A physical model of the broadband continuum of AGN and its implications for the UV/X relation and optical variability

Aya Kubota\textsuperscript{1,2,*} and Chris Done\textsuperscript{1}

\textsuperscript{1}Department of Physics, University of Durham, South Road, Durham, DH1 3LE, UK
\textsuperscript{2}Department of Electronic Information Systems, Shibaura Institute of Technology, 307 Fukasaku, Minuma-ku, Saitama-shi, Saitama 337-8570, Japan

Accepted XXX. Received YYY; in original form ZZZ.

ABSTRACT

We develop a new spectral model for the broadband spectral energy distribution (SED) of Active Galactic Nuclei (AGN). This includes an outer standard disc, an inner warm Comptonising region to produce the soft X-ray excess and a hot corona. We tie these together energetically by assuming Novikov-Thorne emissivity, and use this to define a size scale for the hard X-ray corona as equal to the radius where the remaining accretion energy down to the black hole can power the observed X-ray emission. We test this on three AGN with well defined SEDs as well as on larger samples to show that the average hard X-ray luminosity is always approximately a few percent of the Eddington luminosity across a large range of Eddington ratio. As a consequence, the radial size scale required for gravity to power the X-ray corona has to decrease with increasing Eddington fraction. For the first time we hardwire this into the spectral models, and set the hard X-ray spectral index self consistently from the ratio of the hard X-ray luminosity to intercepted seed photon luminosity from the disc. This matches the observed correlation of steeper spectral index with increasing Eddington ratio, as well as reproducing the observed tight UV/X relation of quasars. We also include the reprocessed emission produced by the hot inner flow illuminating the warm Comptonisation and standard disc regions and show that this predicts a decreasing amount of optical variability with increasing Eddington ratio as observed, though additional processes may also be required to explain the observed optical variability.

Key words: black hole physics – galaxies: Seyfert – accretion, accretion discs

1 INTRODUCTION

Active Galactic Nuclei (AGN) are powered by mass accreting onto a supermassive black hole (SMBH). The well known Shakura & Sunyaev (1973) disc model makes very simple predictions for this emission if it is emitted locally and thermalises to a blackbody. The disc temperature increases inwards (modulo a stress-free inner boundary condition at the innermost stable circular orbit, $R_{\text{ISCO}}$), so the total spectrum is the sum over all radii of these different temperature components (multi-colour disc blackbody; e.g., Mitsuda et al. 1984). However, the observed spectral energy distribution (SED) of AGN are much more complex than this predicts. There is a ubiquitous tail at X-ray energies, as well as an unexpected upturn below 1 keV, termed the ‘soft X-ray excess’.

The hard X-ray tail indicates that some part of the accretion energy is not dissipated in the optically thick disc (where it would thermalise) but is instead released in an optically thin region (e.g., Elvis et al. 1994). The resulting Comptonised spectrum from 1–100 keV indicates that this region has electron temperature $kT_e \sim 40$–100 keV and optical depth $\tau \sim 1$–2 (Lubiński et al. 2016; Fabian et al. 2015).

The origin of the ‘soft X-ray excess’ is not well understood. It can be fit by a second Comptonisation region with very different parameters from the coronal emission, one where the electrons are warm, $kT_e \sim 0.1$–1 keV and optically thick $\tau \sim 10$–25 (e.g., Magdziarz et al. 1998; Czerny et al. 2003; Gierliński & Done 2004b; Porquet et al. 2004; Petrucci et al. 2013; Middei et al. 2018). Alternatively, it could be produced by reprocessing/reflection of the coronal emission on the very inner disc, where extremely strong relativistic effects smear out the expected strong line emission from ionised material (Crummy et al. 2006). The fastest soft X-ray variability is correlated with, and lags behind, the hard X-ray variability, so some fraction of the soft X-ray excess must be produced from reprocessing/reflection of the corona flux (e.g., Fabian et al. 2013; De Marco et al. 2013). However, recent results have shown that the majority of the soft excess does not arise from reflection (Mehdipour et al. 2011, 2015; Noda et al. 2013; Matt et al. 2014;...
Boissay, Ricci, & Paltani 2016; Porquet et al. 2018), favouring the warm Comptonisation model.

The warm Comptonisation scenario also helps to explain another puzzling component of the broadband AGN SED, namely a ubiquitous downturn seen in the UV, at energies far below those expected for the peak disc temperature (e.g., Zheng et al. 1997; Davis, Woo, & Blaes 2007). A warm Comptonisation spectrum can extend across the absorption gap, connecting the UV downturn and the soft X-ray upturn with a single component (Elvis et al. 1994; Laor et al. 1997; Richards et al. 2006). This carries a dominant fraction of the luminosity in the SED of AGN at lower Eddington ratio, \( \frac{L_{\text{bol}}}{L_{\text{Edd}}} \) (Jin et al. 2012a,b), again arguing against a purely reprocessing/reflection origin for the soft X-ray excess, though some contribution could be present (e.g., Lawrence 2012). The SED of high \( \frac{L_{\text{bol}}}{L_{\text{Edd}}} \) are instead dominated by disk emission, which can extend into the soft X-ray bandpass for the lowest mass, Narrow Line Seyfert-1 (NLS1) galaxies, but these still have a small fraction of their bolometric power emitted in a soft X-ray excess component (Jin et al. 2012a,b; Done et al. 2012; Jin et al. 2013; Matzeu et al. 2017).

Neither of the Comptonisation components are well understood. However the warm Comptonisation region is especially problematic as, unlike the hot corona, it does not have a clear counterpart in the much lower mass black hole binary systems (BHB). These often show spectra at \( \frac{L_{\text{bol}}}{L_{\text{Edd}}} \approx 0.1-0.2 \) which are dominated by the thermal accretion disc emission, with only a small tail to higher energies from a hot Comptonising corona (e.g., Kubota, Makishima, & Ebisawa 2001; Gierlinski & Done 2004a; Steiner et al. 2009).

One obvious break in scaling between BHB and AGN is that the SMBHs have discs which peak in the UV rather than X-ray temperature range. The UV is a region in which atomic physics is extremely important whereas plasma physics dominates in BHB. Nonetheless, the best models of the accretion disc structure including UV opacities (Hubeny et al. 2001) find that the spectra are fairly well described by a sum of modified blackbody components (with atomic features superimposed), similar to BHB spectra (Davis & Hubeny 2006). The addition of UV opacity within the disc alone then may not be enough to explain the soft X-ray excess (though it does also depend on the heating profile within the disc): instead it may be connected to the ability of UV line opacity to launch winds from AGN discs (e.g., Proga, Stone, & Kallman 2000; Laor & Davis 2011) and/or the huge change in opacity connected to Hydrogen ionisation at close to Hydrogen ionisation at \( \sim 10^4 \) K. There are few free electrons below this temperature, so electron scattering is not important, but the dissipation mechanism is only blackbody for radii \( R > R_{\text{corona}} \). Inwards of this, they assumed that the flow instead emits the accretion energy as a warm or hot Comptonisation component. These energy conserving models (optXagnF: D12) give an additional physical constraint on the components, and more importantly, highlight the fundamental parameters of mass and mass accretion rate (for any assumed spin) in setting the overall SED (Jin et al. 2012a,b; Ezikode et al. 2017). These models reveal a systematic change in the SED which can be modeled by a decrease in \( R_{\text{corona}}/R_g \) (where \( R_g = GM/c^2 \)) correlated with a increase in the hot Comptonisation power law spectral index as \( \frac{L_{\text{bol}}}{L_{\text{Edd}}} \) increases (Jin et al. 2012a,b; Ezikode et al. 2017; see also Shemmer et al. 2006, 2008 and Vasudevan & Fabian 2007, 2009 for the hard X-ray spectral index).

In this paper, we develop a new model which addresses the underlying physics of these changes, where we assume that the flow is completely radially stratified, emitting as a standard disc blackbody from \( R_{\text{out}} \) to \( R_{\text{warm}} \), as warm Comptonisation from \( R_{\text{warm}} \) to \( R_{\text{hot}} \) and then makes a transition to the hard X-ray emitting hot Comptonisation component from \( R_{\text{hot}} \) to \( R_{\text{ISCO}} \). The warm Comptonisation component is optically thick, so we associate this with material in the disc. Nonetheless, the energy does not thermalise to even a modified blackbody, perhaps indicating that significant dissipation takes place within the vertical structure of the disc, rather than being predominantly released in the midplane (e.g., Davis et al. 2005). At a radius below \( R_{\text{hot}} \), the energy is emitted in the hot Comptonisation component. This has much lower optical depth, so it is not the disc itself. It could either be a corona above the inner disc, or the disc could truncate, so that the hot material fills the inner region close to the black hole. We show that the observed steepening of the 2–10 keV spectral index with increasing \( \frac{L_{\text{bol}}}{L_{\text{Edd}}} \) can be most easily explained with a true truncation.

We describe the model structure in section 2, and apply it to observed broadband spectra of individual AGN in section 3. We use these data to set some of the model parameters, so that we can predict the entire AGN SED as a function of only mass and mass accretion rate (for a given black hole spin) in section 4. In section 5, we show that these models reproduce the observed tight relationship between the UV and X-ray emission in Quasars (Lusso & Risaliti 2017) as well as predict a decrease in the fraction of reprocessed optical variability with increasing \( \frac{L_{\text{bol}}}{L_{\text{Edd}}} \) as observed. Thus, this AGN SED model succeeds in describing multiple disparate observational trends, which gives confidence that the assumed geometry captures most major aspects of the source behaviour.

## 2 OVERALL DISC MODEL

We follow D12 and assume a radial emissivity like Novikov-Thorne (hereafter NT), defining the flux per unit area at a radius \( R \) on the disc as \( F_{\text{NT}}(R) = \sigma T_{\text{e}}^4(R) \), where \( \sigma T_{\text{e}}^4(R) \) is the effective temperature at this radius. Converting to dimensionless units, with \( \rho = R/R_g \), \( \eta = M/M_{\text{Edd}} \) and \( \rho_{\text{Edd}} = \eta M_{\text{Edd}}^{-1/2} \) gives \( F_{\text{NT}} \propto (\eta/M)\rho^{-3} \) for \( \rho >> 6 \). Here \( \eta \) is a spin dependent efficiency factor, assumed fixed at 0.057 for a non-spinning black hole throughout this paper.

### 2.1 Standard Disc and warm Comptonisation region

In the standard disc region we assume that the NT emission thermalises locally either to give a blackbody \( B_{\nu}(T_{\text{e}}) \) at the local blackbody temperature, defined from \( F_{\text{NT}}(R) = \sigma T_{\text{e}}^4(R) \), or that electron scattering within the disc distorts this into a modified disc blackbody spectrum. This can be approximated as a colour temperature corrected blackbody, \( B_{\nu}(\eta T_{\text{e}}^4/R_g^4) \), where \( \eta T_{\text{e}}^4/R_g^4 \) depends on the importance of electron scattering compared to true absorption processes, which itself depends on disc temperature, especially close to Hydrogen ionisation at \( \sim 10^4 \) K. There are few free electrons below this temperature, so electron scattering is not important, and \( f_{\text{col}} \) changes close to 1, whereas above this temperature there are multiple free electrons so \( f_{\text{col}} > 1 \). This effectively shifts the peak of the blackbody over by a factor \( f_{\text{col}} \), and reduces its norm by a factor \( f_{\text{col}}^{-1} \).
so this gives a shift to higher energy and decrease in normalisation in the disc spectra from each annulus which onsets at around the hydrogen ionisation energy. Thus the standard disc with this colour correction transition always has less UV emission (shortwards of $\sim 10^{15} \text{ Hz} \approx 2000\text{A}$) than predicted from simple models with $f_{\text{col}} = 1$ (D12). Figure 1 shows a comparison of the standard disc (geometry I) with $f_{\text{col}} = 1$ (red solid) to that where $f_{\text{col}}(T_{\text{NT}})$ is derived from an analytic treatment of the vertical structure of the disc (dashed red line, see also Davis & Hubeny 2006, D12). This clearly shows how the outer disc emission is identical, while the inner disc emission is shifted to higher temperatures/lower luminosities.

Concerning the warm Comptonising region, the UV data do indeed show a downturn, but this is stronger than predicted by the effect of a changing $f_{\text{col}}$ in general. Davis, Woo, & blues (2007) show that the observed AGN spectra have redder UV slopes than predicted from disc models even including electron scattering. Instead, what is required to fit this UV downturn is that the emission is much more strongly distorted from a blackbody than predicted in the standard disc. While this could be modeled by a larger colour temperature correction, a shifted blackbody becomes a progressively poorer approximation for the spectrum as $f_{\text{col}}$ increases. Hence we replace $f_{\text{col}}$ with a fully Comptonised shape and do not include this factor in our new code as the disc vertical structure is clearly very different to that of Shakura & Sunyaev (1973). Comptonisation also gives the possibility to connect the observed downturn in the UV to an upturn seen in the soft X-ray spectra, forming a single component spanning the unobservable EUV range (D12, Mehdipour et al. 2011, 2015). This warm Comptonising emission could be produced if some fraction of the dissipation takes place higher up in the disc, rather than being concentrated towards the equatorial plane (Czerny et al. 2003; Różańska et al. 2015). Residual emission in the denser disc material on the midplane can then act as a source of seed photons, together with the reprocessed emission from illumination from the upper layers of the disc (Petrucci et al. 2017).

Figure 14 in Davis et al. (2005) shows the predicted (colour temperature corrected) blackbody spectrum of a disc annulus where the vertical dissipation goes with density as in standard disc models, compared to one where the dissipation is arbitrarily changed so that 40% of the power is released in the photosphere (Fig. 16 of Davis et al. 2005). The spectrum is strongly Comptonised into a steep tail to higher energies, but clearly contains the imprint of the seed photons as a downturn at low energies. This seed photon temperature is determined both by the intrinsic dissipation in the lower layers of the disc (the remaining 60% of the accretion power in this specific example), and the thermalised flux resulting from irradiation by the Comptonising upper layers. Both these physical processes give seed photons which are close to the surface temperature predicted by the standard disc dissipation, so the seed photon temperature imprinted onto the steep Comptonised emission is itself close to this temperature (Fig. 14 of Davis et al. 2005).

Thus the expectation is that the seed photon energy should change with radius in the same way as the expected standard disc temperature. D12 discuss this in their Appendix, but make the simplifying assumption in optxagn that this can be approximated as a single Comptonisation spectrum with seed photon temperature set by the maximum temperature of the standard disc emission i.e. $kT_{\text{seed}} = kT_{\text{NT}}(R_{\text{corona}})$. This is adequate if the low energy part of this component is mostly unobservable due to interstellar absorption. However, there are now data where this region of the spectrum can be seen, motivating a more careful approach. Also, the optxagn approximation always requires that there is an outer standard disc in order to provide the code with a temperature for the seed photons. This need not be the case in the physical situation envisaged. The warm Comptonisation region could instead cover the entire outer disc as its seed photons are from deeper layers of the underlying disc rather than from an external source.

Petrucci et al. (2017) tested a model where the entire optical/UV/soft X-ray flux is from a warm Comptonisation region with a slab geometry over the disc. They show that reprocessing in this geometry hardwires the Compton amplification factor $A$ to

$$L_{\text{tot}} = A L_{\text{seed}} = L_{\text{seed}} + L_{\text{diss,warm}}$$

where, $L_{\text{tot}}$, $L_{\text{seed}}$ and $L_{\text{diss,warm}}$ are the total luminosity, seed photon luminosity underneath the Comptonising skin and power dissipated in the warm corona, respectively. Their eq.(19) with the slab corona entirely covering the disc and large optical depth with complete thermalisation, gives

$$\frac{L_{\text{diss,warm}}}{L_{\text{seed}}} = A - 1 = 2 \left(1 - \frac{L_{\text{diss,disc}}}{L_{\text{seed,tot}}}\right) - 1$$

where $L_{\text{diss,disc}}$ is the intrinsic dissipation which thermalises in the disc. If there is no intrinsic dissipation (‘passive disc’ on the midplane: Petrucci et al. 2017, 2013) then all these seed photons are set by thermalisation of the warm Compton as $L_{\text{diss,disc}} = 0$. Thus

$$\frac{L_{\text{diss,warm}}}{L_{\text{seed}}} = 1$$

hence $L_{\text{seed}} = L_{\text{tot}}/2$. This is emitted from the same surface area as the standard disc, so this hardwires the seed photon temperature $T_{\text{seed}} \approx T_{\text{NT}}$.  

Figure 1. Comparison of spectra for a black hole of $M = 10^8 M_\odot$ with $n_\text{h} = 0.05$. Geometry I shows the Novikov-Thorne disc extending down to $R_{\text{ISCO}}$ without (red solid) and with (red dashed) color-temperature correction. Geometry II shows an outer Novikov-Thorne disc plus a warm Comptonisation region from $r = 40$ down to $R_{\text{ISCO}}$. The green solid line shows AGNSED model used in this paper (see section 2.3) where seed photons are from the underlying cool material in the midplane compared to the optxagn assumption of seed photons from the inner edge of the standard disc (green dashed). Geometry III is complete coverage of the warm Comptonising region.
Petrucci et al. (2017) showed that $A = 2$ is equivalent to a photon index of the warm component, $\Gamma_{\text{warm}} = 2.5$, which generally gave a good fit to the observed soft X-ray excess component when combined with a Comptonising electron temperature $kT_{e,\text{warm}} \sim 0.2$ keV to give the observed rollover in soft X-rays. Based on this passive disc picture, our new model, calculates the Compton emission at each annulus of radius $R$ and width $\Delta R$ in the soft compton region, using the ntheta-comp model (Zdziarski, Johnson, & Magdziarz 1996; Życki, Done, & Smith 1999) in xspec. We set the seed photon temperature to the local disc temperature $T_{\text{disc}}(R)$, and set the local luminosity to $\sigma T_{\text{disc}}^4(R) \cdot 2\pi R \Delta R \cdot 2$, and sum over all annuli which produce the warm Comptonisation. Both photon index and electron temperature are free parameters, assumed to be the same for all the disc annuli which produce the warm Comptonisation.

The green solid line in Fig.1 shows our new version of the warm Comptonisation, summed over all radii from $r_{\text{warm}} = 40 < r_{\text{out}}$ to $r_{\text{ISCO}} = 6$ as in geometry II of Fig.1. We compare this to the optr-aGNF model for the same parameters (green dashed line), showing the difference in behaviour around the seed photon energy (see also Fig. A1b in D12). The blue line in Fig.1 corresponds instead to the geometry of Petrucci et al. (2017) sketched as geometry III in Fig.1, i.e. where there is no outer disc so $r_{\text{warm}} = r_{\text{out}}$. The most noticeable effect is that the normalisation of the SED in the optical/UV is reduced. This is important, as it changes the otherwise quite robust relation between the luminosity in some band on the one hand, and the flux at some energies on the other. This is important, as it changes the otherwise quite robust relation between the luminosity in some band on the one hand, and the flux at some energies on the other. This is important, as it changes the otherwise quite robust relation between the luminosity in some band on the one hand, and the flux at some energies on the other.

We note here that unlike Petrucci et al. (2017), our new model does not require the seed photons to be present in the cold disc at all radii, only that they are present in the inner parts of the disc. This is important, as it changes the otherwise quite robust relation between the luminosity in some band on the one hand, and the flux at some energies on the other. This is important, as it changes the otherwise quite robust relation between the luminosity in some band on the one hand, and the flux at some energies on the other.

2.2 Hot Comptonisation region

There is also an additional X-ray component which dominates over the soft X-ray excess beyond 1–2 keV, extending up to $kT_{e} \sim 40–100$ keV, with $\tau \sim 1–2$ (Fabian et al. 2013; Lubiński et al. 2016; Petrucci et al. 2017). The low optical depth clearly distinguishes this component from the disc material, and the warm Compton region, so it needs to arise in a different structure. This could either be a corona above a disc, with some fraction of the accretion energy dissipated in this optically thin material, or the optically thick disc could truncate, leaving a true hole in the inner disc. For $m \lesssim 0.2$, the hard X-ray photon spectral index is usually $\lesssim 1.9$, i.e. it is flatter than expected even in the limit where all the accretion energy is emitted in the corona. Reprocessing and thermalisation of the (assumed isotropic) illuminating flux even by a completely cold, passive disc, sets a lower limit on $\Gamma_{\text{hot}} \sim 1.9$ (Haardt & Maraschi 1991; Stern et al. 1995; Malzac, Dunmort, & Mouche 2005). Hence we assume that the disc truly truncates at $r_{\text{hot}}$ for low $m$, as is supported by the lack of strong reflection and lack of strong relativistic smearing these AGN (Matt et al. 2014; Yaqoob et al. 2016; Porquet et al. 2018).

In a truncated disc geometry, the seed photons seen by the hot flow are predominantly from the inner edge of the warm Comptonisation region, so these have typical seed photon energy of $T_{\text{NT}}(R_{\text{hot}}) \cdot \exp(y_{\text{warm}})$, where $y_{\text{warm}} = 4\pi^2 kT_{e,\text{warm}}/m_e c^2$ is the Compton y-parameter for the warm comptonising corona. We use the xspec model nthcomp to describe this, with total power

$$L_{\text{hot}} = L_{\text{diss,hot}} + L_{\text{seed}}$$

Here, the inner flow luminosity, $L_{\text{hot}}$, is the sum of the dissipated energy from the flow, $L_{\text{diss,hot}}$, and the seed photon luminosity which is intercepted by the flow, $L_{\text{seed}}$.

This gives $L_{\text{diss,hot}}$ as

$$L_{\text{diss,hot}} = 2 \int_{R_{\text{ISCO}}}^{R_{\text{hot}}} \sigma T_{\text{NT}}^4(R) \cdot 2\pi R dR$$

with the truncated radius $R_{\text{hot}}$. This is shown geometrically in Fig.2a. Since the X-ray emission is not very optically thick we assume it is isotropic, unlike the disc/warm comptonisation region where we assumed a disc geometry. $L_{\text{seed}}$ is the intercepted soft luminosity from both the warm Comptonisation region and the outer disk. This can be calculated assuming a truncated disc/spherical hot flow geometry (Fig.2a, i.e. a flow scale height $H \sim R_{\text{hot}}$) as

$$L_{\text{seed}} = 2 \int_{R_{\text{hot}}}^{R_{\text{out}}} (F_{\text{NT}}(R) + F_{\text{rep}}(R)) \frac{\Theta(R)}{\pi} 2\pi R dR$$

$$\Theta(R) = \frac{1}{2} \sin 2\theta_0$$

For $R > R_{\text{hot}}$, with $\sin \theta_0 = H/R$, and $F_{\text{NT}}(R) + F_{\text{rep}}(R)$ is the flux from the warm Comptonised and/or outer disc including reprocessing (discussed in the following section).

We caution that there can be many other factors which influence $L_{\text{seed}}$, e.g. overlap of the disc and hot flow (Zdziarski, Lubiński, & Smith 1999) and/or any radial/vertical gradient in the structure of the hot flow. Nonetheless, we start from the simplest possible assumption which is a spherical, homogeneous source with $H = R_{\text{hot}}$ but we leave $H$ as a parameter in the following equations so that it can be used as a tuning parameter for alternative geometries by changing the seed photons intercepted by the source. Smaller $H$ gives a smaller solid angle, so fewer seed photons and harder spectral indices, but has no effect on $R_{\text{hot}}$ as this is set by the energetics.

2.3 Modeling reprocessing

The assumed geometry shown in Fig. 2a has some fraction of the hot Comptonisation illuminating the warm Comptonisation and cool outer disc regions. We include this self consistently, so that the radiating flux increases the local flux above that given by the intrinsic $M$. Though our geometry assumes that the hot corona is an extended source, with $H \sim R_{\text{hot}}$ as above (see Fig. 2a), Gardner & Done (2017) show that illumination from an extended source can be well approximated by a point source at height $H$ on the spin axis (lamppost: Fig. 2b). We thus utilized the lamppost geometry for the hot inner flow to calculate the reprocessed flux as it is simpler than integrating over an extended source.

The reprocessed flux for a flat disc at a radius $R$ is then written as

$$F_{\text{rep}}(R) = \frac{1}{4\pi R^2} \frac{H}{\sqrt{R^2 + H^2}} \left[1 - a \right]$$

$$a = \frac{3\Gamma_{\text{IN}} M \dot{M} L_{\text{hot}}}{8\pi R^3} \frac{H}{\sqrt{R^2 + H^2}}$$

$$\frac{1}{2} \left[ 1 + \left( \frac{H}{R} \right)^{3/2} \right]$$

$$MNRAS 000, 1–16 (2018)$$
The geometry for hard X-ray reprocessing is given by $R(>R_{\text{out}}) = \sigma T_{\text{eff}}(R)^3 = F_{\text{NT}}(R) + F_{\text{rep}}(R)$. Both $F_{\text{NT}}(R)$ and $F_{\text{rep}}(R)$ depend on radius as $R^{-3}$ for $R \gg R_g$, thus the effect of the reprocessing is basically to increase the flux across both the standard and warm Comptonisation disc by the same factor which is of order $1 + H/6R_g$. Hence a larger X-ray source increases the fraction of X-ray power which illuminates the disc, as well as increasing the fraction of bolometric power which is dissipated in the X-ray region via the change in $R_{\text{hot}} = H$.

Figure 3 shows a comparison of example spectra with (solid) and without (dashed) reprocessing for a black hole of $10^8 M_\odot$ with $m = 0.05$ (blue) and 0.5 (red). We set $L_{\text{disc,hot}} = 0.02 L_{\text{Edd}}$ and $kT_{\text{e,hot}} = 100 \text{ keV}$ for both, which implies $r_{\text{hot}} = 23$ and 9 for $m = 0.05$ and 0.5, respectively. $T_{\text{hot}}$ is set to be 1.8 and 2.2 for $m = 0.05$ and 0.5, respectively. We also include a warm Comptonisation region with $kT_{\text{e,warm}} = 0.2 \text{ keV}$ and $\Gamma_{\text{warm}} = 2.5$. Figure 3a shows models where the warm Comptonisation region extends from $r_{\text{hot}}$ to $r_{\text{warm}} = 2r_{\text{hot}}$, so that there is a standard outer disc region from $r_{\text{warm}}$ to $r_{\text{out}}$, while Fig. 3b shows the alternative geometry where the warm Comptonisation extends over the entire outer disc, i.e. $r_{\text{warm}} = r_{\text{out}}$.

The lower panels of Fig. 3a and b highlight the effect of reprocessing by showing the ratio of the spectra including reprocessing to the intrinsic emission. Reprocessing makes a larger fraction of the optical emission for the lower $m$, as here the ratio of the X-ray flux to optical disc emission is much larger, and the larger size scale of the X-ray source means that a larger fraction of the X-ray emission is intercepted by the disc. The difference is most marked around the maximum in the SED as the flux increase from reprocessing is enhanced by the associated temperature increase in disc or seed photon energy.

We call this new model AGNSED, and in the appendix define all the parameters. The model is publicly available for use in the xspec spectral fitting package. We also release a simplified model qsoSED where many of the parameters are fixed. This is more suitable for fitting fainter objects such as distant quasars, where the signal to noise is limited.

3 APPLICATION TO OBSERVED SPECTRA

We apply AGNSED to a small sample of AGN, spanning a wide range of $m$, chosen to have good multi-wavelength data. We select NGC 5548 ($m \sim 0.03$; Mehdiipur et al. 2015) and Mrk 509 ($m \sim 0.1$; Mehdiipur et al. 2011), for which big multiwavelength observation campaigns have been performed. Based on the long-term observations with the Reflection Grating Spectrometers (RGS) on board XMM-Newton, their intrinsic absorption were...
extremely well determined (Mehdipour et al. 2015; Detmers et al. 2011; Mehdipour et al. 2011) and removed from the SEDs. In this paper, we fit the best estimate of the continuum spectra from these AGN, deconvolved from the instrument response, and corrected for reddening and absorption. We read the resulting flux files into xspec using the rlx2xspec command. These deconvolved data were kindly provided by M. Mehdipour. In order to apply the model to higher energies, we fit all three SED with flx2xsp using the reddening and absorption. We read the resulting flux files into xspec command. These deconvolved data were kindly provided by M. Mehdipour. In order to apply the model to higher AGN emission. The resulting optical/UV continuum is rather blue, so we fit this by a single, warm Comptonisation region, using blackbody and cannot easily be fit with any disc blackbody based model, either AGN emission. The resulting optical/UV continuum is rather blue, so we ignore the V and I band continuum points in the fit. The X-ray emission is extremely bright compared to the optical/UV, and very hard.

We then fit the data with agnsed, including three emission regions. There is a clear iron line in the X-ray data, but the accompanying Compton hump is rather weak (Ursini et al. 2015; Cappi et al. 2016) so this line probably originates in optically thin material in the BLR (Yaqoob et al. 2001; Brenneman et al. 2012; Ursini et al. 2015). We model this simply by including a gaussian in the fit. The model overpredicts the optical data for $r_{out} = r_{sg}$ for $m_i \sim 0.03$. This could again indicate a slight oversubtraction of the host galaxy from our data, but we are able to fit by allowing the outer disc radius to be a free parameter, giving $r_{out} = 280$. The overall continuum shape and luminosity is then fairly well reproduced by agnsed with $M = 5.5 \times 10^7 M_\odot$ and $m_i = 0.03$. The best fit parameters are shown in table 2, and the best fit model is overlaid on the deconvolved data points in Fig. 4a. The estimated $\Gamma_{warm}$ of 2.28 is harder than the passive disc prediction of 2.5 and may indicate patchy corona as suggested by Petrucci et al. (2017). We discuss this in more detail in Section 4.3.

We also try to reproduce the data without any standard outer disc component, as in Mehdipour et al. (2015) and Petrucci et al. (2017). However, in our fit the seed photon energy is not a free parameter, but is set at the underlying disc temperature from reprocessing. The UV data are clearly in tension with this, as they show a stronger downturn than predicted by the warm Comptonisation models with seed photon energy set by the underlying disc area from reprocessing. A warm Comptonisation region covering the outer disc also changes some other aspects of the fit. The lower normalisation in the optical/UV (see Fig. 2, geometry III) means that the same parameters of mass and accretion rate underpredicts the optical data. Including the warm layer across all of the disc means that there should be an increase in $(M M)^{1/3}$ to compensate for the decrease in normalisation from Comptonisation. However, the observed bolometric luminosity $L_{bol} = \eta \dot{M} c^2$ which is fairly well constrained by the data. Hence the only possibility to increase the optical emission is to increase the mass. This now peaks at the upper limit, giving a slight decrease in $m_i \propto M/M$. The outer radius is now not constrained from the data, with little change in goodness of fit from $r_{out} = 10^8$ to $10^9$ so we set this back to the self gravity radius. We show the best fit with these assumptions in Fig. 4b, and tabulate the parameters in table 2.

In order to explain the optical data points which peak energy at 8–10 eV with entire warm Comptonisation, blackhole mass needs to be as large as $1 \times 10^8 M_\odot$ with $m_i \sim 0.01$ and $L_{bol, warm} \sim 0.01 L_{Edd}$. This clearly exceeds the reasonable range of blackhole mass of NGC 5548. Hence we conclude there is most likely a standard outer disc in NGC 5548.

### 3.1 NGC 5548: $m_i \sim 0.03$

The Seyfert-1 galaxy NGC 5548 is one of the most widely studied nearby AGN, with well constrained mass $(2–6) \times 10^7 M_\odot$. There was a multi-wavelength campaign on this object in 2012–2014 (e.g., Kaastra et al. 2014), and the broadband spectra were analyzed by Mehdipour et al. (2015). We use the data from summer 2013 shown in Fig. 10 of Mehdipour et al. (2015), which includes data points from NuSTAR, INTEGRAL, RGS and the European Photon Imaging Camera (EPIC-pn) on XMM-Newton, the Cosmic Origins Spectrograph (COS) on the Hubble Space Telescope (HST), the UltraViolet and Optical Telescope (UVOT) on Swift, and from two ground-based optical observatories: the Wise Observatory (WO) and the Observatorio Cerro Armazones (OCA). During this campaign, there are multiple absorption systems seen in the X-ray (Mehdipour et al. 2015; Kaastra et al. 2014; Cappi et al. 2016), which have been removed from our data using the best fit modelling of the RGS spectra (Mehdipour et al. 2015). Nonetheless, there is some uncertainty associated with this, which affects the determination of the intrinsic soft X-ray spectrum.

There is also strong host galaxy contamination in the optical, so this was removed (Mehdipour et al. 2015, Fig. 10) to isolate the AGN emission. The resulting optical/UV continuum is rather blue, and cannot easily be fit with any disc blackbody based model, either a standard disc or warm Comptonised one. Mehdipour et al. (2015) fit this by a single, warm Comptonisation region, using blackbody (not disc blackbody) seed photons in order to get such a steeply rising optical/UV continuum. It seems more likely that this is a consequence of a slight oversubtraction of the host galaxy, so we ignore the V and I band continuum points in the fit. The X-ray emission is extremely bright compared to the optical/UV, and very hard.

<table>
<thead>
<tr>
<th>System</th>
<th>$m_i$</th>
<th>$z$</th>
<th>$D$ (Mpc)</th>
<th>$D_L$ (Mpc)</th>
<th>$M (10^7 M_\odot)$</th>
<th>$r_{out}$</th>
<th>$r_{sg}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NGC 5548</td>
<td>0.03</td>
<td>0.03175</td>
<td>0.034397</td>
<td>0.154338</td>
<td>2–6</td>
<td>10–30</td>
<td>4.6–14</td>
</tr>
<tr>
<td>Mrk 509</td>
<td>0.03</td>
<td>0.03175</td>
<td>0.034397</td>
<td>0.154338</td>
<td>2–6</td>
<td>10–30</td>
<td>4.6–14</td>
</tr>
<tr>
<td>PG 1115 + 407</td>
<td>0.03</td>
<td>0.03175</td>
<td>0.034397</td>
<td>0.154338</td>
<td>2–6</td>
<td>10–30</td>
<td>4.6–14</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Reference</th>
<th>$m_i$</th>
<th>$z$</th>
<th>$D$ (Mpc)</th>
<th>$D_L$ (Mpc)</th>
<th>$M (10^7 M_\odot)$</th>
<th>$r_{out}$</th>
<th>$r_{sg}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2013</td>
<td>0.03</td>
<td>0.03175</td>
<td>0.034397</td>
<td>0.154338</td>
<td>2–6</td>
<td>10–30</td>
<td>4.6–14</td>
</tr>
<tr>
<td>2009</td>
<td>0.03</td>
<td>0.03175</td>
<td>0.034397</td>
<td>0.154338</td>
<td>2–6</td>
<td>10–30</td>
<td>4.6–14</td>
</tr>
<tr>
<td>2002</td>
<td>0.03</td>
<td>0.03175</td>
<td>0.034397</td>
<td>0.154338</td>
<td>2–6</td>
<td>10–30</td>
<td>4.6–14</td>
</tr>
</tbody>
</table>


3.2 Mrk 509: $m_i \sim 0.1$

Mrk 509 is the nearby Seyfert-1/quasar, and is one of the first objects in which the soft X-ray excess was discovered (Singh, Garmire, & Nousek 1985). There was a large multi-wavelength campaign on this object (Kaastra et al. 2011a,b), with simultaneous optical-UV and X-ray monitoring from XMM-Newton’s OM and EPIC-pn together with the HST/COS and archival observation by the Far Ultraviolet Spectroscopic Explorer (FUSE) (Mehdipour et al. 2011). As in Mehdipour et al. (2015), they fit the continuum SED without any outer disc emission, just using a warm
(0.2 keV) optically thick ($\tau \sim 17$) Comptonisation component with free seed photon temperature, together with a hard ($\Gamma \sim 1.9$) power-law X-ray continuum.

There is a clear iron line in the X-ray spectrum, together with a Compton hump, so we include this in the model using $\text{gsMOOTH*TBABS}$ ($\text{Nandra et al. 2007}$). The best fit model is shown in Fig. 3c and detailed in Table 2. The data are then well fit with our three component $\text{AGNSED}$ continuum (i.e. including an outer disc) for a black hole mass of $1 \times 10^7 M_\odot$ with $m = 0.1$. The transition radius from the outer disc to warm Comptonised disc is around $r_{\text{warm}} = 40$, while the observed X-ray emission requires $r_{\text{out}} = 21$.

We also try a fit where the entire outer disc is covered by the warm Comptonisation (Fig. 4d). This is statistically worse than the model with an outer standard disc, but unlike NGC 5548, the data match fairly well to the model around the UV peak. This model also gives $r_{\text{warm}} = 2.6$, consistent with a passive disc.

### 3.3 PG 1115+407: $m \sim 0.4$

PG 1115+407 is a NLS1 galaxy with mass from single epoch spectra of $4.6 \times 10^7 M_\odot$ using historical data with FWHM $H \beta$ of 1720 km/s ($\text{Porquet et al. 2004}$), or $9.1 \times 10^7 M_\odot$ with the (narrow line subtracted) Sloan Digital Sky Survey (SDSS) FWHM $H \beta$ of 2310 km/s ($\text{Jin et al. 2012a}$). Hence we assumed a black hole mass range of $(0.46-1.4) \times 10^7 M_\odot$, including 0.2 dex uncertainty on the SDSS limit (Table 1). We re-analyzed the same data set shown in $\text{Jin et al. (2012a,b)}$, by concentrating on XMM/OM and XMM/EPIC-pn data alone since the SDSS data points were not simultaneous with the XMM observation We fit the data with $\text{TBABS*REDDEN*AGNSED}$, where $\text{TBABS}$ is used with $\text{Anders & Ebihara (1982) abundance and E(B – V) is tied to N_H \cdot (1.7 \times 10^{-22}) as was done in Jin et al. (2012a).}$ The observation is only 9.4ks, and the spectrum is steep. This makes it difficult to constrain any reflection component so this is not included in the model.

As shown in Table 2, the model with an outer disc fits the data well, and $N_H$ of $2.2 \times 10^{20} \text{cm}^{-2}$ is consistent with galactic absorption of $(1.5-1.9) \times 10^{20} \text{cm}^{-2}$ ($\text{Kalberla et al. 2005; Dickey \\& Lockman 1990}$). The unsorbed SED derived from this best fit model is shown in Fig. 4e. Black hole mass is estimated as $M = 1.0 \times 10^7 M_\odot$ with $m = 0.4$. The size of the hot corona is $r_{\text{out}} = 9.8$, which is much smaller than for the lower $m$ AGN. For the warm Comptonising region, while $r_{\text{warm}}$ is similar to that of Mrk 509, $\Gamma_{\text{warm}}$ is much steeper at $\sim 3.1$. This most likely indicates that there is some intrinsic disc power dissipated underneath the warm corona rather than a completely passive disc. We compare this to models where the entire disc is dominated by the warm Compton component. The fit results are shown in Table 2 and Fig. 4f. The fit is slightly worse in terms of $\chi^2$, and has slightly larger absorption at $N_H = 3.1 \times 10^{20} \text{cm}^{-2}$.

### 4 FULL AGN BROADBAND SPECTRAL MODEL

In this section, we evaluate the results of fitting $\text{AGNSED}$ to the observed SED of NGC 5548 ($m \sim 0.03$), Mrk 509 ($m \sim 0.1$), and PG 1115 + 407 ($m \sim 0.4$), and use these, together with other results in the literature, to build a full SED picture where the only free parameters are $M$ and $m$.

### 4.1 Existence of an outer standard disc component

All the AGN in section 3 are consistent with $\text{AGNSED}$ of three components, where there is an outer disc, together with warm Comptonising region and hot corona, powered by NT emissivity for a low spin black hole. This is always a better fit than assuming $r_{\text{warm}} = r_{\text{out}}$, i.e., a model where the warm Comptonisation region extends over the entire outer disc, although there are several uncertainties, e.g., on the inclination and absorption corrections. Our model is different to that fit by $\text{Mehdipour et al. (2015) and Petrucci et al. (2017),}$ where the optical/UV data are from the warm Comptonisation component alone. This difference is due to our assumption that the warm Comptonisation is intrinsically linked to a NT disc. The data do fit just as well to an unconstrained warm Comptonisation model as this...
has the same optical/UV shape as a standard disc (see Fig.1 geometry III). However, we have additional requirements on the luminosity and seed photon temperature from our assumed NT emissivity. The optically thick, warm Comptonisation thus suppresses the flux below that predicted by the outer disc, so these models require a higher $M$ and/or higher absolute mass accretion rate, $\dot{m}$, but the latter is fairly well constrained by the observed bolometric luminosity from the broadband spectra.

A larger $M$ through the outer disc could fit the data if this is counteracted by strong energy losses, e.g., if the system powers a UV line driven wind (Laor & Davis 2014). However, it seems somewhat fine tuned that these wind losses (which vary with $M$ and $\dot{m}$) would be always able to almost exactly compensate for the extra power predicted by NT emissivity which assumes a constant $M$ with radius. Similarly, high black hole spin would give higher luminosity for a given $M$ through the outer disc, which can overpredict the total luminosity unless this is mainly dissipated in the unobservable EUV bandpass. Again, this seems fine tuned. The simplest solution is that we are seeing evidence for an outer disc whose properties are somewhat fine tuned that these wind losses (which vary with $r$) is that we are seeing evidence for an outer disc whose properties are not fully consistent with a truncated disc geometry. However, it seems counteracted by strong energy losses, e.g., if the system powers a UV line driven wind (Laor & Davis 2014).

### 4.2 Hot coronal emission

As shown in table 2, the observed power dissipated in the hot inner flow is $L_{\text{diss,hot}} = 0.02-0.04L_{\text{Edd}}$ in our three AGN with different $\dot{m}$. This is also seen in the sample of 50 AGN in Jin et al. (2012a). These have different masses and $\dot{m}$, but the X-ray luminosities are all the same within a factor 2–3 when the SEDs are stacked into three groups of low, medium and high $\dot{m}$ and referenced to the same black hole mass (Fig. 8b in D12).

#### 4.2.1 truncated disc and inner hot flow geometry

In our model, the approximately fixed value for $L_{\text{diss,hot}}$ measured from the data then determines $\dot{m}_{\text{hot}}$ from the NT emissivity. For a total $\dot{m} \sim 0.03$, most of the entire flow energy is needed to power the hard X-ray region, thus $\dot{m}_{\text{hot}}$ is large. Conversely, for $\dot{m} \sim 0.4$, only a very small fraction of the available power is needed to make the hard X-ray flux, so $\dot{m}_{\text{hot}}$ is small. Figure 5a shows how the value of $\dot{m}_{\text{hot}}$ decreases as a function of increasing $\dot{m}$ in models where $L_{\text{diss,hot}}$ is fixed at $0.01L_{\text{Edd}}$ (dashed red), $0.02L_{\text{Edd}}$ (solid green) and $0.05L_{\text{Edd}}$ (dotted blue). The open stars show the values measured from fitting to the data scatter around the green line, consistent with constant $L_{\text{diss,hot}} = 0.02L_{\text{Edd}}$, especially considering the uncertainties on mass determination. The predicted decrease in size scale of the X-ray source with increasing $L_{\text{bol}}/L_{\text{Edd}}$ is compatible with the observations that the X-ray variability timescale decreases with increasing $L_{\text{bol}}/L_{\text{Edd}}$ (McHardy et al. 2016).

We also calculate the self consistent spectral index, $\Gamma_{\text{hot}}$, for the flow from eq.(14) in Beloborodov (1999) as

$$\Gamma_{\text{hot}} = \frac{7}{3} \left( \frac{L_{\text{diss,hot}}}{L_{\text{seed}}} \right)^{-0.1}$$

With the geometry of the truncated inner flow shown in Fig, 2a, $L_{\text{diss,hot}}$ and $L_{\text{seed}}$ are calculated via eq.(2) and (3), respectively. Figure 5b shows the resulting $\Gamma_{\text{hot}}$ assuming $L_{\text{diss,hot}} = 0.01L_{\text{Edd}}$ (dashed red), $0.02L_{\text{Edd}}$ (solid green) and $0.05L_{\text{Edd}}$ (dotted blue). The data (open stars) are in good agreement with the truncated disc geometry for $L_{\text{diss,hot}} = 0.02L_{\text{Edd}}$. The observed spectral indices are then consistent with a truncated disc geometry across the entire range of $\dot{m}$ considered here. This is surprising, especially at high $\dot{m}$, where the corona is more generally drawn as either X-ray hot plasma over the inner disc, or as a lamppost (compact source on the spin axis of the black hole). We explore truncated disc geometries in section 4.2.2 and 4.2.3.

Figure 4. The best estimated models overlayed on the data set of NGC 5548 (Mehdipour et al. 2015, Fig. 10), Mrk 509 (Mehdipour et al. 2011, Fig. 12), and PG 1115 + 407 (Jin et al. 2012a,b). The outer disc emission, the warm compton component, and the hard compton component are shown in magenta, green, and blue, respectively. Panels (a), (b), (c), (d), (e) and (f) corresponds to NGC 5548 with and without outer disc, Mrk 509 with and without outer disc and PG 1115 + 407 with and without outer disc, respectively.
4.2.2 passive disc and inner hot corona geometry

Instead of the truncated disc and inner hot flow, there can be an inner disc corona extending down to rISCO. The inner disc corona can be characterised by the fraction, f, of power dissipated in the corona with the remaining cooler disc material in the midplane (Svensson & Zdziarski 1994).

We first assume a maximal corona, with f = 1 extending over the inner disc from rhot to rISCO i.e. a total power dissipated in the corona of $L_{\text{diss,hot}} = 0.02L_{\text{Edd}}$ with a passive disc on the midplane. The difference between this and the truncated disc geometry (section 4.2.1) is that the inner disc on the midplane will intercept half of the X-ray emission from the corona for an isotropic source. The albedo, $a$, determines how much of the illuminating flux can be reflected. The reflected fraction at low energies depends strongly on the ionisation of the disc, but photons above ~50–100 keV cannot be reflected elastically due to Compton downscattering. This gives a maximum albedo for completely ionised (most reflective) material and this value depends on spectral shape. We evaluate $f_{\text{nthcomp}}$ as a function of ionisation of the disc, but photons above $\sim$50–100 keV cannot be reflected elastically due to Compton downscattering. This gives a maximum albedo for completely ionised (most reflective) material and this value depends on spectral shape. We evaluate this for a Compton spectrum ($n_{\text{THCOMP}}$) with $kT_e = 100$ keV and different values of $\Gamma$ and $a$. We evaluate this for a Compton spectrum ($n_{\text{THCOMP}}$) with $kT_e = 100$ keV and different values of $\Gamma$ and calculate the reflection albedo using REFLECT (Magdziarz & Zdziarski 1995) with $\xi = 10^6$ erg s$^{-1}$ cm. We choose this rather than the newer reflection models such as RELXILL as in the corona region only the emission lines and recombination continuum will add to the thermalised flux in making soft seed photons. This gives $a_{\text{max}} = 0.55 \sim 0.81$ for $\Gamma = 1.5 \sim 2.3$.

On the other hand, the seed photon power from reprocessing in the corona region results in

$$\frac{L_{\text{diss,hot}}}{L_{\text{seed}}} = \frac{f}{1 - \frac{2}{5}f - \frac{1}{2}fa} = \frac{2}{1 - a}$$

with maximal corona, $f = 1$ (see eq.3a) in Haardt & Maraschi (1993). This indicates

$$\Gamma_{\text{hot}} = \frac{7}{3} \left( \frac{2}{1 - a} \right)^{-0.1}$$

via eq.(6). Thus, $a_{\text{max}}$ and $\Gamma_{\text{hot,min}}$ is self-consistently determined as $a_{\text{max}} \sim 0.7$ and $\Gamma_{\text{hot,min}} \sim 1.9$ for an inner disc corona geometry. In Fig. 6, which shows the truncated disc results as a baseline model (green solid line) together with the data (open stars) from Fig. 5, we plot $\Gamma_{\text{hot}}$ as a horizontal dotted black line. This horizontal dotted black line shows the minimum photon index. The observed $\Gamma_{\text{hot}}$ for Mrk 509 sits on this lower limit, so can be explained also by this geometry. PG 1115 + 407 is somewhat steeper at $\Gamma_{\text{hot}} = 2.2$, which can also be explained by this geometry for $a = 0.3 < a_{\text{max}}$. However, NGC 5548 and other AGN with $\Gamma_{\text{hot}} < 1.9$ require a more photon starved geometry.

4.2.3 entire slab hot corona

The value of $\Gamma_{\text{hot}}$ becomes larger if there is intrinsic disc power (i.e., $f < 1$), which adds to the seed photons in the local slab geometry. This requires larger $r_{\text{hot}}$ to keep the same observed $L_{\text{diss,hot}}/L_{\text{Edd}}$. The most extreme case is where the corona extends over the entire optically thick disc so that $f$ is constant with radius. For such an entire slab geometry, the seed photons are given by eq.(3a) in Haardt & Maraschi (1993) as

$$\frac{L_{\text{seed}}}{L_{\text{Edd}}} = \left( 1 - \frac{1}{2f} - \frac{1}{2fa} \right) n\dot{m}$$

In this geometry the hard X-ray dissipation of $L_{\text{diss,hot}}/L_{\text{Edd}} = f\dot{m} = 0.02$ implies $f = 0.02\dot{m}$. We use this in the equation above to calculate $L_{\text{diss,hot}}/L_{\text{seed}}$ as

$$\frac{L_{\text{diss,hot}}}{L_{\text{seed}}} = \frac{f\dot{m}}{\left( 1 - \frac{1}{2f} - \frac{1}{2fa} \right) n\dot{m}} = \frac{2}{100\dot{m} - 1 - a}$$

and hence derive the spectral index via eq.(6). We plot these in Fig. 6 for three values of the albedo namely $\dot{a} = 0$ (dotted), 0.3 (solid) and 0.7 (dashed). These always give much steeper $\Gamma_{\text{hot}}$ than observed. Figure 6 shows that steep spectra of $\Gamma_{\text{hot}} = 3.1$–3.4 are predicted for $\dot{m} = -0.6 \sim 0$ while the observed photon indices are usually harder as $1.7 \sim 2.4$ (e.g., from 55 samples in Jin et al. (2012a). For lowest $\dot{m}$, $\Gamma_{\text{seed}}$ is still as large as 1.9. Thus the entire slab for the hot Comptonisation component is quite unlikely for both high and low $\dot{m}$. This problem is discussed in detail also e.g., by Stern et al. (1995), Malzac, Dumont, & Mouchet (2005) and Poutanen, Vedelina, & Zdziarski (2017) for the case of BHBs in the low/hard state. The problem is even more marked for AGN as the seed disc photons are at lower energies, making Compton cooling more efficient and leading to steeper predicted photon indices (Haardt & Maraschi 1993).

4.2.4 summary of constraints on the geometry of the hot corona

To summarise, the data at $\dot{m} \leq 0.1$ have $\Gamma_{\text{hot}} < 1.9$ which is incompatible with a disc-corona geometry even in the limit where all the power is dissipated in the corona. Spectra at higher $\dot{m} \geq 0.1$ have spectra which can be produced in an inner disc-corona geometry, but these require some fine tuning in order to produce the spectral indices observed. By contrast, the truncated disc/hot inner flow geometry can predict the behaviour of the spectral index over the entire range of $\dot{m}$, making it likely that this geometry is continued across all $L_{\text{hot}}/L_{\text{Edd}}$.

4.3 Warm comptonisation region

The warm Comptonisation region extends from $r_{\text{hot}}$ to an outer radius $r_{\text{warm}} \lesssim r_{\text{out}}$. Ideas which associate this with the changing vertical structure of a disc due to the importance of atomic opacities predict that the warm Comptonisation region should onset at an approximately fixed temperature. One attractive idea is that each annulus of the disc which is at the same temperature as an O star would be modified by a UV line driven wind (Laor & Davis 2014). The maximum disc temperature considering these wind losses is $(2–8) \times 10^4$ K in their models, which is similar to the range seen here for the onset of the warm Comptonisation of $(1–6) \times 10^4$ K. Thus it is possible that the onset of warm Comptonisation does link to the changing disc structure induced by UV opacities, though strong wind losses such as those predicted by Laor & Davis (2014) are ruled out by the observed efficiencies.

This overprediction of wind losses is probably linked to the assumption in Laor & Davis (2014) that there is only a disc, with no hard X-ray emission which will strongly suppress UV line driving by overionisation (Proga, Stone, & Kallman 2000). It seems plausible that the UV bright disc launches a UV driven disc wind, but that this becomes ionised as it rises up and is exposed to the X-ray source. The failed wind falls back down, impacting the disc, leading to shock heating of the photosphere, making the warm Comptonisation region. There are no calculations of this at the current time, but we expect that the extent of the failed wind will depend on the level of...
X-ray ionisation. This is clearly larger for lower $\dot{m}$. Guided by the fits to the individual objects above, we tie the size scale, $r_{\text{warm}} = 2r_{\text{hot}}$.

While the data do not favour all the outer disc being covered by the warm corona, they are (mostly) consistent with the idea that the disc underneath the warm Comptonising material is passive i.e., the optically thick material underneath the corona only reprocesses the luminosity dissipated further up in the disc (Petrucci et al. 2017). There is a trend seen also in (Petrucci et al. 2017), $\Gamma_{\text{warm}}$ is somewhat steeper for high $\dot{m}$, (e.g., PG1115+407 indicates some intrinsic power in the disc), and somewhat flatter at low $\dot{m}$ (e.g., NGC 5548). Steeper spectra can easily be produced with some intrinsic emission on the disc midplane. However, the lower spectral indices at low $\dot{m}$ are more difficult to explain.

Petrucci et al. (2017) suggest that $\Gamma_{\text{warm}} \leq 2.5$ is from partial covering of the corona over the passive midplane, so that some of the reprocessed photons do not re-intercept the warm Comptonisation region to cool it. While this does indeed allow reprocessed photons to escape, this also means that these seed photons from the disc are seen directly which is not consistent with their assumption that the optical/UV is dominated by warm Comptonisation alone, with no thermal emission from a disc (see also the discussion of this in Petrucci et al. 2017). Partial covering also seems physically unlikely as the optically thick, warm material has thermal pressure so should expand outwards so this additionally requires magnetic confinement. Instead, we suggest that the harder spectral indices could instead be produced by irradiation heating being more important at low $\dot{m}$ (see also Lawrence 2012). By definition, irradiation heats the photosphere at $\tau = 1$ rather than the deeper regions at $\tau = 10 - 20$ where the majority of the warm Comptonisation must be produced. We suggest that a more accurate treatment of an irradiated warm Comptonisation region above a passive disc could produce the harder indices observed at low $\dot{m}$.

![Figure 6. Same as Fig. 5b, but expected values of $\Gamma_{\text{hot}}$ for slab geometry with $L_{\text{diss,hot}} = 0.02L_{\text{edd}}$ (i.e., $f = 0.02$ with the fraction of power dissipated in the corona, $f$) are shown in black lines, together with the observed values of $\Gamma_{\text{hot}}$ for Mrk 509, NGC 5548 and PG 1115 + 407 (open stars) and $\Gamma_{\text{hot}}$ for truncated disc geometry with $L_{\text{diss,hot}} = 0.02L_{\text{edd}}$ (solid green). Albedo is assumed to be $a = 0$ (dash dot), 0.3 (solid) and 0.7 (dash). Horizontal dotted straight lines represent the lower limit of $\Gamma$ under an assumption of localized slab corona with maximal albedo, $a = 0.7$ and by assuming 'passive disc' underneath the corona, i.e., $f = 1$.](image)

![Figure 5. Radius of the hot inner flow, $r_{\text{hot}}$ (a) and photon index of the hot Compton component, $\Gamma_{\text{hot}}$ (b), are plotted against $\log \dot{m}$. The values are calculated assuming a fixed $L_{\text{diss,hot}}$ of 0.01$L_{\text{edd}}$ (dashed red line), 0.02$L_{\text{edd}}$ (solid green line), and 0.05$L_{\text{edd}}$ (dotted blue line). The spectral index is calculated with reprocess. The observed values of $r_{\text{hot}}$ and $\Gamma_{\text{hot}}$ for Mrk 509, NGC 5548 and PG 1115 + 407 are shown with open stars.](image)

![Table 3. Parameters used in section 5.1 and 5.2. ¹Geometry of hot inner flow + warm comptonising skin + outer disc. ²Geometry of hot inner flow + warm comptonising skin (i.e., without outer disc).](Table3)
5 PREDICTIONS OF THE FULL SED MODEL FOR THE OBSERVATIONAL RESULTS

5.1 UV/X relation

We use the individual AGN fits to define the full SED model in order to compare to a large sample of objects spanning a wide range in \( m - M \). Lusso & Risaliti (2017) show that there is a well defined relationship between the UV and X-ray luminosity of AGN, and claim this has low enough scatter to be used as a tracer of the cosmological expansion. Finding the underlying physics is then extremely important, as it can only be used with confidence when it is robustly understood.

Guided by the individual AGN fits above, we fix \( L_{\text{disk,hot}} = 0.02L_{\text{Edd}} \), which defines \( r_{\text{hot}} \). We assume that the hot inner flow is quasi-spherical, and that the optically thick flow truncates at \( r_{\text{hot}} \) so that the spectral index, \( \Gamma_{\text{hot}} \), can be calculated from the ratio of dissipation in the hot region to intercepted seed photons. The best fit models above strongly support a geometry where there are three dissipation in the hot region to intercepted seed photons. The best fit models above strongly support a geometry where there are three components, but again we compare the data to a model where the entire outer disc is covered by the warm Comptonisation material.

The inclination angle is expected to be between 0° and 60° for type 1 AGN so we fix this at 45°. Full model parameters are shown in Table 3. The model with \( r_{\text{warm}} = 2r_{\text{hot}} \) defines our simplified model QSOSED.

We calculate a grid of models spanning \( m = 0.03 - 1 \) and \( M = 10^{6} - 10^{10}M_{\odot} \). This is consistent with the range of \( m \) and \( M \) in Lusso & Risaliti (2017) (the majority of their sample have \( m = 0.03 - 1 \) and \( (1 - 10) \times 10^{5}M_{\odot} \). Lusso et al. 2012). Figure 7a shows the resulting relation between the monochromatic rest frame luminosity at 2500Å (i.e., 5 eV) and 2 keV, with lines connecting varying \( m \) for constant \( M \) from our model with an outer standard disc. Figure 7b shows the slightly different predictions from a model where the warm Comptonisation region covers the entire outer disc. Both these give a fairly well defined correlation between the UV and X-rays, though with some scatter. We compare these to the best fit UV/X relation derived from 545 SDSS quasars by Lusso & Risaliti (2017) of

\[
\log L_{2500\text{Å}} - 25 = 0.633 \cdot (\log L_{2500\text{Å}} - 25) - 1.959
\]

(solid black line) on Fig. 7a and b. It is clear that the observed correlation is a slightly different slope than predicted by our models over this entire range. Our models with an outer disc match quite well to the observed relation at high masses (Fig. 7a), while models with just a warm Comptonisation region are offset by their smaller predicted UV luminosity and match better at low masses (Fig. 7b).

Our predicted correlation is easy to understand, as it arises due to our assumptions that the X-ray flux is fixed at \( L_{X} = 0.02L_{\text{Edd}} \cdot M \) while the UV is from a disc/comptonised disc so \( L_{UV} \propto (M/M_{\odot})^{2/3} \propto (M^{2/3}n)^{2/3} \). This thus predicts \( L_{X} = 3/4 \log L_{UV} - 1/4 \log \dot{m} + b \) where \( b \) is a constant. There is clearly scatter in the models from \( \dot{m} \), but the range should be constrained between 0.02 – 1. The lower limit is where the entire accretion flow is expected to make a transition to an ADAF. Narayan & Yi (1995), so that there is no bright UV emitting disc left, so that there is no source of ionising flux to excite a BLR. The upper limit comes from the expectation that super-Eddington objects are rare. Thus there is only a limited range of 1.5 dex in \( \dot{m} \), and this reduces to 0.75 dex with the square root factor. However, the data from Lusso & Risaliti (2017) have a scatter of only 0.2 dex.

We study the predicted behaviour in more detail in Fig. 8, using the individual data points from Lusso & Risaliti (2017) (B. Lusso, private communication). These are selected from the SDSS quasar sample, so have absolute i-band magnitude brighter than \(-22\). This already limits the black hole mass to \( > 10^{7.5}M_{\odot} \) for objects with a standard disc below Eddington, and the masses reported in (Lusso et al. 2012, their Fig.6) are clustered around \((1 - 10) \times 10^{9}M_{\odot} \). Thus their data only include high black hole masses, so our models with an outer standard disc match fairly well in normalisation and slope to that observed (Fig. 8a), whereas models with complete coverage of the outer disc with a warm Comptonisation underpredict the UV luminosity (Fig. 8b).

Nonetheless, there is still a mismatch between the range predicted by our models and the observed data, even including an outer standard disc. The data extend to slightly higher UV luminosity than expected for Eddington limited systems. Some of this can be inclination, as more face on systems will have stronger UV flux, but this makes only a difference of 0.15 dex between our assumed mean inclination of 45° and 0°. While this may explain the AGN not covered by the grid in the model with an outer standard disc, it is not enough to explain the larger number missed by the grid if the warm corona covers the entire outer disc. Instead, these require a substantial population of super-Eddington AGN. Super-Eddington AGN are seen in the local Universe (Jin, Done, & Ward 2015; Done & Jin 2016; Jin et al. 2017), though they are rare, but their high UV luminosity enhances their probability of selection. We will extend the model to super-Eddington flows in a later work (Kubota & Done, in preparation), but note here that there are multiple uncertainties with the structure of these flows which makes robust prediction difficult.

There is the opposite problem for the highest mass black holes at the lowest \( m \), where the grid extends into a region where there are no data points. We suggest that this could be due to selection effects. High mass black holes are rarer, so require sampling a larger space volume in order to have a realistic probability of finding some. This means that they are generally seen at larger distances, so are only selected in flux limited samples if they have high luminosity, weighting the selection of high mass black holes towards higher \( m \) (including super-Eddington rates).

Thus the observed UV/X-ray relation is predicted by our model, where the X-ray luminosity is fixed at the 0.02\( L_{\text{Edd}} \) and the UV is from an outer standard disc, with selection effects (mostly the limited range of black hole mass) suppressing some of the predicted scatter. This is a very different explanation to that of Lusso & Risaliti (2017). Their ‘toy’ model uses the same standard disc equations to estimate the UV flux, but they set the X-ray flux using the gravitational power emitted from the outer disc down to the radius at which the disc becomes radiation pressure dominated. As they note in their paper, producing the X-rays at large radii in the disc rather than close to the black hole is in conflict with micro-lensing size scales, as well as with the rapid X-ray variability. We suggest that their model works because it effectively hardwires \( L_{X} \) to a constant value. The radius at which radiation pressure dominates in the disc, \( R_{\text{rad}} \), increases as \( m \) increases, so leaving a smaller and smaller fraction of power dissipated in the outer disc, and hence reproducing the observed decrease of \( L_{X}/L_{bol} \) with \( m \) (Vasudevan & Fabian 2007).

Formally, this gives \( R_{\text{rad}} \propto (\alpha M^{2/3}M_{\odot})^{16/21}(1 - f - f/7R_{S}) \), where \( f \) is the fraction of the accretion power which is dissipated in the hard X-ray coron (Svensson & Zdziarski 1994). Then the X-ray luminosity down through the corona from \( R_{\text{rad}} - R_{\text{rad}} \) is \( L_{X} \propto f GM\dot{M}/R_{\text{rad}} \propto \alpha^{-2/21}M^{19/21}m^{-5/21}f(1 - f)^{-6/7} \) (see their eq.(14) in detail). Hence \( L_{X} \) is roughly proportional to \( M \) and has only a weak dependence on \( m \), so their toy model is almost identical with our assumption of constant \( L_{\text{disk,hot}} = 0.02L_{\text{Edd}} \).

Our model hardwires the same absolute value of \( L_{X} \), but in a
5.2 Optical variability

The X-rays vary rapidly in a stochastic manner about a mean, so their reprocessed emission should also carry the imprint of this rapid variability. The assumption in our SED is that the hard X-rays carry a fixed luminosity but arise from a smaller region as $m$ increases. Hence the reprocessed luminosity depends on $L_{\text{disc,hot}} \times \dot{n}_{\text{hot}}$ (see Section 2.3) which decreases as $m$ increases. This reprocessed flux is seen against the remaining, constant component from the disc and/or warm Comptonisation region which increases with $m$. Thus the variable reprocessed emission forms a smaller fraction of the optical/UV emission at higher $m$, which qualitatively matches what is observed (MacLeod et al. 2010; Ai et al. 2013; Simm et al. 2016; Kozłowski et al. 2016).

Our model explicitly includes the reprocessed emission from X-ray illumination of the outer disc and warm Comptonisation region, so here we calculate the contribution that the varying X-ray emission can make to the optical variability. We illustrate this with our three component SED model, $\text{agnSED}$, (with all parameters as above, tabulated in table 3 with $\dot{n}_{\text{warm}} = 2\dot{n}_{\text{hot}}$) for AGN of 10$^9$ M$_\odot$ with $m = 0.05$ and 0.5 in Fig. 9a and b, respectively. The black lines show spectra based on the simple NT emissivity including repro-cessing, while red lines are the result of stochastic variability (so no impact on $\dot{n}_{\text{hot}}$, etc) increasing $L_{\text{hot}}$ by a factor of 2. The emission from both the outer disc and warm Comptonising region increases with the increase in $L_{\text{hot}}$, and it is clear that reprocessing makes a much larger fraction of the optical emission at low accretion rates than at high ones.

We quantify the fractional change in optical flux at 4000Å (3.1 eV), $\Delta f_{4000}/f_{4000}$, to a factor 2 increase in $L_{\text{disc,hot}}$ across the entire range of AGN masses ($M = 10^9 \sim 10^{10}$ M$_\odot$) and mass accretion rates ($\dot{m} = 0.03$–1). Figure 10a shows this fractional variability as the colour coding across the grid of log $M$/M$_\odot$ and log $\dot{m}$. It is obvious that lower $\dot{m}$ gives larger variability, though there is also a much smaller effect where the variability increases with larger mass. This occurs when reprocessing starts to affect the variability at the peak of the warm Comptonisation region, where the temperature shift increases the amplitude of variability (see Fig. 3).

We match this to the observed amplitude of variability seen in a large sample of quasars in SDSS stripe 82. MacLeod et al. (2010) characterise the variability at rest frame 4000Å with a damped random walk. The mean asymptotic amplitude of variability in optical magnitudes is characterised by the structure function extrapolated to infinite time, $S_F(\infty)$. This is plotted as a function of $i$-band magnitude, $M_i$, and black hole mass in their Fig. 14. In order to compare our models directly to their results, we convert our mass and $m$ to $M_i$ and convert our fractional variability at 4000Å to a magnitude difference ($2.5 \ln f_{4000}/f_{4000} = \Delta m$). Figure 10b shows this magnitude difference as a function of black hole mass and $M_i$ across the whole range of models calculated in Fig. 10a.

Figure 11a shows a zoom of Fig. 10b, limiting it to the same range in mass and $M_i$ as used by MacLeod et al. (2010). This can then be compared directly against the data in Fig.11b (C. Macleod in private communication). The range in $M_i$ for each black hole mass spanned by our models at a given $m$ is shown by the cyan lines for $m$ of 0.03, 0.1 and 1. This makes it plan that the most variable AGN are those with implied $m < 0.03$. These plausibly connect to the ‘changing look’ quasars if these are triggered by a state change from an outer disc to an ADAF flow (e.g., Noda & Done 2018).

Figure 11a also stresses the need to use the non-linear conversion between optical flux and bolometric luminosity which is inherent in the standard disc equations. Hence our data with $m = 0.03 – 1$ do not span the entire range of $M_i$ which are associated with this range in $m$ in Fig.15 of MacLeod et al. (2010). There are again some AGN with $m > 1$. These are rare (Fig. 12 in MacLeod et al. 2010), but they considerably extend the range in $M_i$ for the lowest mass AGN included here.

The colour grid is the same between Fig. 11a and b, and the models with a factor 2 variability in X-rays give the observed amount of optical variability at $\dot{m} = 0.03$. Our models predict a weak trend for higher variability at higher black hole masses at fixed $m$, which is opposite to the observed weak trend for higher variability at lower $M$ but this may not be a serious discrepancy as the timescales for the higher mass black holes are longer, which lead to some variability being missed. A much bigger discrepancy is that the models predict almost no variability at $\dot{m} = 1$, unlike the data which still show variability at the 10% level. This clearly shows that some other component is required to make at least part of the optical variability, though the most rapid variability (e.g. from Kepler light curves: Aranżana et al. 2018) must arise from X-ray reprocessing. An additional source of longer term optical variability also matches with results from more intensive monitoring campaigns which stress the lack of correlation between the X-ray and optical lightcurves (e.g., Árvalo et al. 2009), Gardner & Done (2017) suggest that variability of the soft X-ray excess may play a role, but in our models here this still makes little impact on the optical spectrum at $\dot{m} = 1$. Instead, there should be intrinsic variability in the disc spectrum assuming our disc dominated SED are the correct description of AGN close to the Eddington limit. Standard disc models do indeed predict that AGN discs should be highly unstable due to their dominant radiation pressure, but the non-linear outcome of what should be limit cycle variability is not yet known (Hameury, Viallet, & Lasota 2009 use a heating prescription which goes with only gas pressure to avoid complete disc disruption).

6 SUMMARY AND CONCLUSIONS

We construct a new spectral model $\text{agnSED}$ which includes an outer standard disc, a middle region where the disc is covered by optically thick, warm Comptonising electrons, and an inner region of hot plasma which emits the power law X-ray component. We assume that these regions are separated in radius, and that their emission is determined by the overall NT emissivity. This sets the size scale of the hot X-ray plasma and we include reprocessing of the X-rays from this source which illuminate the outer and warm Comptonising disc.

We fit this model to multiwavelength SEDs of three well observed AGN with very different Eddington ratios, NGC 5548 ($\dot{m} \sim 0.03$), Mrk 509 ($\dot{m} \sim 0.1$), and PG 1115 + 407 ($\dot{m} \sim 0.4$). The observed spectra are well reproduced with the model, and require an outer standard disc as well as a warm Comptonisation component. This is different to conclusions from previous spectral fits as we constrain our warm Comptonisation component to have seed photons and luminosity from an underlying disc rather than allowing these to be free parameters. The midplane disc is generally passive i.e. the seed photons are produced by reprocessing rather than intrinsic dissipation, which sets the spectral index to $\Gamma_{\text{warm}} = 2.5$ (Petrucci et al. 2017). The transition between the standard disc and
Figure 7. Monochromatic luminosities $\log L_X$ against $\log L_{2500}$ for black hole of $M = (0.1-1) \times 10^7 M_\odot$ (cyan), $(0.16-1) \times 10^8 M_\odot$ (blue), $(0.16-1) \times 10^9 M_\odot$ (green), $(0.16-1) \times 10^{10} M_\odot$ (red). From left to right $\mu t$ changes from 0.03 to 1. The observed UV/X relation in the range of $\log L_{2500} - 25 = 3.8-7.4$ (Lusso & Risaliti 2017, Fig. 3) is shown with a solid line. A dashed line is an extrapolation of the solid line. (a) Our three component flow, with an outer disc, warm Comptonisation region and hot inner flow. (b) A model where there is no standard outer disc.

Figure 8. Enlargements of Fig. 7 are overlayed on the observed data points in Fig. 3 of Lusso & Risaliti (2017) shown with open grey circles.

warm Comptonisation is always at temperatures consistent with the peak in UV opacity which might point to its origin in the changing disc structure due to failed UV line driven winds (Laor & Davis 2014). The hot plasma has almost constant dissipation, consistent with $0.02-0.04 \dot{M}_Edd$ for all $\mu t$. This implies a smaller size scale with increasing $\mu t$, as inferred from X-ray variability (McHardy et al. 2006). The hard X-ray spectral index is consistent with this dissipation always taking place in a region with no underlying disc i.e. a truncated disc/hot inner flow geometry.

Fixing this derived geometry gives a full SED model which depends only on mass and mass accretion rate. This model successfully explains the observed tight UV/X relation shown by Lusso & Risaliti (2017) as a combination of the constant hard X-ray dissipation together with selection effects which mean that the rarer, higher mass quasars are seen preferentially at larger distances so require higher Eddington fractions to be detected. This selection effect introduces scatter and bias but our model gives a physically based understanding of these factors, so that the relation can be used to probe cosmology.

The model includes the contribution to the optical/UV flux from X-ray illumination of the outer disc and warm Comptonisation region. We calculate the optical variability resulting from a stochastic change in X-ray flux. This predicts the fast variability in optical should be a strongly decreasing function of Eddington fraction, as the fixed (average) hard X-ray dissipation is a smaller fraction of the bolometric luminosity at higher Eddington ratios. This matches to some of the trends seen in systematic surveys of AGN variability e.g., SDSS Stripe 82 (MacLeod et al. 2010), but there is more variability seen in high Eddington fraction AGN than predicted. This probably indicate that such highly radiation pressure dominated discs are somewhat unstable. This should motivate theoretical studies to give better understanding of such discs.

ACKNOWLEDGEMENTS

We thank to M. Mehdipour for providing us SEDs in Mehdipour et al. (2011, 2015) and helpful comments on the data. We are also grateful to C. Macleod and E. Lusso for providing us the data points in MacLeod et al. (2010) and Lusso & Risaliti (2017), and useful discussions and comments. Special thanks to H. Noda and C. Jin for helpful discussions. AK is supported by research program in foreign country by Shibaura Institute of Technology. CD acknowledges support from STFC (ST/P000541/1), and use-
Figure 9. Effects of hard X-ray reprocess for a black hole of $M = 10^8 M_\odot$ with $\dot{m} = 0.05$ (a) and 0.5 (b). SEDs in which the hard X-ray luminosity is increased by a factor of 2.0 (red) are compared with those with Novikov-Thorne emissivity with hard X-ray reprocess (black).

ful conversations with O. Blaes and J.M. Hameury. We also thank P.O.Petrucci as our referee for valuable comments.

REFERENCES

Anders E., Ebihara M., 1982, GeCoA, 46, 2363
Davis S. W., Hubeny I., 2006, ApJS, 164, 530

Figure 10. (a)The time variability $\log \Delta f_{4000}/f_{4000}$ are shown as color grid of black hole mass $\log M/M_\odot$ and $\log \dot{m}$. Hot X-ray emission is increased by a factor of 2.0. (b) Same as the top panel but $\log \Delta f_{\text{flux}}/f_{\text{flux}}$ and $\log \dot{m}$ are converted into $\log \Delta \text{mag}$ at 4000Å and i-band absolute magnitude $M_i$. SEDs are based on the parameters of model (1) in table 3.

Done C., Gierliński M., Kubota A., 2007, A&ARv, 15, 1
Figure 11. (a) Enlargement of Fig. 10b. Black dots represent the places which we calculate. (b) log SF(∞) at 4000Å are plotted in space of $M_1$ and log $M/M_⊙$ (Fig.14 in MacLeod et al. 2010). These data points are given by C.Macleod in private. Colour grid is the same between these two panels. Contours of constant $\Delta m_{avg}$ in the top panel are overlaid on the bottom panel. Solid cyan lines show constant m of 0.03, 0.1 and 1.

APPENDIX A: PARAMETERS OF THE MODEL

We show all the spectral parameters of AGN SED. The model has some switching parameters. If instead of $\alpha$, albedo is fixed at $a = 0.3$. Seed photon temperature for the hot Comptonisation component is calculated internally (see section 2.2). $r_{hot}$ is adopted as a fitting parameter instead of $I_{diss, hot}$. The model has some switching parameters. If

Noda H., Makishima K., Nakazawa K., Uchiyama H., Yamada S., Sakurai S., 2013, PASJ, 65, 4
Novikov I. D., Thorne K. S., 1973, blho.conf, 343

Table A1. Parameters in \textsc{agnsed}.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>par1</td>
<td>mass, black hole mass in solar masses</td>
</tr>
<tr>
<td>par2</td>
<td>dist, comoving (proper) distance in Mpc</td>
</tr>
<tr>
<td>par3</td>
<td>( \log m, m = \frac{M}{M_{\text{Edd}}} ) where ( \eta M_{\text{Edd}}c^2 = L_{\text{Edd}} )</td>
</tr>
<tr>
<td>par4</td>
<td>( a^* ), dimensionless black hole spin</td>
</tr>
<tr>
<td>par5</td>
<td>( \cos i ), inclination angle ( i ) for the warm Comptonising component and the outer disc.</td>
</tr>
<tr>
<td>par6</td>
<td>( kT_{e,\text{hot}} ), electron temperature for the hot Comptonisation component in keV. If this parameter is negative then only the hot Comptonisation component is used.</td>
</tr>
<tr>
<td>par7</td>
<td>( kT_{e,\text{warm}} ), electron temperature for the warm Comptonisation component in keV. If this parameter is negative then only the warm Comptonisation component is used.</td>
</tr>
<tr>
<td>par8</td>
<td>( \Gamma_{\text{hot}} ), spectral index of the hot Comptonisation component. If this parameter is negative, the code will use the value calculated via eq.(6).</td>
</tr>
<tr>
<td>par9</td>
<td>( \Gamma_{\text{warm}} ), spectral index of the warm Comptonisation component. If this parameter is negative then only the outer disc component is used.</td>
</tr>
<tr>
<td>par10</td>
<td>( r_{\text{hot}} ), outer radius of the hot Comptonisation component in ( R_g )</td>
</tr>
<tr>
<td>par11</td>
<td>( r_{\text{warm}} ), outer radius of the warm Comptonisation component in ( R_g )</td>
</tr>
<tr>
<td>par12</td>
<td>( \log r_{\text{out}} ), log of the outer radius of the disc in units of ( R_g ). If this parameter is negative, the code will use the self gravity radius as calculated from \textcite{Laor &amp; Netzer 1989}.</td>
</tr>
<tr>
<td>par13</td>
<td>( h_{\text{max}} ), the upper limit of the scaleheight for the hot Comptonisation component in ( R_g ). If this parameter is smaller than parameter 10, the hot Comptonisation region is a sphere of radius ( h_{\text{max}} ) by keeping ( L_{\text{diss,hot}} ) determined by ( r_{\text{hot}} ) via eq.(2).</td>
</tr>
<tr>
<td>par14</td>
<td>Switching parameter for the reprocessing, 0 or 1. If this parameter is 0, reprocessing is not considered. If this parameter is 1, reprocessing is included.</td>
</tr>
<tr>
<td>par15</td>
<td>Redshift</td>
</tr>
</tbody>
</table>

Parameter 6 is negative, the model gives the hot comptonisation component. And if parameter 7 is negative, the model gives the warm comptonisation component. If parameter 9 is negative, the model gives the outer disc. If parameter 12 is negative, the code will use the self gravity radius as calculated from \textcite{Laor & Netzer 1989}. \textsc{qosed} is the simplified version of \textsc{agnsed} by fixing some parameters at the typical values and by including reprocessing. The spectral parameters are shown in table A2. The rest of the parameters are fixed at \( kT_{e,\text{hot}} = 100 \text{ keV}, kT_{e,\text{warm}} = 0.2 \text{ keV}, \Gamma_{\text{warm}} = 2.5, r_{\text{warm}} = 2r_{\text{hot}}, r_{\text{out}} = r_{\text{rg}} \) and \( h_{\text{max}} = 100 \). Also, \( \Gamma_{\text{hot}} \) is calculated via eq.(6) and \( r_{\text{hot}} \) is calculated to satisfy \( L_{\text{diss,hot}} = 0.02L_{\text{Edd}} \). 

This paper has been typeset from a TEX/L Tex file prepared by the author.