g., Kanamori and Heaton, 2000,
Venkataraman and Kanamori, 2004; Kanamori and Brodsky, 2004; Abercrombie and Rice, 2005; Viesca and Garagash, 2015], it is useful for placing estimated source parameters and their uncertainty in context. For example, had we used the upper limit of the field estimated fault strength (48 MPa) rather than the average, the resulting seismic efficiency of 37% would still be much higher than typical seismological estimates [e.g., Wyss, 1970; McGarr, 1999].

Scenario 2 is complete stress drop, then, $\tau = 52$ MPa, $\xi = 0.26$, and $\tau_a = 25$ MPa, again, a case of high seismic efficiency $\eta = \frac{\tau}{\tau} = 0.48$.

Both of these scenarios 1 and 2 would be out of the range of typical earthquake source properties, as follows.

In the following analysis we use the stress drops of a recent global compilation [Allman and Shearer, 2008] for reference. These are determined from seismically inferred corner frequencies ($f_c$) using the Madariaga source model [Madariaga, 1976]. Because stress drops depend on $(f_c/C)^3$ where $C$ is a model-dependent scalar, small differences in the scalar (model) produce much large differences in stress drop, up to a factor of 5.5 [e.g., Kaneko and Shearer, 2014]. Thus constraints on source properties from stress drop are weak. Specific differences between models and the difficulties that arise in using stress drop in studies of source physics are discussed in section 3.2 below. Typical values of stress drop are a few MPa albeit with significant logarithmic variability (Figure 3, after Allman and Shearer [2009]). The dashed lines that are superimposed mark 99, 95, and 90% of the stress drops in the Allman and Shearer dataset. For instance, 1% of the earthquakes have stress drops larger than the 99% line, and so on. The 99, 95 and 90% lines are associated with stress drops of 110 MPa, 40 MPa and 23 MPa, respectively. Stress drops as large as those in scenarios 1 and 2 are found only in a few percent or less of natural earthquakes. This apparent inconsistency between seismologically inferred values of MPa static stress drop and the $\sim 77$ MPa dynamic stress drop from the field and extrapolated
from laboratory observations of melting (Figure 1) is a paradox long expected from theoretical considerations of shear heating [Sibson, 1975; Lachenbruch, 1980; Rice, 2006; Noda et al., 2009]. Similar, but potentially stronger constraints on source properties come from apparent stress because it is not model dependent. For comparison with the scenario estimates of apparent stress, Figure 4 shows apparent stresses compiled by Baltay et al. [2010]. The estimated apparent stresses using Orowan’s (Scenario 1) and the complete stress drop (Scenario 2) assumptions are outside the range of these seismic observations that lie between 0.1 and 10 MPa (Figure 4).

We also consider the implied overshoot of these scenarios (Table 1). The energy balance with stress as the dependent variable (3) can be rewritten in terms of stress drop, overshoot and apparent stress as

\[
\frac{\tau_a}{\Delta \tau_s} = 0.5 - \xi
\]

[Savage and Wood, 1971; McGarr, 1994; 1999]. Keep in mind that the model dependence of stress drop means that bounds on overshoot are dependent on the choice of source model; for all the standard source models stress drop tends to be a fixed factor of apparent stress [e.g., Singh and Ordaz, 1994; Kaneko and Shearer, 2014]. Since both stress drop [Hanks, 1977] and apparent stress [Ike and Beroza, 2001] are arguably magnitude independent, earthquake overshoot is also magnitude independent according to (5). For the Madariaga model at 0.9β, slip overshoots the static value by 20% [Madariaga, 1976], which corresponds to a stress measure of overshoot (4) of 0.17 which is not so different from scenario 2. Because they involve restrictions on stress drop, with the exception of overshoot, the source parameters from scenarios 1 and 2 are independent of the choice of source model; this is not the case for scenarios 3 and 4 that follow.

Scenario 3 is typical stress drop. Instead of complete stress drop or Orowan's assumption, take the stress drop to be Δτ_s = 3.8 MPa, then, \( \bar{\tau} = 102 \) MPa, \( \bar{\xi} = -19.3 \), and \( \bar{\tau}_a = 75 \) MPa. This would be a case of extreme undershoot; undershoot larger than can be inferred from seismic observations.
(see analysis of data of Venkataraman, and Kanamori, [2004], in Beeler, 2006), and again, high seismic efficiency \( h = \frac{a}{\tau_s} = 0.73 \).

**Scenario 4** is typical overshoot, \( \xi = 0.17 \), leading to \( \Delta \tau_s = 93 \text{ MPa} \), \( \bar{\tau}_s = 57.5 \text{ MPa} \) and \( \tau_a = 30.7 \text{ MPa} \), this too would be a case of high seismic efficiency \( h = \frac{a}{\tau_s} = 0.53 \).

To put the scenarios in context with seismological observations they are plotted versus seismic moment in **Figures 3 and 4** by assuming a circular rupture. Using the average slip from the exhumed pseudotachylites of 0.59 m [Di Toro et al., 2006], and the stress drops from **Table 1**, we can calculate the radius

\[
 r = \frac{7\pi \mu \Delta \delta}{16 \Delta \tau_s} \tag{6}
\]

(area \( A = \pi r^2 \) and seismic moment \( M_0 = \mu A \Delta \delta \), **Table 1**). For all scenarios the apparent stress is outside the typical values. All the stress drops except for the case where a typical value was assumed are in the upper few percent of the observations. More extreme earthquake source properties result if the lab-inferred value of the melt shear strength is used instead of the field values.

**Discussion**

Partitioning of radiated and thermal energy during earthquake slip might be most easily considered by normalizing equation (3) by the average stress, defining a total thermal efficiency, \( \hat{\zeta} = 1 \),

\[
 \hat{\zeta} = 1 \tag{7}
\]

the ratio of the average dynamic shear strength to the average co-seismic shear stress, where \( \eta \) is the seismic efficiency as defined above. As noted by McGarr [1994; 1999], for dynamic rupture controlled by low temperature friction at very small displacements, the thermal efficiency is high, for example, greater than 90% [Lockner and Okubo, 1983], and the seismic efficiency is less than 10%. However, for much more extreme dynamic weakening, such as seen for shear
melts with low dynamic shear strength, so long as the initial stress is high, the seismic efficiency must be significantly larger than it is in low temperature friction experiments.

In this context, we can draw a number of conclusions about earthquake source properties associated with the pseudotachylites. Based on our four scenarios, we expect that radiated energy will be similar to or exceed shear heating during the earthquake-generated formation of natural shear melts, equivalently the seismic efficiency is similar to or exceeds the thermal efficiency. A related conclusion is that, because the radiated energy is large, from equation (3), fault shear stress during earthquakes cannot be estimated from exhumed pseudotachylite; the estimates from previous studies assumed negligible radiated energy and directly equated shear stress with the field-measured strength. Thus the estimates from prior studies are likely an implausible lower bound on the shear stress and if so the field studies of exhumed pseudotachylite have underestimated stress. The degree that stress differs from strength depends on how much the slip overshoots (or undershoots) the value that would result from the dynamic stress drop alone (the difference between the final stress and the shear strength) and also on the ‘strength excess’ (how much the failure strength of the fault exceeds the initial stress, see discussion below). Our calculations suggest underestimation by 1.9 to 2.8 times. Overshoot is not determined in the existing shear melting laboratory experiments but it is an active target for laboratory investigation [e.g., Sone and Shimamoto, 2009; Di Toro et al., 2011a]. Overshoot might reasonably be inferred from careful measurement in subsequent tests or in relatively simple calculations of dynamic shear melting. According to this analysis, earthquakes that produce pseudotachylite are outside the range of seismic observations of apparent stress (Figure 4).

Reconciling the energy balance.

There are, however, a number of ways in which our energy accounting may have gone astray. Much uncertainty in our balance is associated with the choice of a Madariaga source model that has the largest stress drop of the conventional models. Still, had we used a dataset in which the stress drops were determined using the Brune model that has the lowest stress drops, apparent...
stress still would be out of the bounds of the Baltay et al. [2010] dataset for all four scenarios, and the discrepancy between the predicted and observed stress drops would be even larger. As above, while acknowledging that the choice of source model has first order implications for earthquake source properties, source model choice does not effect our conclusion that the presence of pseudotachylite implies an unusual earthquake source. Additional discussion of source models is found in section 3.2 below.

We now consider whether relaxing the two critical assumptions about initial stress and dissipated energy may allow shear melting to produce more typical earthquake source properties. First, we have assumed that the heat inferred from pseudotachylite is equivalent to all energy that does not go into the radiated field (i.e., \( = ^{t}m \)). This ignores any off-fault damage that may be generated during rupture, such as brittle failure associated with stress concentrations about the tip of the propagating rupture [Andrews, 1976; 2005] or from slip on rough fault surfaces [Chester and Chester, 2000; Dieterich and Smith, 2009; Dunham et al., 2011]. Such energy is most often partitioned into a 'shear fracture energy' term in an expanded energy balance [e.g., Tinti et al., 2005]. Fracture energy is heat and latent-heat, the energy that goes into the creation of shear and tensile fracture surfaces and into slip on shear fractures in the damage zone about the rupture [Ida, 1972; Andrews, 1976]. In well-posed dynamic rupture models it is the portion of this energy associated with inelastic deformation about the tip of the rupture that limits the propagation speed [Andrews, 1976; 2005]. Andrews [2005] has further shown that the size of this energy contribution scales with the dynamic stress drop, thus mechanisms such as shear melting, which produce large strength losses, implicitly require some compensation in off-fault fracture energy as well as in radiation.

Second, we have assumed up to this point that the initial stress is approximately equal to the static fault strength which, in the case of the felsic crystalline rocks of the motivating studies, implies high initial stress in the crust. If instead we assume that the initial stress is lower than the failure stress, as depicted in the schematic Figure 2, there is a strength excess, \( S_e \) defined by the
difference between the failure strength and the initial stress [Andrews, 1985]. Such an excess arises naturally in regions with strength or stress heterogeneity. For example imagine a fault surface that on average is strong but with a limited contiguous region of weak material. If the incipient rupture starts in that weak area and that region is sufficiently large and slips far enough to raise the stress on the adjacent portion of the strong region to its failure stress, then an earthquake rupture can occur at a lower stress than the average failure strength of the fault.

To relax both critical assumptions about initial stress and dissipated energy we modify equation (3). To consider contributions of damage to source properties it is convenient to use a stress-measure of fracture energy. Fracture energy, $G_e$, has the dimensions of energy per unit area, so the 'fracture stress' then is fracture energy divided by the total slip, $c = G_e / \tau_s$. Replace the shear resistance in (3) with the sum of that which goes in to shear heat and that which resides in fracture energy, $\hat{\tau} = \hat{\tau}_m + \tau_c$. To incorporate the strength excess we replace the average stress in (3) with $0 - \Delta \tau_s / 2$, and replace the initial stress with $p - S_e$. Making these substitutions the balance (3) becomes

$$c + S_e = \frac{p - s}{2} a \hat{\tau}_m.$$  

Implementing (8a) for pseudotachylite, $\tau_p = 104$ MPa, and $\hat{\tau}_m = 26.8$ MPa. To produce a stress drop within the 95% bound and apparent stresses to be at the upper limit of the observations, corresponding to $\Delta \tau_s = 40$ and $\tau_d = 10$ MPa, respectively, (8a) is

$$c + S_e = 47.2 \text{MPa}$$  

Fracture energy.

If the right-hand side of (8b) were all due to fracture energy ($S_e = 0$), the fracture stress would exceed the stress drop. For comparison with typical observations, a measure of the associated efficiency is the ratio of fracture energy times the fault area to the energy associated with the stress drop: $c = G_e / \tau_s$; equivalently the ratio of the fracture stress to the stress drop: $\hat{c} = c / \tau_s$. Beeler et al. [2012] compiled some limited and model-dependent data on this
efficiency from *Abercrombie and Rice* [2005] and found no natural values greater than 0.5. The minimum fracture efficiency to bring the pseudotachylite data in line with typical earthquakes is 1.2. However, as none of the prior estimates of fracture stress or efficiency strictly include off-fault damage or consider the impact of roughness on fracture energy, these remain topics for further research.

**The strength excess and fault roughness.**

Consider instead that all of the right-hand side of (8b) was from the strength excess ($\tau_c=0$), then the difference between the initial stress and the failure strength would be ~47 MPa. In that case the heterogeneity would have to be quite high in association with these earthquakes in crystalline rock. Since the source region is a batholith and arguably not highly heterogeneous in elastic or friction properties we can only appeal to stress heterogeneity to produce the necessary strength excess. Some insight into the allowable amplitude of stress heterogeneity may be found in studies of roughness contributions to shear strength [*Chester and Chester*, 2000; *Dieterich and Smith*, 2009; *Dunham et al.* 2011; and *Fang et al.* [2013]. The idea is that fault shear resistance consists of two components, the shear resistance due to frictional slip on a planar fault surface, and that which results from fault roughness. Based on measurements of natural fault roughness, the amplitude to wavelength ratio $\alpha$ appropriate for faults that host intermediate sized earthquakes is between $10^{-3}$ and $10^{-2}$ [*Power and Tullis*, 1991; *Sagy and et al.*, 2007]. According to the modeled estimates to date, the upper end of this range produces dramatic stress heterogeneity on the fault and significant additional shear strength beyond the interface friction [*Chester and Chester*, 2000; *Dieterich and Smith*, 2009], deemed roughness drag, $\tau_{drag}$, by *Fang and Dunham* [2013]. How roughness may define the strength excess would be to allow earthquake nucleation on relatively flat portions of the fault at stress levels equal to the frictional strength.

Since roughness drag increases the shear heating above that associated with slip on planar surfaces with the same frictional strength [*Griffith et al.*, 2010], this contribution is included in
the pseudotachylite-estimated co-seismic shear strength (1b). Drag may be used to explain the
difference between lab and field-measured values of shear strength. Formally

\[ \text{drag} = \frac{8}{\lambda_{\text{min}}} \cdot 2G', \]  

(9)

where \( \lambda_{\text{min}} \) is the minimum wavelength of the roughness and \( G' \) is the shear modulus divided by
1 minus Poisson's ratio [Fang and Dunham, 2013]. Taking the ratio of slip to \( \lambda_{\text{min}} \) to be of order
one [Fang and Dunham, 2013], the amplitude ratio is \( \frac{\alpha = \text{drag}}{\sqrt{G \cdot 8^3}} \). Assuming the
difference between the lab and field shear strengths (~16 MPa) is the dynamic roughness drag,
and \( G' = 40 \) GPa, then \( \alpha = 0.0013 \).

The roughness drag as estimated by Fang and Dunham [2013] (9) and in the prior study by
Dieterich and Smith [2009] is calculated for a discontinuity in otherwise intact rock assuming a
small amount fault slip relative to the smallest wavelength of roughness, elastic stress transfer,
and no dilatancy. Results of these assumptions are that the roughness drag is not pressure
dependent and it does not depend on the absolute level of the differential stress. As such the
same roughness drag applies to both the sliding and failure strengths, at all depths, so long as the
amplitude and characteristics of the roughness are not changed substantially by slip or by
ambient stress levels. Accordingly our estimated value of 16 MPa inferred from sliding is also
the strength excess due to fault roughness-generated stress heterogeneity. Even if we allow that
our failure strength of 104 MPa is overestimated by 16 MPa, that is not enough of a strength
excess to bring the pseudotachylite source properties in line with more typical earthquakes.

Admittedly these estimates do not consider contributions from material heterogeneity;
nonetheless those should be small in the relatively homogeneous source region of the
pseudotachylite. Contributions from slip heterogeneity are also not considered. Since those will
correlate with fault roughness in a homogeneous material [Duham et al., 2011; Fang and
Dunham, 2013] we expect that the difference between our estimate and the needed value of 47
MPa precludes reconciling the observations and typical earthquake source properties with this
model of the strength excess. Nonetheless, given that our roughness estimate is based entirely on
the difference between field and lab melt shear strengths, along with the large uncertainties
associated with the field-inferred strength, and our assumption of the high Byerlee failure
strength, the strength excess remains perhaps the most poorly constrained of all the poorly
constrained earthquake source properties.

To assess whether the combined effects of strength excess and fracture energy are sufficient to
bring pseudotachylite into line with typical earthquakes, use the strength excess of 16 MPa in
(8b) to reduce the needed fracture stress from 47 to 31 MPa. The associated minimum fracture
efficiency would be ~0.8, exceeding the limited observations [Abercrombie and Rice, 2005] by a
factor of 1.5. Again we conclude that seismically generated pseudotachylite requires atypical
earthquake source properties, a result that seems robust even when limitations of the assumptions
are taken into account.

Future work on fault roughness.

There are physical limits on the estimate of roughness drag in equation (9). The underlying
theory breaks down at high but realistic amplitude ratios [Dieterich and Smith, 2009; Fang and
Duham, 2013], especially at near surface and intermediate depths. For example, at a modest
effective normal stress of 100 MPa the strength of intact granite is about 150 MPa while the
frictional strength is about 85 MPa. From (9), using the same slip and elastic assumptions as
previously, the roughness drag of a fault at the upper end of the natural amplitude ratio range,
$\alpha = 0.01$, is 990 MPa, more than ten times the frictional strength and approximately six times the
intact rock strength. Empirically this is out of bounds and arises mostly because the estimate
forbids the dilatancy that limits rock and fault strength in the first place [Brace et al., 1966;
Escartin et al., 1997]. Similarly at more modest values of the amplitude ratio but at greater depth
where the normal stress is high, according to (9), friction will dominate the shear resistance as
friction increases with normal stress while the roughness contribution does not. This is hard to
reconcile with existing laboratory data in which both sliding friction and intact rock strength
increase with confining pressure. In practice many of these issues with (9) are dealt with in
numerical fault models [Fang and Dunham, 2013]. There, the stresses that arise from slip on rough surfaces are calculated incrementally with slip (rather than assuming that $\Delta \delta/\lambda_{min} = 1$) and when the drag stress reaches the failure strength of surrounding rock the material yields via a separate pressure dependent plasticity relation.

Simpler models of rough faults and the bounds on the resulting stress heterogeneity might be constructed using existing laboratory data. Among the non-physical aspects of the theory underlying (9) are: no dilatancy and that the fault is zero-thickness and fully localized resulting a stationary shear zone. On the latter, natural fault zones have finite thickness that likely provides some degree of freedom to deform internally to accommodate roughness of the fault bounding rock. On the former, disallowing rigid and fracture dilatancy on a fault between rock surfaces is contrary to the most basic physical observations of brittle deformation and frictional slip [e.g., Brace et al., 1966; Marone et al., 1990]. Because of these issues we suggest that the contribution of roughness to fault shear resistance is inherently pressure dependent, such that it is smaller than (9) at near surface conditions where, in the presence of very low normal stress and distributed shear, roughness likely leads to rigid dilation rather than damage in the surrounding rock, and also so that the contribution from roughness does not diminish relative to friction at elevated confining pressure. Furthermore the roughness contribution is bounded by existing experimental data to be less than or equal to the strength of intact rock minus the frictional failure strength at the confining pressure and temperature of interest. Future experiments on faults with amplitude ratios between 0.01 and 0.001, at effective normal stresses and temperatures spanning those of the brittle crust should better establish the contributions of roughness to fault strength.

**Stress drop and the choice of source model.**

Choice of source model has a very large effect on the inferred bounds of static stress drop, such as the 95% bound $\Delta \tau_s = 40$ MP from Allman and Shearer [2009] that is superimposed on Figure 3. The Madariaga source produces stress drops that are a factor of 2.6 larger than from the Sato and Hirasawa [1973] model and 5.5 times larger than Brune [1970]. Decreasing the
upper bound in Figure 3 to that which would be inferred from Brune [1970], would place all scenarios except #3 further out of range of typical stress drops. This model dependency of static stress drop is a significant barrier to using stress drop as a metric in studies of source physics [McGarr, 1999]. And while there is no strict constraint on stress drops from pseudotachylite, our analysis suggests that regardless of the source model used the stress drops from pseudotachylite are unusual for earthquakes.

There are, unfortunately, additional fundamental problems relating the stress drop from standard source models to pseudotachylite. For each of the Brune, Sato and Hirasawa and Madariaga source models, the ratio of apparent stress to static stress drop is fixed with a value 0.22 < τ_a / Δτ_s < 0.4. In other words, these are all crack-like rupture models that overshoot. In contrast, experimental measurements suggest that the shear melts show rapid 'co-seismic' strength recovery [Di Toro et al., 2011a] that, when extrapolated to a propagating, confined rupture, are more consistent with undershoot and pulse-like propagation. In the absence of a definitive earthquake source model that allows for undershoot or seismic methods that reliably distinguish undershoot from overshoot it will remain difficult to use static stress drops to relate laboratory observations to earthquake seismology.

**Source properties of shear melts.**

The source parameters in scenarios 1 to 4 are perhaps the seismic corollary to the interpretation of the geologic record that pseudotachylite is rare [Sibson and Toy, 2006]. Although the interpretation is not without controversy [Kirkpatrick et al., 2009; Kirkpatrick and Rowe, 2013], the corollary is not unexpected. While pseudotachylite is known to form under a wide range of conditions, for example in presence of fluids, in metamorphic terrains and even in large events within melange [e.g. Toy et al., 2011; Bjornerud et al., 2010, Meneghini et al., 2010], the friction melting experiments of Di Toro et al. [2006a] suggest that pseudotachylites are easily formed during imposed localized slip on pre-cut faults in cohesive rocks that are dry. Many field studies also suggest that the typical ambient conditions of pseudotachylite is the dry
crystalline basement of the continental crust [Sibson and Toy, 2006], as is the case for most nappes in the Western Alps, where pseudotachylites are not uncommon fault rocks [Pennacchioni et al., 2007]. The higher stress drops characteristic of intraplate earthquakes [Scholz et al., 1986], including those of some very high stress drop earthquakes [e.g., Viegas et al., 2010; Ellsworth et al. 2011] may indicate related properties of the source, once differences in source model are accounted for. Large stresses relative to the failure strength, large stress drops, and relatively low fault roughness may lead to some diagnostic rupture properties associated with pseudotachylite formation. High initial stress levels promote a strong tendency for super-shear rupture up to the compressional wave speed, specifically when the ratio of the strength excess to the dynamic stress drop, $S$, is lower than 1.77 [Andrews, 1985] as claimed to be observed experimentally by Passelegue et al. [2013]. Taking the 16 MPa strength excess, an initial stress of 104 MPa, and sliding strength of 26.8 MPa, Andrews' $S$ ratio is no higher than 0.26 and super shear rupture is expected. A large stress drop, low roughness and high initial stress may also tend to promote propagation as an expanding crack rather than as a slip pulse [Zheng and Rice, 1998].

An appealing third idea explaining the difference between typical earthquake stress drops and the ~77 MPa values inferred for pseudotachylite dynamic stress drops relaxes our implicit assumption that pseudotachylites are representative of the dynamic properties of the earthquakes that generated them. Sibson [2003] suggested that faults have significant spatially varying dynamic properties, allowing the majority of the shear strength to be concentrated in regions of high geometric complexity (e.g., fault bends or step-overs). Fang and Dunham [2013] reached a similar conclusion when considering large ruptures. This kind of model, where part of the fault is dynamically weak but most of the shear strength is concentrated elsewhere, perhaps in relatively limited areas, is similar to the numerical fault models with heterogeneous stress conditions that allow fault slip at low average stress levels [Lapusta and Rice, 2003; Noda et al., 2009]. Under the Sibson [2003] conceptual model, pseudotachylite is generated on parts of the fault that are
geometrically simple prior to rupture, but it does not contribute significantly to the dynamic shear strength of the entire fault. Our scenario 3 where we have imposed a typical stress drop is related to this kind of event. Doing so requires that the rupture dimension is much larger than the other scenarios, producing an M6 earthquake. In any event, the Sibson model would remove the discrepancy between typical earthquake stress drops and the implied strength loss by pseudotachylite in granite rock and would allow pseudotachylite to be more common as advocated by Kirkpatrick and Rowe [2013]. Meanwhile the mechanical properties of pseudotachylite would be largely irrelevant to the average seismically-inferred source properties such as static stress drop and apparent stress. Testable implications of this model would be that during seismic slip the majority of shear generated heat would be concentrated in distinct local regions of low stress drop. In cases where the stress is high, regions of low shear strength due to the formation of pseudotachylite would appear as 'asperities' in seismic inversions where the stress drop and radiated energies are high [e.g., Kanamori, 1994; Bouchon, 1997; Kim and Dreger, 2008]. A hope is that the character of radiated energy from such asperities could be quantitatively related to laboratory and field studies of fault properties and in some cases related to a particular shear deformation mechanism in the fault zone (e.g., melting, thermal pressurization). This would require particular mechanisms to have characteristic source properties, for example a distinctive frequency content. Making such a link between various source properties and source mechanisms might be made using synthetic seismograms generated by spontaneous dynamic rupture simulations [e.g., Andrews, 2005; Harris, 2004], as developments in that field are directed specifically at the physics within the source [Harris et al., 2009].

Conclusions

The analysis of the energy budget and source properties of pseudotachylite-generating intermediate sized earthquakes of the Gole Larghe fault zone in the Italian Alps where the dynamic shear strength is well-constrained by field and laboratory measurements suggests these
earthquakes have unusual source parameters. The assumptions are: that seismically determined corner frequency relates to stress drop by the Madariga [1976] relation, that the heat inferred from pseudotachylite thickness and fault displacement is equivalent to all energy that does not go into the radiated field, and that the initial stress is approximately equal to the static fault strength. For the felsic crystalline rocks of the source region, the final assumption results in an initial shear stress on the order of 100 MPa. Stress drops and apparent stress are larger than a few 10 's of MPa, unlike typical earthquakes, and the radiated energy equals or exceeds the shear-generated heat. Relaxing these assumptions, the observations still cannot be reconciled with typical earthquake source properties unless fracture energy is routinely significantly greater than in existing models, pseudotachylite is not representative of average fault shear strength during the earthquake that generated it, or unless the strength excess is larger than we have allowed.

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**References**


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Appendix - Estimated initial stress

The hypocentral source region of the pseudotachylite at Gole Larghe was at approximately 10 km depth, in a strike-slip faulting regime in Tonalite [Di Toro and Pennacchioni, 2005; Di Toro et al., 2005]. To estimate the ambient stress level we follow these cited prior studies and assume an Andersonian strike-slip regime [Anderson, 1951] in which the lithostatic stress from overburden $\sigma_L$ is the mean of the greatest and least principal stresses $L = m = \left( S + \frac{S_3}{2} \right)$. The fault is optimally oriented for failure in the stress field and assumed to limit the stress level in the surrounding rock. These conditions are depicted in the Mohr diagram (Figure A1), where the fault is assumed to be cohesionless with a friction coefficient $\mu = \tau / \sigma_e$, defining the friction angle $\mu = \tan \phi$, $\tau$ is shear stress, $\sigma_e$ is the effective normal stress ($\sigma_e = \sigma_n - p$), $\sigma_n$ is normal stress and $p$ is pore fluid pressure. Here the ratio of pore pressure to the lithostatic stress is denoted by the ratio $\lambda = p / \sigma_L$ [Sibson, 1974]. From the Mohr construction (Figure A1), effective normal stress is

$$\sigma_e = \sigma_L \left( 1 - \frac{1}{\lambda} \right) \cos^2 \phi. \quad (A1)$$

The lithostatic gradient is taken to be 26 MPa/km and $\sigma_L = 260$ MPa. To estimate a representative effective normal stress we follow Di Toro et al. [2005] and average the results from assuming the pore pressure is hydrostatic with pore pressure gradient 10 MPa/km, with those from assuming dry conditions. That is, using $\lambda = 10/26$ and $\lambda = 0$ in (A1), resulting in $\sigma_e = 93$ and 151 MPa, and a representative $\sigma_e = 122$ MPa for $\mu = 0.85$ [Byerlee, 1978] that is appropriate for crystalline rock. These assumptions correspond to a shear resistance at failure of $\tau = 104$ MPa.
Table 1. Possible earthquake source properties for shear melting at 10 km depth, effective normal stress = 122 MPa and initial stress of 104 MPa.

<table>
<thead>
<tr>
<th>scenario</th>
<th>average strength, ( \hat{t} ) (MPa)</th>
<th>static stress drop, ( s = 0 )</th>
<th>apparent stress, ( \tau_a ) (MPa)</th>
<th>overshoot, ( = 0.5 \frac{a}{s} )</th>
<th>seismic efficiency, ( = \frac{a}{\hat{t}} )</th>
<th>thermal efficiency, ( \hat{t}/- )</th>
<th>( r ) (m)</th>
<th>( A ) (m²)</th>
<th>Moment (Nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Orowan ( \hat{t} = 1 )</td>
<td>26.8</td>
<td>77.2</td>
<td>38.6</td>
<td>0</td>
<td>0.59</td>
<td>0.41</td>
<td>78.7</td>
<td>3.1e5</td>
<td>1.1e15</td>
</tr>
<tr>
<td>complete stress drop ( s = 0 )</td>
<td>26.8</td>
<td>104</td>
<td>25.2</td>
<td>0.26</td>
<td>0.48</td>
<td>0.52</td>
<td>61.8</td>
<td>1.7e5</td>
<td>1.3e15</td>
</tr>
<tr>
<td>typical stress drop ( \Delta \tau_s = 3.9 ) MPa</td>
<td>26.8</td>
<td>3.9</td>
<td>75.3</td>
<td>-19.3</td>
<td>0.73</td>
<td>0.27</td>
<td>2575</td>
<td>1.2e8</td>
<td>1.2e18</td>
</tr>
<tr>
<td>typical overshoot ( = 0.166 )</td>
<td>26.8</td>
<td>93</td>
<td>30.7</td>
<td>57.5</td>
<td>0.166</td>
<td>0.53</td>
<td>0.47</td>
<td>59.0</td>
<td>2.1e5</td>
</tr>
</tbody>
</table>

Four scenarios are considered and source parameters are tabulated for an average shear strength of 26.8 MPa (field). For each scenario the assumed values are in bold in the Table. The values for the stress parameters in the Table can be derived directly from the initial, and average strength, the definitions in the column headers, and the assumptions that are listed in the scenario rows, using the assumed (bold) table values.
Figure Captions

Figure 1. Natural and laboratory observed shear strength of granitic melt. Shown for reference is the approximate static strength of pre-existing faults in granitic rocks (solid line) [Byerlee, 1978]. The dashed line is the regression of experimental data from Di Toro et al. [2006b], extrapolated to higher normal stress. The field inferred shear strengths of Di Toro et al. [2005; 2006a], that are calculated from measured thickness-displacement ratios using equation (1c), are plotted as the open symbols at the inferred mean normal stress. The box shows the range of possible field-inferred shear and normal stresses.

Figure 2. Earthquake stress versus slip diagram after McGarr [1994]. Fault strength is shown as the heavy black line while shear stress is the heavy black dashed line between $\tau_0$ and $\tau_1$, the starting and ending stresses. The average stress, $\bar{\tau}$, is denoted by the heavy grey dashed line and the average fault strength, $\hat{\tau}$, by the grey dashed line. The apparent stress is the difference between these lines. This example is a case of overshoot [Savage and Wood, 1971] where the final stress is less than the average strength. This is also a case where the starting stress is lower than the failure strength $\tau_p$, defining a strength excess $S_e$.

Figure 3. Variation of stress drop with seismic moment. Stress drops from the previous studies of Abercrombie [1995], Tajima and Tajima [2007] and Allman and Shearer [2009]. Here all stress drops are calculated using the Madariaga [1976] model. In the case of Tajima and Tajima [2007], the stress drops were calculated using their tabled moment and corner frequency, $f_c$, using $\Delta = M_0 (f_c/(0.42 \beta))^3$ and $\beta = 3.9 \text{ km/s}$, assuming rupture propagation at $0.9\beta$, as in Allman and Shearer [2009]. An implication of these and other compilations [e.g., Hanks, 1977; Baltay et al., 2011] is that stress drop is moment independent. The dashed lines are the 99, 95, and 90% boundaries from the global dataset of Allman and Shearer [2009] (solid circles). For
example 1% of the stress drops are larger than the 99% line (110 MPa). The 95 and 90% lines are stress drops of 40.3 and 22.9 MPa, respectively. Stress drops from exhumed pseudotachylite for the scenarios listed in Table 1 are shown in grey. Moment is calculated assuming a circular rupture, equation (6) in the text, a shear modulus $\mu = 30,000$ MPa, the average slip from the exhumed pseudotachylite (0.59 m) and the stress drops for each scenario (Table 1), see text.

Figure 4. Variation of apparent stress with seismic moment. Compilation of apparent stress (right axis) from Baltay et al. [2010; 2011]. The dashed lines are for 10 and 0.1 MPa and are the approximate bounds on the observations. The implication of this and other compilations [e.g., Ide and Beroza, 2001] is that apparent stress is moment independent. Apparent stresses for exhumed pseudotachylite for the scenarios listed in Table 1 are plotted in grey. Seismic moments for the pseudotachylite are calculated as described in the caption to Figure 3.

Figure A1. Schematic Mohr diagram of the estimated initial stress state for pseudotachylite at the Gole Larghe fault zone (see Appendix text for description).