Generating artificial reference images for open loop correlation wavefront sensors

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ABSTRACT
Shack–Hartmann wavefront sensors for both solar and laser guide star adaptive optics (with elongated spots) need to observe extended objects. Correlation techniques have been successfully employed to measure the wavefront gradient in solar adaptive optics systems and have been proposed for laser guide star systems. In this paper, we describe a method for synthesizing reference images for correlation Shack–Hartmann wavefront sensors with a larger field of view than individual sub-apertures. We then show how these supersized reference images can increase the performance of correlation wavefront sensors in regimes where large relative shifts are induced between sub-apertures, such as those observed in open-loop wavefront sensors. The technique we describe requires no external knowledge outside of the wavefront-sensor images, making it available as an entirely ‘software’ upgrade to an existing adaptive optics system. For solar adaptive optics we show the supersized reference images extend the magnitude of shifts, which can be accurately measured from 12 per cent to 50 per cent of the field of view of a sub-aperture and in laser guide star wavefront sensors the magnitude of centroids that can be accurately measured is increased from 12 per cent to 25 per cent of the total field of view of the sub-aperture.

Key words: atmospheric effects – instrumentation: adaptive optics – Sun: granulation.

1 INTRODUCTION
Adaptive optics (AO) is integral to all next-generation solar and Extremely Large Telescope (ELT) class ground-based telescopes, including the European Solar Telescope (Collados et al. 2013) and the ELT (Cuby et al. 2010; Davies et al. 2010). These telescopes will employ complex AO systems that use tomography and multiple deformable mirrors in order to increase either the corrected field of view (FOV) using multi-conjugate adaptive optics modalities (Davies et al. 2010) or the number of corrected targets (multi-object adaptive optics) (Cuby et al. 2010).

Extended objects are currently the only source available for wavefront sensors (WFSs) in solar AO (typically solar granulation) and are also present on ELTs due to laser guide star (LGS) elongation. The impact of LGS elongation on AO is the subject of ongoing studies (Gilles & Ellerbroek 2006; Thomas et al. 2008; Conan et al. 2009; Schreiber et al. 2010; Anugu, Garcia & Correia 2018). Furthermore, the available WFS camera options for first light ELT instruments impose restrictions on the available FOV resulting in truncation, or limited sampling, of the LGS plume. Similarly, for solar AO the effect of how to best use and analyse extended sources in WFSs is the subject of similar studies (Löfdahl 2010). One solution to the problem of measuring centroids on extended structure for solar AO, proposed by Rimmle & von der Luehe (1990), is the use of correlations in order to accurately measure centroids when observing extended structures. This technique has been employed successfully in a number of solar AO systems, including the Swedish Solar Telescope (SST) (Scharmer et al. 2002), GREGOR (Soltau et al. 2013), and the New Solar Telescope (Cao et al. 2010), and has also been shown to improve LGS WFSs on-sky (Basden et al. 2014).

Correlation techniques image are subject to the same noise sources as other centroiding techniques, including all of the noise sources associated with electrical and optical noise. However, there is also another source of noise that correlation techniques are subject to, which most other techniques are not. This extra noise is due to different structure being present in the reference and sub-aperture images which are cross-correlated. This noise term is a source of model error, and in the rest of the paper referred to as ‘model error’. Model error is especially relevant in open-loop AO systems, whose WFSs observe the full strength of atmospheric turbulence, not just residuals after a correction has been applied to the wavefront, as is the case for closed-loop WFSs.

In this paper, we propose a computational solution to model error that employs the use of multiple sub-apertures to generate a...
tions; this manifests itself as a high background in the correlation image. There is structure distributed continuously in all directions, the technique described in Townson, Saunter & Kellerer (2015) was used in order to choose optimal centroiding parameters for estimating the centre of mass (COM) of the correlation images. The simulations were also run in noiseless conditions to only show the effects of model error.

2 MODEL ERROR

Model error is defined here to be noise sources that arise in correlation images from structure that is not present in both the reference and sub-aperture images; this is also referred to as ‘truncation’ for LGS in night-time AO. An illustration of this is given in Fig. 1.

We expect the centroid measurement to correspond to the shift between the sub-aperture image and the reference image. Here the model error can be seen to add a strong signal to the correlation image, which then skews the centroid measurement away from the value of the shift between the two images. The left-hand panel shows the ‘full’ FOV, with the two yellow boxes showing the FOVs of the reference image and the sub-aperture image. The red line indicates the shift between the reference and the sub-aperture image. In the middle panel, the reference and sub-aperture images are individually displayed; it can be seen that there is an additional structure in the sub-aperture image which is not present in the reference image. The right-hand panel shows the resulting correlation image from cross-correlating the reference and sub-aperture images. The red line shows the shift between the two images, and the yellow line shows the measured centroid of the correlation image. The difference between the centroid and the true image shift is due to model error, and arises from the structure in the correlation image created from the non-common elements between the reference and sub-aperture images. This shifts the centroid estimate towards it and away from the actual value.

The example shown in Fig. 1 shows a highly simplified case where there are only two structures in the whole field. For solar granulation, there is structure distributed continuously in all directions; this manifests itself as a high background in the correlation image, with many small peaks distributed across it. In LGS images, there is continuous structure along the direction of the laser plume. Although centroiding correlation images that display structure unrelated to the overlap of content common to both images can add noise to the centroid measured, there are methods that attempt to minimize the influence of this erroneous structure, such as those in Townson et al. (2015) and Löfdahl (2010). These methods make use of windows and threshold values around the peak of the correlation image to remove the influence of non-common structure.

However, while these methods minimize some of the effects of model error, they make no attempt to remove it, leaving it present in the correlation images and still making a contribution to the error in any centroid measurement. Also, for large shifts between sub-aperture and reference images, the overlap region where the peak of the correlation signal is generated is reduced compared to a small shift. This reduction in the area of overlap for the peak of the correlation image increases the noise on the signal in the correlation image, which, in turn, adds noise to centroids on the correlation image. These effects increase when the relative shift between sub-aperture image and the reference image increases, making the problem greater for open-loop WFSs.

3 MINIMIZING MODEL ERROR

We suggest that the structure in every sub-aperture image should be wholly contained in the reference image, this should remove the effect of model error. Sub-aperture images sample different FOVs due to atmospheric turbulence perturbing the path of incoming wavefronts (Shack & Platt 1971; Roddier 1981). By combining a set of sub-aperture images, either from a single WFS frame or from a temporal sample, a larger FOV can be reconstructed than the FOV contained in any individual sub-aperture image. This larger image now samples the full FOV, which all parts of the WFS observe. This generated image can be used as the reference image for correlation WFSing and provide a reference image that includes completely the smaller individual sub-apertures. The supersized reference image can be used with subsequent frames of a WFS, so long as the structure of images in the FOV observed remains unchanged.

Each pixel in the generated reference image will be the result of combining multiple sub-aperture images, reducing noise (Basden et al. 2014). However, for the purposes of this paper, we concentrate on the model error aspect of synthesizing supersized reference images, especially addressing the ‘chicken and egg’ problem of...
Similarly to Fig. 1 the left-hand part shows a large FOV, with the yellow box highlighting the FOV of a single sub-aperture. The middle region shows just the sub-aperture image, as the reference image is taken to be the full FOV shown in the left-hand part of the figure. The right-hand part shows the correlation image from a cross-correlation of the sub-aperture image with the full FOV. The red line indicates the shift of the sub-aperture and the yellow line shows the measured centroid of the correlation image. There is still a discrepancy between the shift and the centroid measurement; however, this difference is greatly reduced compared to Fig. 1.

requiring good image shift measurements in order to generate a supersized reference image, which, in turn, is required to measure image shifts.

Fig. 2 illustrates the effect of using a supersized reference image in a correlating WFS in a similar layout to Fig. 1.

Here the full field is used as the reference image, so only one sub-aperture FOV is highlighted with a yellow window. When this sub-aperture is correlated with the full field, the resulting correlation image shows similar features to Fig. 1, but the peak of the correlation is much stronger, so the similar structure, which adds features to the correlation image, has less of an impact on the centroid measurement than it did for Fig. 1. This can be seen through the red and yellow lines overlaid on the correlation image, which correspond to the image shift and centroid measurement, respectively. The lines are much closer than they were in Fig. 1, showing the centroid is more accurate. The correlation from the overlap of the larger and smaller triangles is still in the correlation image, biasing the centroid measurement, but it has a reduced effect compared to Fig. 1.

In the next section, we go on to describe a method to generate supersized reference images using WFS data and show results from simulation on both solar granulation and LGS WFS images. However, in order to generate a supersized reference image a set of sub-aperture images must be centroided. This can be an issue in open-loop correlation WFSs and generally for correlation WFSs before the AO loop is closed. In the following, we describe a method for overcoming this issue.

### 3.1 Measuring large relative image shifts

In regimes where the relative shifts between sub-aperture images and reference images are a significant fraction of the FOV of the sub-aperture, correlation wavefront sensing fails. Using a supersized reference image can allow for shifts of this magnitude to be accurately measured; however, there is an issue in generating a supersized reference image in this regime where traditional correlation wavefront sensing fails. In addition, the centroiding parameters used to measure the location of the peak of a correlation image can add noise to the measured centroids. To minimize noise arising from centroiding parameters, we estimate the optimal window and threshold values for a COM on the correlation images using Townson et al. (2015).

Whilst large image shifts exist between some sub-apertures in any particular WFS frame, adjacent sub-apertures usually have small relative shifts due to the continuous structure of turbulence. Indeed, for any chosen sub-aperture in a WFS frame, there will be a number of other sub-apertures with similar absolute shifts. Fig. 3 shows the absolute shift of each sub-aperture for an $r_0$ of 10 cm in the upper histogram. The lower histogram in Fig. 3 shows the smallest relative

![Figure 2](https://example.com/figure2.png)

**Figure 2.** Similarly to Fig. 1 the left-hand part shows a large FOV, with the yellow box highlighting the FOV of a single sub-aperture. The middle region shows just the sub-aperture image, as the reference image is taken to be the full FOV shown in the left-hand part of the figure. The right-hand part shows the correlation image from a cross-correlation of the sub-aperture image with the full FOV. The red line indicates the shift of the sub-aperture and the yellow line shows the measured centroid of the correlation image. There is still a discrepancy between the shift and the centroid measurement; however, this difference is greatly reduced compared to Fig. 1.

![Figure 3](https://example.com/figure3.png)

**Figure 3.** The upper plot shows the distribution in shifts of sub-apertures in a WFS for an $r_0$ of 0.10 m. For a typical open-loop solar WFS, shifts larger than 1 arcsec are difficult to measure accurately, leaving a significant number of sub-apertures without a reliable centroid. However, there is nearly always another sub-aperture within this range in the WFS. The lower plot shows the absolute smallest relative shift for all sub-apertures in a WFS. Here there are significantly more pairs of sub-apertures with small relative shifts and a small fraction which have relative shifts above 1 arcsec.
shift between each sub-aperture and its closest neighbour for a WFS in the same conditions.

If we use a pixel scale of 0.25 arcsec pixel$^{-1}$ and a sub-aperture size of 16 pixels, then a shift of 1 arcsec will be the limit of what can be reliably centroided using a traditional correlation, corresponding to roughly 25 per cent of a sub-aperture width. However, by choosing the reference sub-aperture individually for every sub-aperture in the WFS, the measured shift can be minimized, reducing the magnitude of shifts measured from the upper part of Fig. 3 to that shown in the lower part. The individual relative measurements can then be ‘tiled’ across the WFS frame and combined to generate the absolute shift of each sub-aperture as shown in Fig. 4(b). The relative shift between sub-aperture $S$ and $R$ in Fig. 4(a) is likely to be large as the sub-apertures have a large physical separation, meaning the measured centroid is likely to have a large error. In Fig. 4(b), the relative shift between sub-aperture $S$ and sub-aperture $R$ can be found by summing the relative shifts between adjacent sub-apertures, as depicted by the red dotted line. There are many different combinations of sub-apertures that could be combined to calculate the relative shift between $S$ and $R$, giving many estimates of the shift. These can be combined to reduce the error on the shift measurement. This method can be extended to the full WFS frame, using a combination of all pairs of sub-apertures to generate correlation images then fitting the individual sub-aperture shifts and using a least squares type.

Using a least squares fit, which includes every possible pair of sub-apertures in a WFS frame, to estimate the centroids of a set of sub-aperture images mandates that every pair of sub-apertures is cross-correlated. While this includes the pairs of sub-apertures with large relative shifts, it also includes all of the larger number of pairs with small relative shifts that can be accurately centroided. This process can be further optimized by adding a weighting function in the least squares fit. Centroid measurements that are large can be given a low weighting, and small measures give a greater weighting. This suppresses the contribution of pairs of sub-apertures with large measured relative shifts, as these are known to include a larger model error. This leaves us with the least squares problem of the form described in equation (1):

\[
\begin{pmatrix}
  w_{0,1} & -w_{0,1} \\
  w_{0,2} & -w_{0,2} \\
  w_{1,2} & -w_{1,2}
\end{pmatrix}
\begin{pmatrix}
  R_{0} \\
  R_{1} \\
  R_{2}
\end{pmatrix}
=
\begin{pmatrix}
  R_{0,1}^{0} \\
  R_{0,1}^{1} \\
  R_{0,1}^{2}
\end{pmatrix}^{T},
\]

where $w_{i,j}$ is the weight applied to the centroid of sub-aperture $i$, cross-correlated with sub-aperture $j$, $R_{i}$ is the absolute shift of sub-aperture $i$, and $R_{i,j}$ is the relative shift between sub-apertures $i$ and $j$. The values of $R_{0,1}$ are measured by centroiding the correlation image between the sub-apertures, and the weights applied are the inverse of the magnitude of these centroids, such that

\[
w_{i,j} = \frac{1}{|R_{i,j}|},
\]

There are other metrics which could be used as a weighting variable for the least squares fit, such as the contrast or sharpness of the individual sub-aperture images or the residuals from a unitary weighted fit. However, using the magnitude of the measured shift is a natural solution to the problem we are trying to solve; in that, it suppresses the measurements that experience the largest model error. On real AO systems there may be other noise effects, which mean a different choice of weighting function would be more appropriate.

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**Figure 4.** A $3 \times 3$ grid of sub-apertures with cross-correlations shown for a single reference image Fig. 4(a) and using all pairs of sub-apertures Fig. 4(b). In Fig. 4(a), we see three ‘good’ cross-correlations, shown in blue, where the sub-apertures are adjacent and have relatively small shifts. We also see ‘bad’ cross-correlations in orange. These are drawn for sub-apertures that are not adjacent to the reference image, where the model noise is likely to be larger. Fig. 4(b) shows only the adjacent sub-aperture pairs that are cross-correlated using the ‘tiling’ method. Whilst there are still many pairs of sub-apertures that are considered to be ‘bad’, there are also many that are ‘good’. Every sub-aperture in the WFS frame can be cross-correlated using only ‘good’, blue, cross-correlations. The absolute shift of each sub-aperture can then be determined using only information contained in the cross-correlations from adjacent pairs of sub-apertures.

### 3.2 Reference image generation

Using the technique described in Section 3.1, a series of sub-aperture images, with large relative shifts, from a WFS can have their individual image shifts measured. The simplest way to synthesize a reference image from WFS images and image shift measurements is to align the individual images using the shift measurements and sum them. This has been implemented before by Basden et al. (2014), where the technique is used to increase the signal-to-noise ratio (S/N) of the reference image for LGS. However, by keeping...
Figure 5. Images of generated reference images shown beside supersized reference images. The upper images show the case for images of solar granulation and the lower images show the case for images of elongated LGSs, shown on a logarithmic scale to highlight the edges of the laser plume. The left-hand images show the full FOV observed by a single sub-aperture and the right-hand images show the full synthesized supersized reference images. The scale of the sub-aperture and supersized reference images is the same for each object, with the padding showing the areas where extra information is present in the supersized reference images.

all parts of the aligned image rather than cropping to the FOV of a sub-aperture, we can create a supersized reference image. This has the effect of reducing noise in the reference image, in a similar way to Basden et al. (2014), but also offers a solution to model error.

By using all sub-apertures in a WFS frame, a supersized reference image can be created which contains no regions that are not sampled by at least one sub-aperture image. The fill factor can be increased further if multiple frames are used together to create a supersized reference image. However, the edges of the supersized reference image can still be undersampled if there are too few sub-aperture images with large absolute shifts.

Here, to create supersized reference images, initially the sub-aperture images were up-sampled to $10 \times$ their original size, to enable alignment of the images to a sub-pixel scale. The images were then stacked, rounding the shifts to the nearest tenth of a pixel, so the shifts were all an integer number of pixels on the up-sampled sub-aperture images. All parts of the images were kept after the alignment, such that the resulting stacked image had a larger FOV than the original FOV in the sub-aperture images. Although fast Fourier transform methods exist for co-aligning images, these were not employed as they typically do not allow for a larger sized output image than input. This supersized image was then binned back down to the original scale of the WFS, generating an image similar to the input sub-aperture images, but with higher S/N and a larger FOV. Example synthesized supersized reference images from simulated solar and LGS WFS images are shown in Fig. 5. The LGS image contains elongation, which is representative of those expected to be observed at the edge of the ELT pupil.

The initial supersized reference images, which are created from using the centroids from the least squares fit described in Section 3.1, are not always sufficient to be used as reference images for cross-correlation. This is due to the accuracy of the centroid measurements, which arise from the least squares technique. However, the synthesized supersized reference image does contain a larger FOV and show the structure found in the sub-aperture images, so can be used in order to estimate the shifts of the same set of sub-apertures again, to a higher accuracy. This process can then be repeated, in a bootstrap-type method, multiple times in order to ‘refine’ the synthesized supersized reference image. After a certain number of iterations, the centroid estimates will no longer change from each iteration, so the generated supersized reference image stabilizes. This occurs when the centroids from the sub-apertures are optimal, so the synthesized reference image is also optimal for the input set of sub-aperture images. This supersized reference image can then be used as the reference image to measure the centroids in subsequent WFS frames.

Due to the distribution of shifts in Fig. 3, the edges of the supersized image are contained in relatively few of the sub-aperture images. The resulting S/N in a supersized reference image therefore varies across the supersized image. In the centre of the image, the S/N is highest and it decreases further from the centre. The resulting shift estimates by using a supersized reference image will therefore be more reliable for small shifts and less reliable for large shifts, where the edges of the supersized reference images contribute signal to the cross-correlation. This effect can be reduced by using more sub-aperture images, from different frames, to generate a supersized reference image. Though the estimates from a supersized reference image with poor S/N at the edges of the FOV will be more accurate than if there was no structure in the reference image, i.e. the reference image had a smaller FOV. This effect of differential noise properties across the supersized reference image is not investigated here, as noiseless images are used in the simulations to only show the effect of model error.

4 COMPARISON OF REFERENCE IMAGES

The technique described in Section 3 was compared with the widely used method of using a single sub-aperture image as the reference image in correlation WFSing. WFS images of solar granulation and LGSs were simulated with relative shifts representative of Von Karman atmospheric turbulence, and centroided by cross-correlating them with a single, central un-vignetted sub-aperture as the reference image in order to obtain a baseline performance for the standard method of performing correlation WFSing. The least squares method of measuring centroids, described in Section 3.1, was performed and its root mean square (rms) error measured, along with the rms error from using synthesized reference images generated from the WFS image. The synthesized reference images were used in two situations, the first where the supersized reference image was windowed to the original FOV of a single sub-aperture, comparable to the method used in Basden et al. (2014), and the second where the full FOV of the supersized reference image was used. The results for both sub-aperture images of solar granulation and highly elongated LGS images are shown in Fig. 6.

Using a single sub-aperture as the reference image works well in both the solar and LGS cases for small shifts, of up to 2 pixels (12.5 per cent shift of FOV). This is expected as the simulations were run in noiseless conditions, so where there is a large overlap of sub-aperture images with the reference image, the centroid estimate taken from using a cross-correlation has a high S/N.

The initial method for estimating the centroids for creating a supersized reference image, using the least squares method described in Section 3.1, performs better than simply using a single sub-aperture as a reference image. It can be seen in both the solar and
images, the accuracy of centroiding is not improved for the case of daytime observation compared to the least squares method, but there is a less significant improvement in centroiding accuracy for the LGS case. The difference in performance is due to the general structure typically observed for each of the different cases and is explored in more detail in Section 4.1. In addition, for noiseless simulations it is interesting that the generated reference offers better performance than using a single sub-aperture as the reference. This is due to the statistics of the image shifts, as the generated reference image will always be centred on an image shift of 0 pixel, whereas the absolute shift of a single sub-aperture can be anywhere in the distribution, skewing the relative shifts with respect to a single sub-aperture used as the reference image.

The full supersized reference image performs the best of all the techniques shown here. For small shifts the supersized reference image performs at a similar level to the other methods, and then offers a significant increase in performance for increasingly large shifts until it begins to fail at shifts with a magnitude of 7 pixels for images of solar granulation. This accuracy in centroiding measurements remains at the sub-pixel level for all magnitudes of shifts for the sub-aperture images until the shifts reach 50 per cent of the sub-aperture FOV, a much greater shift than any of the other methods are able to perform up to. For the LGS case, the supersized reference offers a much more modest increase in centroiding accuracy and is already struggling to achieve a performance required for WFSing in AO when the magnitude of shift reaches 25 per cent of the sub-aperture FOV. This discrepancy in performance between the two types of images is due to the difference in general structure contained in the images and is discussed more in the following sections.

### 4.1 Comparison of solar and laser guide star reference images

The main differences in performance between the solar granulation images and the images of an LGS shown in Fig. 6 are in the performance of the synthesized reference images. The images of solar granulation contain a continuous structure across the FOV in all directions, whereas the images of LGSs only contain structure along one dimension (the direction of elongation). This restricts the advantage of using a supersized reference image to one dimension for the LGS, making the gains of the supersized reference image better for the solar case than for the LGS case.

This differing structure also affects the relative performance from using a windowed synthesized reference image from combining multiple sub-aperture images. The windowed generated reference image is more effective for solar granulation as the structure in the sub-aperture images extends over all directions.

Another difference with WFS frames observing LGSs arises from the fact that the orientation and level of elongation seen in a sub-aperture are dependent on the exact geometry and location of the sub-aperture, which differs between sub-apertures. This can be mitigated to a certain extent by taking a time series of images from a single sub-aperture and synthesizing a reference image for every sub-aperture from a temporal set of frames from the same sub-aperture. The generated reference images would then vary across pupil for different sub-apertures. However, this assumes that the observed sodium plume is stable over the time period the data set for creating the supersized reference image as well as the length of time the synthesized reference image is the applied for. This assumption seems reasonable, with data from Pfrommer & Hickson (2010) and Michaille et al. (2001) suggesting the sodium layer is stable over...
periods of minutes, apart from occasional spikes in the profile from micro-meteorites, at a rate of ≈20 h⁻¹.

5 DISCUSSION

Overall, using a supersized reference image in a correlation WFS offers an advantage over other types of reference images, which are restricted to the FOV of a single sub-aperture image. Supersized reference images offer improved performance where shifts between sub-aperture images are large (over 12 per cent of the sub-aperture FOV). This is due to the fact that using a supersized reference image combats model error in the correlation images. In the solar case, where structure is continuous in all directions around a target FOV, the technique offers a level of performance similar to standard correlation centroiding techniques that observe small shifts, but extend the magnitude of shift, which can be reliably centroided from ∼12 per cent to ∼50 per cent of the FOV of a sub-aperture. Above this magnitude of shift a failure region is reached. This region is determined by the ability of reliable centroid estimates to be made initially, which can then be iterated upon to generate the final supersized reference image. The technique could work with a larger magnitude of shifts, if the initial estimates of centroids were improved. This technique has direct implications for existing open-loop WFS instruments, such as S-DMM* (Scharmer & van Werkhoven 2010) and Solar SLODAR (Townsend 2016).

The technique performs less well for sub-apertures observing highly elongated LGS. Previous studies have shown cross-correlation and matched filter to offer better centroid accuracy than simply centroiding the LGS plume (Basden et al. 2014, 2017). This is due to the signal being restricted to one dimension, along the direction of elongation. However, an improvement in the accuracy of centroid estimates is still observed, until, like for the solar case, a ‘catastrophic’ failure point is reached. The technique does offer a valid improvement to the accuracy of centroid estimates, achieving a sub-pixel accuracy for FOVs of up to 25 per cent of the total FOV, rather than the 12 per cent, which conventional reference images offer. This is due to the larger FOV in the reference image reducing the impact of truncation on the centroiding measurements. Generating supersized reference images also does not require any external knowledge of the sodium layer, so no external observations of the sodium plume are required.

There is a significant overhead associated with initially generating a supersized reference image as described here. The least squares method requires significant amounts of computation to generate centroids, then subsequent iterations to improve the centroid estimates for all pairs of sub-apertures with successive ‘generations’ of synthetized supersized reference images are required.

However, this process is only required to create an initial supersized reference image, so only performed once. The initial step to generate a first supersized reference image scales as the number of sub-apertures in the WFS, with the total number of correlations required scaling as O(n²) for n sub-apertures, where using a single reference image scales as O(n). Even for ELT scale LGS WFS (80 × 80 sub-apertures) a supersized reference could be generated in ∼1 s on the WFS processing hardware.

Updating a supersized reference image, because either the structure in the FOV has evolved or the conditions have changed significantly, can be performed using the images of a previous WFS frame, or temporal set of images, and the accurate centroids from the working AO system. Utilizing the output centroids from a working AO system eliminates the overhead associated with measuring centroids for generating the supersized reference image, vastly reducing the computational cost in a working system. Updating the reference image would add negligible computational overhead to the AO system, as the centroiding is already performed as part of the AO loop. Running an AO loop with a supersized reference image increases the computational cost of centroiding compared to using a single sub-aperture as a reference image. For a typical solar WFS with 16 × 16 pixels, 0.25 arcsec pixel⁻¹ in a sub-aperture in conditions with r0 = 10 cm the supersized reference image would typically be 20 × 20 pixels, an increase of 0.25×. This increase in size increases the centroiding complexity by 1.6×. However, in the full AO loop, this increase in computation takes centroiding from ∼10 per cent of the total computation time to ∼14 per cent of the total computation time, an increase of < 5 per cent.

Increasing the magnitude of tilt that a WFS can measure allows for a number of avenues to be explored. The technique could be used for closed-loop WFS design. By improving the magnitude of shift that can be measured in a given WFS, finer sampling of the WFS target could be used on a reduced FOV. This would potentially allow for more accurate centroids to be attained in closed-loop WFS, or to circumvent issues which arise from the limited number of pixels available in fast, sensitive cameras, which are required for WFSing, such as the truncation of LGS images. This is highly relevant for the case of LGS WFS for ELTs, where there is a trade-off between the number of sub-apertures in the WFS and the sampling resolution of the LGS. Using a smaller FOV in solar WFSs would also increase the sensitivity of the WFS to high-altitude turbulence.

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REFERENCES


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