Selective reflection from Rb layer with thickness below $\lambda/12$ and applications

A. Sargsyan$^1$, A. Papoyan$^{1,*}$, I.G. Hughes$^2$, C.S. Adams$^2$, and D. Sarkisyan$^1$

$^1$Institute for Physical Research, NAS of Armenia, 0203, Ashtarak-2, Armenia
$^2$Joint Quantum Centre (JQC) Durham-Newcastle, Department of Physics, Durham University, South Road, Durham DH1 3LE, United Kingdom
$^*$Corresponding author: papoyan@ipr.sci.am

Compiled March 14, 2017

We have studied the peculiarities of selective reflection from Rb vapor cell with thickness $L < 70$ nm, which is smaller than the length scale of evanescent fields $\lambda/2\pi$ and more than an order of magnitude smaller than the optical wavelength. A $240 \text{ MHz}$ red shift due to the atom-surface interaction is observed for a cell thickness of $L = 40$ nm. Also completely frequency resolved hyperfine Paschen-Back splitting of atomic transitions to four components for $^{87}\text{Rb}$ and six components for $^{85}\text{Rb}$ is recorded in strong magnetic field ($B > 2 \text{ kG}$). © 2017 Optical Society of America

OCIS codes: (020.3690) Line shapes and shifts; (300.6320) Spectroscopy, high-resolution; (300.6210) Spectroscopy, atomic

http://dx.doi.org/10.1364/ao.XXX.XXXXXX

Selective reflection (SR) of resonant optical radiation from the interface between an atomic vapor and the dielectric window of spectroscopic cells was initially observed by R. Wood in 1909 [1], and revisited in 1970s when narrow-linewidth tunable cw lasers became available [2–4]. Thanks to high contrast sub-Doppler signal response, the SR technique became a powerful spectroscopic tool, which was successfully used, in particular, to study the van der Waals (vdW) interaction of atoms with dielectric window of the cell manifested by a red shift of the SR frequency [5–8]. Spectroscopy with atomic vapor nanometric-thickness cells (NC) is another technique capable of yielding information on atom-surface processes. The vDW interaction of Rb and Cs atoms confined in the NC was studied in [9] using resonant fluorescence spectra.

Merging the SR and NC methods significantly extends their applied interest. On account of the dispersive shape of the signal, the SR from NC was used to lock the laser’s frequency [10]. Recently it was demonstrated that the SR from a Rb vapor NC with thickness $L \approx 370$ nm is convenient to form frequency reference of atomic transitions [11]. It was also shown that the same technique implemented for D$_1$ line of Cs and 300 nm gap thickness is expedient to study the behavior of atomic transitions in strong magnetic field [12].

In this Letter we focus on the peculiarities of selective reflection for the conditions when the response of a resonant medium is formed over an essentially sub-wavelength depth in an atomic vapor layer geometrically restricted by the two inner surfaces of the nanometric-thickness cell ($L < 70$ nm). For the first time, we have implemented a "derivative SR" (DSR) method for atomic layers with thickness in the range of tens of nm.

Fig. 1. Layout of the experimental setup: (ECDL) cw laser, (FI) Faraday isolator, (BS) beam splitter, (NC) Rb nanometric-thickness cell inside an oven, (PM) permanent magnet, (PD) photodetector, ($\lambda/4$) quarter-wave plate ("SR" and 'ref' denote selective reflection and reference channels). Upper right inset: photograph of the NC, oval marks 20 – 90 nm region. Upper left inset: geometry of the 3 reflected beams. The beam (SR) propagates in the direction of $R_2$.

The experimental arrangement is schematically sketched in Fig. 1. The collimated circularly-polarized beam of a single-frequency narrow-band ($\gamma_L \sim 1 \text{ MHz}$) cw external cavity diode laser with $\lambda = 795$ nm and power $P_L \sim 0.5 \text{ mW}$ was directed
at normal incidence onto the specially fabricated Rb NC with a large apertured area of smoothly changing thickness in the range $L = 20 - 90$ nm (see the upper left inset). The thickness $L$ was measured by an interferometric technique presented in [13]. The SR beam was carefully separated from two other beams reflected from the front and rear surfaces of the cell (see the upper right inset), and after passing through a $\lambda = 795$ nm interference filter was recorded by a photodiode (PD (middle curve), and 2.7 kG (lower curve). For labeling, see Siglent oscilloscope. Studies of a sub-Doppler spectrum emerging the derivatives of SR signal (DSR) formed in a real time by the $B = 2.4$ kG is shown in Fig.2 (upper spectrum). The lower lines are $B = 85$ kG transition diagrams for $Rb$ and $F$ notation is used in the inset diagram of Fig.2. Decoupling between $J$ and $I$ develops when $B \geq B_0$, $F$ is no longer a good quantum number, and the splitting of atomic levels is described by the projections $m_J$ and $m_f$ (hyperfine Paschen-Back regime) [16–18]. In this regime four and six atomic transitions belonging to $87$Rb and $85$Rb, respectively, remain in the spectra (as is evident in Fig.2 and Fig.3).

The influence of the applied magnetic field on the hyperfine structure is characterized by parameter $B_0 = A_{HFS}/\mu_B$, where $A_{HFS}$ is the hyperfine coupling constant for 5S level, and $\mu_B$ is the Bohr magneton [15]. $B_0 \approx 0.7$ kG for $85$Rb, and $B_0 \approx 2$ kG for $87$Rb. When $B < B_0$ (Zeeman regime), the splitting of levels is described by the total angular momentum of the atom $F = J + I$ and its projection $m_F$, where $J$ is the total electron angular momentum, and $I$ is the nuclear spin angular momentum. The $F$ and $m_F$ notation is used in the inset diagram of Fig.2. Decoupling between $J$ and $I$ develops when $B \geq B_0$, $F$ is no longer a good quantum number, and the splitting of atomic levels is described by the projections $m_J$ and $m_f$ (hyperfine Paschen-Back regime) [16–18]. In this regime four and six atomic transitions belonging to $87$Rb and $85$Rb, respectively, remain in the spectra (as is evident in Fig.2 and Fig.3).

The recorded DSR spectrum for $L = 50 \pm 2$ nm recorded at $B = 2.15$ kG. Upper-right inset: $B = 0$ spectra (from top to bottom: SR, DSR, and reference), exhibiting $-130$ MHz red shift with respect to $87$Rb $F_g = 1 \rightarrow F_e = 1$, 2 reference frequencies. Upper-left inset: the estimate of distance-dependent vdW red shift; the horizontal line tangent to an overall curve 3 marks the minimum shift value ($-130$ MHz).

1. In the figures the excited levels are marked by primes.

Fig. 3. Experimental DSR spectrum for $L = 50 \pm 2$ nm recorded at $B = 2.15$ kG. Upper-right inset: $B = 0$ spectra (from top to bottom: SR, DSR, and reference), exhibiting $-130$ MHz red shift with respect to $87$Rb $F_g = 1 \rightarrow F_e = 1$, 2 reference frequencies. Upper-left inset: the estimate of distance-dependent vdW red shift; the horizontal line tangent to an overall curve 3 marks the minimum shift value ($-130$ MHz).
transitions. To estimate the frequency shift for $^{87}$Rb, D$_1$ line arising from interaction of an individual atom with two dielectric windows of the cell (w1 and w2), we have plotted in the upper-left inset the distance-dependent frequency shifts separately for w1: $\Delta \nu_{vdW} = -C_3/z_1^2$ (curve 1), and for w2: $\Delta \nu_{vdW} = -C_3/z_2^2$ (curve 2), where $z_1$ and $z_2$ are distances of the Rb atom from w1 and w2, respectively (in $\mu$m). The overall shift is depicted by curve 3, which is the sum of curves 1 and 2. For $L = 50$ nm, the recorded $\sim 130$ MHz shift is obtained by taking vdW coefficient $C_3 = 1.0 \pm 0.1$ kHz x $\mu$m$^3$, which is consistent with the results of previous studies [7]. As is seen from the diagram, the maximum of the spectral density of an overall signal (the shifted peak) corresponds to the minimum value of the shift, so this value is estimated by the expression

$$\Delta \nu_{vdW} = -2C_3/(L/2)^3.$$  \hspace{1cm} (1)

To record SR signals above the noise level for even smaller cell thickness $L = 40 \pm 2$ nm, the cell temperature was further increased to $T_R = 180$ °C (vapor density $\sim 5 \times 10^{14}$ cm$^{-3}$). The DSR spectrum for this thickness and $B \approx 2.15$ kG is presented in Fig. 4. In these conditions the transition peaks become broader, but the linewidth $\gamma_{DSR} \approx 380$ MHz still does not exceed $\sim 500$ MHz transition width obtained with 1 mm-long Rb cell [18]. Noteworthy, the $F_g = 1 \rightarrow F_e = 1$ transition well seen in DSR spectrum, but hardly at all in the reference trace. This illustrates the applied value of the method. An estimation of the number of atoms contributing to SR signal (Fig.4) for 0.5 mm beam diameter, $L = 40$ nm, and atomic density $5 \times 10^{14}$ cm$^{-3}$ gives $\sim 5 \times 10^8$. Note that the vdW shift for $^{85}$Rb and $^{87}$Rb transitions for the same $L$ value is approximately equal.

Complete resolution of all the DSR peaks makes favorable the determination of a B-field, which can be done in two convenient ways: a) by measuring the frequency shift of DSR peak 1 ($\nu_1$) from the reference transition $F_g = 1 \rightarrow F_e = 2$ (see the inset of Fig.5), also taking into account the value of vdW shift; b) by measuring the frequency separations between the individual transitions $a = \nu_{10} - \nu_1$ and $b = \nu_2 - \nu_1$, and exploiting the dependence of the $a/b$ ratio on the B-field. Note that for case b) there is no need for a frequency reference, and also the value of vdW shift is not important, being the same for all four transitions. Both B-field measurement techniques are graphically elucidated in Fig.5.

Fig. 6. Dependence of DSR linewidth $\gamma_{DSR}$ versus $L$. The inset: four DSR peaks of the $^{85}$Rb D$_1$ line at $L = 25$ nm and $B = 2$ kG; $\gamma_{DSR} \approx 600$ MHz. The inset shows theoretical spectrum calculated using dependences of the frequency shifts and transition probabilities versus magnetic field, see [12]. The SR and DSR broadening observed with reduction of $L$ and/or increase of $T_R$ is caused by vdW interaction, as well as atom-window and atom-atom collisions. The measured DSR broadening $\gamma_{DSR}$ versus $L$ (cross marks) is presented in Fig.6, along with fitted $\gamma_{DSR}[\text{MHz}] \approx 15000/L[\text{nm}]$ dependence (dotted line). Note that the DRS broadening is mainly caused by the vdW interaction (the self-broadening rate resulting from the Rb-Rb collisions is $\approx 1$ GHz/Torr, yielding much smaller contribution). Measuring magnetic field with nanometric-scale spatial resolution remains a challenge in a variety of problems, in particular when strong gradient fields are applied (e.g. 40 kG/mm...
in [19]). Even for \( L = 25 \text{ nm} \), \( \gamma_{\text{DSR}} \) is 600 MHz, so measuring the ratio \( a/b \) for a NC filled with \(^{87}\text{Rb}\) isotope, it is possible to determine the \( B \)-field value with the uniform \( \sim 10 \text{ G} \) precision over the 100 – 10000 G range.

For comparison of the DSR with the absorption spectrum under the same conditions (for parameters, see the caption of Fig.7), we have used \( F_y = 3 \rightarrow F_z = 3.4 \) transitions of Cs D\(_1\) shown in the inset of Fig.7. For this transition the frequency separation of excited levels, \( \sim 1.2 \text{ GHz} \), is the largest among the alkali metals. The latter is advantageous for avoiding the overlap of absorption lines of neighboring transitions. In Fig.7 the upper curve shows the absorption spectrum for \( L \approx 52 \text{ nm} \), and the middle curve presents DSR spectrum. The lowest line is the reference transmission spectrum obtained with an auxiliary NC with \( L = \lambda \), exhibiting VSOP resonances at \( F_{y'} = 3 \rightarrow F_{z'} = 3.4 \) transitions of \(^{133}\text{Cs} \) [14]. The \( F_{y'} = 3 \rightarrow F_{z'} = 3 \) and \( F_{y'} = 3 \rightarrow F_{z'} = 4 \) transitions are strongly overlapped in the absorption spectrum, while DSR-peaks for the same transitions are obviously advantageous: they are background-free, completely resolved, and exhibit noticeable frequency red shift (\( \sim 140 \text{ MHz} \) and 160 MHz, respectively). Estimation of \( C_3 \) vdw coefficient obtained from Eq.(1) gives \( C_3 \approx 1.4 \pm 0.1 \text{ kHz} \times \mu \text{m}^3 \).

The SR signal exhibits a low divergence, relatively high power (\( \approx 0.5 \% \) of the incident radiation), a linear response remaining up to \( P_{L} \approx 5 \text{ mW} \), and high signal-to-noise ratio. Consequently the DSR technique can be used for high-distance remote monitoring and mapping of both homogeneous and highly inhomogeneous \( B \)-fields in a wide range with \( \sim 40 \text{ nm} \) spatial resolution (for comparison with other types of magnetometers, see book [20]). The DSR technique employing nanometric-thickness cells is simple and easily realizable. We note that the recent development of a glass NC [21] can make this technique widely available, both for studies of atom-surface interaction and \( B \)-field mapping.

The work was partially supported by MES RA (projects No. 15T-1C040 and 15T-1C277). The authors are grateful to A. Sarkisyanyan for fabrication of nanocell, and to A. Tonoyan for theoretical calculations.

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