The Cosmic Ballet: spin and shape alignments of haloes in the cosmic web

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ABSTRACT
We investigate the alignment of haloes with the filaments of the cosmic web using an unprecedentedly large sample of dark matter haloes taken from the P-Millennium Lambda cold dark matter cosmological N-body simulation. We use the state-of-the-art NEXUS morphological formalism which, due to its multiscale nature, simultaneously identifies structures at all scales. We find strong and highly significant alignments, with both the major axis of haloes and their peculiar velocity tending to orient along the filament. However, the spin–filament alignment displays a more complex trend changing from preferentially parallel at low masses to preferentially perpendicular at high masses. This ‘spin flip’ occurs at an average mass of $5 \times 10^{11} h^{-1} M_\odot$. This mass increases with increasing filament diameter, varying by more than an order of magnitude between the thinnest and thickest filament samples. We also find that the inner parts of haloes have a spin flip mass that is several times smaller than that of the halo as a whole. These results confirm that recent accretion is responsible for the complex behaviour of the halo spin–filament alignment. Low-mass haloes mainly accrete mass along directions perpendicular to their host filament and thus their spins tend to be oriented along the filaments. In contrast, high-mass haloes mainly accrete along their host filaments and have their spins preferentially perpendicular to them. Furthermore, haloes located in thinner filaments are more likely to accrete along their host filaments than haloes of the same mass located in thicker filaments.

Key words: methods: numerical – galaxies: haloes – large-scale structure of Universe.

1 INTRODUCTION
Starting from almost uniform initial conditions, the Universe has evolved over billions of years to contain a wealth of structure, from small-scale virialized objects, such as haloes and galaxies, to tens-of-Megaparsec-sized structures, such as superclusters and filaments (Peebles 1980; Oort 1983; Springel, Frenk & White 2006; Frenk & White 2012; Tempel 2014; Tully et al. 2014). All these are embedded in the so-called cosmic web, a wispy weiblike spatial arrangement consisting of dense compact clusters, elongated filaments, and sheetlike walls, amidst large near-empty void regions (Bond, Kofman & Pogosyan 1996; van de Weygaert & Bond 2008) and a distinct asymmetry between voids and overdense regions. The large-scale web is shaped by the large-scale tidal field, which itself is generated by the inhomogeneous distribution of matter. Within this context, the cosmic web is the most salient manifestation of the anisotropic nature of gravitational collapse, and marks the transition from the primordial (Gaussian) random field to highly non-linear structures that have fully collapsed into haloes and galaxies.

The same tidal field that shapes the cosmic web is also the source of angular momentum build-up in collapsing haloes and galaxies. This is neatly encapsulated by Tidal Torque Theory (TTT), which explains how in the linear stages of evolution the tidal field torques the non-spherical collapsing protohalo to generate a net rotation or spin (Hoyle 1949; Peebles 1969; Doroshkevich 1970; White 1984). Specifically, this occurs due to a differential alignment between the inertia tensor of the protohalo and the local gravitational tidal tensor. TTT posits a direct correlation between halo properties such as angular momentum, shape, and the large-scale tidal field at their location (see Schäfer 2009 for a review). For example, linear TTT predicts that the halo spin is preferentially aligned with the direction of secondary collapse [Lee & Pen (2001), but see Jones & van de Weygaert (2009)], and thus the spin is perpendicular on the...
direction of slowest collapse, which corresponds to the filament ridge (Efstathiou & Jones 1979; Barnes & Efstathiou 1987; Heavens & Peacock 1988; Lee & Pen 2001; Porciani, Dekel & Hoffman 2002a,b; Lee 2004). This alignment is mostly imprinted at the time of turn-around, when the protohaloes are the largest, and is expected to be preserved during the subsequent non-linear collapse of the protohaloes into virialized objects.

Large cosmological simulations have shown that the alignments of halo shape and spin with their surrounding mass distribution are not as straightforward as predicted by the simplified TTT framework described above. The correlations present in the linear phase of structure formation are preserved in the case of halo shapes, which are strongly oriented along the filament in which the haloes are embedded, with the alignment strength increasing with halo mass (Altay, Colberg & Croft 2006; Aragón-Calvo et al. 2007b; Aragón-Calvo 2007; Bruno et al. 2007; Hahn et al. 2007). In contrast, the spin of haloes shows a more complex alignment with their host filament. This was first pointed out by Aragón-Calvo et al. (2007b), and shortly thereafter by Hahn et al. (2007), which have shown that the spin–filament alignment is mass-dependent, with low- and high-mass haloes having a preferential parallel and perpendicular alignment, respectively. This result has since been reproduced in multiple cosmological simulations with and without baryons (Hahn, Teyssier & Carollo 2010; Codis et al. 2012; Libeskind et al. 2013; Trowland, Lewis & Bland-Hawthorn 2013; Dubois et al. 2014; Forero-Romero, Contreras & Padilla 2014; Wang & Kang 2017). The alignment has been confirmed by observational studies, most outstandingly so in the finding by Tempel, Stoica & Saar (2013) that massive elliptical galaxies tend to have their spin perpendicular to their host filaments while the spin of less massive bright spirals has a tendency to lie parallel to their host filaments (see also Jones, van de Weygaert & Aragón-Calvo 2010; Tempel & Libeskind 2013; Zhang et al. 2013, 2015; Hirv et al. 2017). The transition mass from halo spins preferentially perpendicular to preferentially parallel to their host haloes is known as the spin flip mass. While most studies agree on the existence of such a transition mass, they report highly disparate values for the spin flip mass that spread over more than an order of magnitude in halo mass, from ~0.5 to ~5×10^13 h^−1 M⊙. Furthermore, the spin flip mass varies with the smoothing scales used to identify the large-scale filaments, being higher for larger smoothing scales (Codis et al. 2012; Aragón-Calvo & Yang 2014; Forero-Romero et al. 2014), and decreases at higher redshifts (Codis et al. 2012; Wang & Kang 2018). It suggests that the mechanisms responsible for the tendency of low-mass haloes to have their spins oriented along their host filaments are complex, being both time and environment dependent.

Previous works have postulated a diverse set of explanations for the spin flip phenomenon, with most responsible processes having to do with the nature of halo late-time mass accretion, the so-called secondary accretion (Bertschinger 1985). A theoretical solution is provided by Codis, Pichon & Pogosyan (2015), who explain the dichotomy in spin–filament alignment between low- and high-mass haloes within the TTT framework. The key is that filaments form only in certain large scale tidal field configurations, in which the alignment between the inertia tensor and the tidal field follows a particular distribution that is different from the general expectation. Codis et al. (2015) and Laigle et al. (2015) have suggested also that this is due to the vorticity distribution inside filaments (for galaxies, see Pichon et al. 2011). They have claimed that the filament cross-section can be split into four quadrants, each with an opposite vorticity sign. Low-mass haloes typically reside in one of the four quadrants and thus acquire a spin along the filament, while high-mass haloes overlap multiple vorticity quadrants and acquire a spin that is preferentially perpendicular on their host filament. Welker et al. (2014) have shown that massive galaxies tend to have their spin perpendicular to their filament due to an excess of mergers along the filament direction, while low-mass galaxies tend to be aligned along their filament due to having undergone none or many fewer mergers. However, Bett & Frenk (2012, 2016) have shown that more than 75% of changes in halo spins are due to accretion of small substructures or flyby encounters, and not due to major mergers. On the other hand, Wang & Kang (2017, 2018) have explained the spin–filament alignment in terms of the formation time of haloes and their migration time from sheets into filaments. Low-mass haloes accrete most of their mass at high redshift, while residing in sheets, while high-mass objects undergo most of their growth at low redshift, when they are embedded in filaments.

In this study, we carry out a systematic analysis of the alignment between the spin and shape of haloes and the orientation of the filaments in which the haloes reside. We employ one of the largest cosmological simulations available, P-Millennium, which is characterized by a large volume and very high-mass resolution, with the large dynamic range being critical for our goal of understanding how the large-scale cosmic web influences small-scale phenomena, such as spin and shape orientations of haloes. We identify the cosmic web using the state-of-the-art NEXUS technique, which employs a multiscale formalism to identify in one go both prominent and tenuous filaments (Cautun, van de Weygaert & Jones 2013; see Libeskind et al. 2018 for a comparison to other web detection methods). We employ two NEXUS variants, NEXUS+ and NEXUS_velshear, which identify the web on the basis of the density and the velocity shear fields, respectively. These two NEXUS variants show the largest difference between their identified filamentary network (Cautun et al. 2014) and comparing the halo–filament alignments between the two method reveals key details about the processes behind the halo–filament alignments and their dependence on halo mass.

Our analysis involves two major new themes which have not been studied in the literature and which we show to be indispensable for understanding the halo–filament alignments. First, we study the properties of the entire halo as well as those corresponding to different inner radial cuts. The latter is highly relevant since: (i) galaxies are very strongly aligned with the inner region of the halo, and only poorly with the full halo (Bailin & Steinmetz 2005; Tenneti et al. 2014; Velliscig et al. 2015; Shao et al. 2016; Chisari et al. 2017), and (ii) recent accretion is mainly deposited in the outer regions of the halo (Salvador-Solé, Solanes & Manrique 1998; Wechsler et al. 2002; Tasitsiomi et al. 2004; Wang et al. 2011) and thus the alignments of the inner regions trace the alignment of the full halo at high redshift. The second novel feature involves studying the halo spin–filament alignment as a function of filament properties to find that the spin flip mass shows a very strong dependence on filament thickness.

The layout of the paper is as follows: Section 2 introduces the cosmological simulations and the NEXUS formalism used to identify the cosmic web; Section 3 describes the halo catalogues, how we calculate halo spins and shapes, and presents a detailed comparison of the halo population in filaments between our two web finders; Section 4 presents the main results regarding the halo spin–filament alignment; Section 5 studies the alignment between the shape of haloes and their host filaments; in Section 6 we present a detailed discussion on how secondary accretion is likely to be the main process that shapes the halo spin–filament alignment; and we end with a summary and discussion of our main results in Section 7.
Figure 1. A $2\ h^{-1}\ \text{Mpc}$ slice through the $z = 0$ density field of the P-Millennium simulation. The width and height of the figure corresponds to the side length of the simulation. The colour bar indicates the density contrast, $1 + \delta$.

2 FILAMENT POPULATION

Our analysis is based on a high-resolution simulation with an unsurpassed dynamic range, Planck-Millennium, which we introduce in this section. Here, we also describe the filament identification procedure, which is based on two different versions of the MMF/NEXUS cosmic web detection algorithm: one starting from the density field and the other from the velocity shear field. By comparing the two filament populations, we hope to identify supplementary information on the processes that affect the alignment of halo angular momentum with the large-scale structure.

2.1 Simulation

For this study we used the Planck-Millennium high-resolution simulation (hereafter P-Millennium; McCullagh et al. 2017; Baugh et al. 2018), which is a dark matter only $N$-body simulation of a standard ΛCDM cosmology. It traces structure formation in a periodic box of $542.16\ h^{-1}\ \text{Mpc}$ side length using $5040^3$ dark matter particles, each having a mass of $1.061 \times 10^8\ h^{-1}\ \text{M}_\odot$. The cosmological parameters of the simulation are those obtained from the latest Planck survey results (Planck Collaboration XVI 2014): the density parameters are $\Omega_\Lambda = 0.693$, $\Omega_m = 0.307$, the amplitude of the density fluctuations is $\sigma_8 = 0.8288$, and the Hubble parameter is $h = 0.6777$, where $h = H_0/100\ \text{km s}^{-1}\ \text{Mpc}^{-1}$ and $H_0$ is the Hubble’s constant at present day. In the analysis presented here we limit ourselves to the mass distribution at the current epoch, $z = 0$.

Due to its large dynamic range and large volume, the P-Millennium simulation is optimally suited for investigating the issue of angular momentum acquisition and the relation between spin and web-like environment over a large range of halo masses. P-Millennium simulates the formation nearly 7.5 million well resolved haloes over three orders of magnitude in halo mass, which is critical for the success of this work. This is especially the case for
the alignment between halo spin and filament orientation, which is a subtle effect (e.g. see Aragón-Calvo et al. 2007b; Libeskind et al. 2013), and for robustly characterizing the dependence of this alignment on halo mass, which is one of the principal aspects addressed in this paper. Besides its importance for identifying the subtle dynamical effects underlining the spin transition, the large volume of P-Millennium allows us to fully take into account the large-scale tidal forces responsible for the generation of halo angular momentum and for the formation of the cosmic web.

A visual illustration of the mass distribution in the P-Millennium simulation is shown in Fig. 1. It shows a slice of 2 h^{-1} Mpc width through the entire simulation box, with the white-blue colour scheme representing the density contrast,

\[ 1 + \delta(x, t) = \frac{\rho(x)}{\rho_u}, \]

where \( \rho(x) \) and \( \rho_u \) denote the local and background mean density. Clearly visible is the intricate structure of the cosmic web, with its visual appearance dominated by elongated medium to high-density filaments and low-density voids. The image illustrates some of the characteristic properties of the cosmic web, such as the complex and pervasive connectivity of the filamentary network. We also recognize the multiscale structure of the web: the dominant thick filaments, which are often found in high density regions bridging the cluster mass haloes and the thin, tenuous filamentary tendrils that branch out from the thick ones. These thin filaments typically have lower densities and pervade the low-density void regions. Note that in a two-dimensional slice like the one shown in Fig. 1, it is difficult to make a clear distinction between filaments and cross-sections through planar walls (Cautun et al. 2014). However, the more moderate density of the walls means that they would not correspond to the most prominent high-density ridges seen in the slice.

2.2 Filament detection

We use the MMF/NEXUS methodology for identifying filaments in the P-Millennium simulation. The MMF/NEXUS multiscale morphology technique (Aragón-Calvo et al. 2007a; Cautun et al. 2013) performs the morphological identification of the cosmic web using a Scale-Space formalism that ensures the detection of structures present at all scales. The formalism consists of a fully adaptive framework for classifying the matter distribution on the basis of local variations in the density, velocity or gravity fields, which are encoded in the Hessian matrix. Subsequently, a set of morphological filters is used to classify the spatial distribution of matter into three basic components: the nodes, filaments, and walls of the cosmic web. The outcome of the identification procedure is a set of diverse and complex cosmic web components, from the prominent features present in overdense regions to the tenuous networks pervading the cosmic voids.

The NEXUS version of the MMF/NEXUS formalism (Cautun et al. 2013, 2014) builds upon the original Multiscale Morphology Filter (Aragón-Calvo et al. 2007b,a) algorithm and was developed with the goal of obtaining a more robust and more physically motivated environment classification method. The full NEXUS suite of cosmic web identifiers (see Cautun et al. 2013) includes options for a range of cosmic web tracers, such as the raw density, the logarithmic density, the velocity divergence, the velocity shear, and the tidal force fields. NEXUS has incorporated these options in a versatile code for the analysis of cosmic web structure and dynamics following the realization that they represent key physical aspects that shape the cosmic mass distribution.

The goal of our analysis of halo–filament alignments is to understand the role of large-scale tidal forces in the acquisition of angular momentum in haloes. The dominant tidal field effects and the large-scale peculiar velocity flows are expected to be related to the most prominent web-like structures. This motivates us to employ two methods for identifying the cosmic web filaments, on the basis of their signature in the shear or velocity fields. By contrasting the alignments of the halo spin with the two filament populations, we seek to disentangle the contribution of local small-scale forces from those of larger scale ones.

2.2.1 MMF/NEXUS

A major advantage of the MMF/NEXUS formalism is that it simultaneously pays heed to two crucial aspects of the web-like cosmic mass distribution: the morphological identity of structures and the multiscale character of the distribution. The first aspect is recovered by calculating the local Hessian matrix, which reveals the existence and identity of morphological web components. The second, equally important, aspect uses a scale-space analysis to uncover the multiscale nature of the web, which is a manifestation of the hierarchical evolution of cosmic structure formation.

The scale-space representation of a data set consists of a sequence of copies of the data at different resolutions (Florack & Lindeberg 1998). A feature searching algorithm is applied to all of these copies, and the features are extracted in a scale independent manner by suitably combining the information from all the copies. A prominent application of scale-space analysis involves the detection of the web of blood vessels in a medical image (Sato et al. 1998; Li, Sone & Doi 2003), which bears a striking similarity to the structural patterns seen on Megaparsec scales. The MMF formalism has translated, extended, and optimized the scale-space methodology to identify the principal morphological elements in the cosmic mass and galaxy distribution.

The outcome of the MMF/NEXUS procedure is a volume-filling field which specifies at each point the local morphological signature: node, filament, wall, or void. The MMF/NEXUS methods perform the environment detection by applying their formalism first to nodes, then to filaments, and finally to walls. Each volume element is assigned a single environment characteristic by requiring that filament regions cannot be nodes and that wall regions cannot be either nodes or filaments. The remaining regions are classified as voids.

The basic setup of MMF/NEXUS is to define a four-dimensional scale-space representation of the input tracer field \( f(x) \). In nearly all implementations this is achieved by means of a Gaussian filtering of \( f(x) \) over a set of scales \( \{R_0, R_1, ..., R_N\} \).

\[ f_{R_n}(x) = \int \frac{d^3k}{(2\pi)^3} \frac{1}{\sqrt{2\pi \sigma^2}} e^{-k^2/2} \hat{f}(k) e^{i k \cdot x}, \]

where \( \hat{f}(k) \) is the Fourier transform of the input field \( f(x) \).

Subsequently, the Hessian, \( H_{ij, R_n}(x) \), of the filtered field is calculated via

\[ H_{ij, R_n}(x) = R_n^2 \frac{\partial^2 f_{R_n}(x)}{\partial x_i \partial x_j}, \]

where the \( R_n^2 \) term is as a renormalization factor that has to do with the multiscale nature of the algorithm. When expressed in Fourier space, the Hessian becomes

\[ H_{ij, R_n}(k) = -k_i k_j R_n^2 \hat{f}(k) e^{-k^2/2}. \]

While in principle there are an infinite number of scales in the scale-space formalism, in practice our implementation uses a finite number of filter scales, restricted to the range of \([0.5, 4.0] h^{-1} \text{ Mpc}\)
This range has been predicated on the expected relevance of filaments for understanding the properties of the haloes in our sample, which have masses in the range $5 \times 10^{10}$ to $1 \times 10^{13} M_\odot$ (see next section). The upper filter scale of $4 h^{-1}$ Mpc allows the identification of the most massive filaments, while the lower filter scale allows for the detections of thin and tenuous filaments that host the occasional isolated low-mass haloes.

The morphological signature is contained in the local geometry as specified by the eigenvalues of the Hessian matrix, $h_1 \leq h_2 \leq h_3$. The eigenvalues are used to assign to every point, $x$, a node, filament, and wall characteristics which are determined by a set of morphology filter functions (see Aragón-Calvo et al. 2007b; Cautun et al. 2013). The morphology filter operation consists of assigning to each volume element and at each filter scale an environment signature, $S_{R_\delta}(x)$. Subsequently, for each point, the environmental signatures calculated for each filter scale are combined to obtain a scale independent signature, $S(x)$, which is defined as the maximum signature over all scales,

$$S(x) = \max_{R_{\delta}} S_{R_{\delta}}(x). \quad (5)$$

The final step in the MMF/NEXUS procedure involves the use of criteria to find the threshold signature that identifies valid structures. Signature values larger than the threshold correspond to real structures while the rest are spurious detections. For nodes, the threshold is given by the requirement that at least half of the nodes should be virialized. For filaments and walls, the threshold is determined on the basis of the change in filament and wall mass as a function of signature. The peak of the mass variation with signature delineates the most prominent filamentary and wall features of the cosmic web (for more details and for a study of different threshold values for the environment signature see Cautun et al. 2013).

### 2.2.2 NEXUS+ and NEXUS velocity shear

In our study, we use two NEXUS methods for identifying filament populations. The first, the NEXUS+ algorithm, is based on the local geometry of the density field. The strongly non-Gaussian nature of the non-linearly evolved density field is marked by density ranges over many orders of magnitude. Simply applying a Gaussian smoothing can wash out the anisotropic nature of the matter distribution, especially close to high-density peaks. This can be alleviated by applying a Log-Gaussian filter to each element at each filter scale and an environment signature, $S_{R_{\delta}}(x)$. Subsequently, for each point, the environmental signatures calculated for each filter scale are combined to obtain a scale independent signature, $S(x)$, which is defined as the maximum signature over all scales,

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#### 2.3 Density- versus shear-based filaments

There are several intriguing differences in filament populations identified by NEXUS+ and NEXUS velocity shear. Both procedures identify the most prominent and dynamically dominant arteries of the cosmic web. These massive filaments, with diameters of the order of $5 h^{-1}$ Mpc, may extend over vast lengths, sometimes over tens of Megaparsec. They are the main transport channels in the large-scale universe, along which matter, gas, and galaxies flow towards higher density mass concentrations. As such, they can nearly always be identified with pairs of massive and compact clusters, whose strong tidal forces give rise to very prominent and massive filaments (Bond et al. 1996; Colberg, Krughoff & Connolly 2005; van de Weygaert & Bond 2008; Bos et al. 2016). They are nearly always located on the boundaries of large voids. These filaments have a dominant contribution to the large-scale tidal and velocity field (Rieder et al. in preparation), with their dynamical imprint being recognizable as a distinct shear pattern in the velocity flow.

The contrast between NEXUS velocity shear and NEXUS+ described in detail in Cautun et al. (2013, 2014), is illustrated in Fig. 2, which compares the two filamentary networks in a slice of $20 h^{-1}$ Mpc thickness and of $300 \times 300 (h^{-1}$ Mpc$)^2$ in area. While the prominent and massive filaments are identified by both methods, NEXUS+ manages to identify many more thin filamentary structures that illustrate the multiscale character of the cosmic filamentary network.

A second major difference between the two web finders is due to the non-linear velocity shear field having a larger scale coherence (i.e. being more non-localized) than the density field. This is due to the difference in the non-linear power spectra between velocity shear and density, with the former decreasing faster on small scales (Bertschinger & Jain 1994; Jain & Bertschinger 1994; Bond 1996).
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Figure 2. Left-hand panels: Filaments detected by the NEXUS+ method, which identifies filaments in the density field. Right-hand panels: For the same volume as in the left-hand panels, filaments detected by the NEXUS_velshear method, which identifies filaments in the velocity shear field. The top row shows a $20\, h^{-1}\, \text{Mpc}$ slice of $300 \times 300 \, (h^{-1}\, \text{Mpc})^2$ size across. The bottom row shows a zoom-in into a smaller region of this slice. NEXUS_velshear identifies typically only the thick filaments, whereas NEXUS+ identifies even the thin and tenuous tendril-like filaments in low-density regions.

Myers 1996; van de Weygaert 2002; Romano-Díaz & van de Weygaert 2007). Gravity, and hence tidal fields, are integrals over the density field. Hence they also manifest themselves at a distance from the source (the density fluctuations) that generated them. Shear, as with the velocity field itself, is similar: it results from the action of gravity (the tidal field) over time. Hence, while you are outside the generating source, you still see the imprint of the tidal field on the velocity field.²

For tides, and shear, this means you can have the signature for a filament or a node while far removed from the object, even way into the voids, which is indeed what you see. We need not be amazed that it is also seen in the NEXUS_velshear filament results: they are thicker than the corresponding filaments identified from the density field. Because of this, the NEXUS_velshear filaments are typically thicker than their NEXUS+ counterparts, and thus the NEXUS_velshear filaments tend to include matter and haloes in the immediate vicinity that would visually be more likely to be identified as part of the wall or void regions surrounding the NEXUS+ filaments.

²It is precisely this fact which is central to using the gravitational lensing shear field as a tracer of the source. And thus we need not be amazed it is also seen in the NEXUS_velshear filament results: they are thicker than the equivalent density identified filaments.

An even more detailed and insightful illustration of the differences between the NEXUS+ and NEXUS_velshear filamentary networks is provided by studying the halo distribution. Figs 3 and 4 depict the spatial distribution of haloes assigned to filaments by the two methods. The overall impression is one of NEXUS+ identifying a sharper outline of the cosmic web, while it includes a wide spectrum of small-scale filamentary features that are not seen in the NEXUS_velshear web-like network. While NEXUS_velshear identifies the massive filamentary arteries, it does not recover the small-scale tendrils branching out from these dominant structures or the complex network of tenuous filaments in low-density regions. The large dynamic range of the NEXUS+ procedure, however, does recognize and identify these small filaments. On the other hand, the prominent NEXUS_velshear filaments have a considerable number of haloes assigned to them that lie in the dynamical influence region of the filaments but that may in fact be located in low density boundary regions. As a result, the NEXUS_velshear filaments are more massive and broader than their NEXUS+ equivalents.

3 HALO POPULATION

The halo catalogue has been constructed by first identifying Friends-of-Friends (FOF) groups using a linking length of 0.2 times the mean dark matter particle separation. The FOF groups were further split into bound structures using the SUBFIND algorithm (Springel
et al. 2001), which first associates potential subhaloes to local dark matter density peaks and then progressively discards particles that are not gravitationally bound to these substructures. For each FOF group, SUBFIND identifies the most massive subhalo as the main halo of the group. Our study uses only these main haloes. We define the halo radius, $R_{200}$, as the radius of a sphere located at the halo centre that encloses a mean density 200 times the critical density of the universe. Then, the halo mass, $M_{200}$, is the mass contained within $R_{200}$.

We limit our analysis to haloes more massive than $3.2 \times 10^{10} \, h^{-1} M_{\odot}$, which is motivated by the condition that the structure of a halo is resolved with a sufficiently large number of particles. Following Bett et al. (2007), we select haloes resolved with at least 300 dark matter particles within $R_{200}$. The P-Millennium contains $3.76 \times 10^6$ such main haloes which represent a very large and statistically representative sample. This enables us to characterize the alignment between halo properties and the cosmic web directions to an unprecedented extent.

Figure 3. The distribution of haloes in a $20 \, h^{-1} \text{Mpc}$ slice of the P-Millennium simulation. Each dot represents a halo more massive than $3.2 \times 10^{10} \, h^{-1} M_{\odot}$. It shows: all the haloes (top-left panel), the haloes residing in NEXUS+ filaments (bottom-left) and the haloes residing in NEXUS_velshear filaments (bottom-right). The haloes classified as residing in filaments by both methods are shown in the top-right panel.
Figure 4. Comparison of haloes assigned to filaments by NEXUS+ and NEXUS_velshear. It shows a subregion of the volume shown in Fig. 3 selected to enclose a massive filament. The thickness of the slice is $10 \, h^{-1} \text{Mpc}$. The four panels show: all NEXUS+ filament haloes (top-left), all NEXUS_velshear filament haloes (top-right), haloes assigned to filaments only by nexus+ (bottom-left), and haloes assigned to filaments only by NEXUS_velshear (bottom-right). The red lines in the top two panels depict the orientation of the NEXUS+ and NEXUS_velshear filaments. The filament orientation is shown at the position of a random sample of 20 per cent of the haloes in the slice. The contrast between both methods is substantial: NEXUS+ traces small filaments and tendrils whose minor dynamical impact eludes detection by NEXUS_velshear. Furthermore, the prominent filaments detected by NEXUS_velshear are substantially thicker than their NEXUS+ counterparts.

For all the haloes above our mass threshold limit, we calculate physical properties such as angular momentum and shape. Unless specified otherwise, these properties are calculated using all the gravitationally bound dark matter particles inside the halo radius, $R_{200}$. In order to gain deeper insight, we also calculate properties for the inner region of all haloes. We use two different radial cuts corresponding to the radii that enclose 10 and 50 per cent, respectively, of the halo particles. We refer to these radial cuts as the inner...
10 per cent and 50 per cent of the halo, while when describing the full halo properties we denote that as the entire halo. The inner radial cuts are motivated by the observation that recent mass accretion is mainly deposited on the outer regions of a halo (Wang et al. 2011), and thus, by studying the inner halo, we can probe how recent mass accretion, which is often anisotropic (e.g. Vera-Ciro et al. 2011; Shao et al. 2018), may be affecting halo shape and spin.

### 3.1 Cosmic web environment

We split the halo population into node, filament, wall, and void samples according to the web environment identified at the location of the halo. We do so for both the NEXUS_velshear and NEXUS+ web classification schemes. In general, many of the same haloes are assigned to nodes and filaments by both methods, but there are also differences (see Table 1), which we discuss in more details shortly.

In the present study, we focus on main haloes residing in filaments. The statistics of filament haloes in P-Millennium are presented in Table 1. The filaments contain roughly 35 per cent of the main haloes, with NEXUS+ identifying a slightly larger fraction of filament haloes. Both methods assign roughly the same haloes to filaments, with 96 per cent of the NEXUS_velshear filament haloes also residing in NEXUS+ filaments. For NEXUS+, 84 per cent of its filament haloes are in common with the NEXUS_velshear ones, while the remaining 16 per cent corresponds to haloes that populate filamentary tendrils in underdense regions.

In Fig. 3 we illustrate the similarities and differences in the distribution of filament haloes identified by the two web finders. For this, we show the full halo distribution (top-left panel) as well as the haloes inside NEXUS_velshear and NEXUS+ filaments inside a $200 \times 200 h^{-1}$ Mpc region, of $20 h^{-1}$ Mpc in width. Visually, we find that both methods are successful in recovering the most prominent filaments and also some of the less conspicuous ones, although it is more difficult to visually assess the latter due to the larger slice thickness. The haloes in NEXUS+ filaments (bottom-left-hand panel) trace a sharp and intricate network with prominent filamentary arteries, as well as a substantial web of thinner tenuous branches and minor filaments in low-density areas. In contrast, the NEXUS_velshear filament haloes (bottom-right-hand panel) have a rather different character, tracing mostly thick filaments.

The comparison between NEXUS+ and NEXUS_velshear filaments reveal that the latter are considerably thicker. This is a reflection of the non-local character of the velocity shear field, which, compared to NEXUS+, leads to assigning to the same filament haloes that are found at larger distances from the filament spine. The extent of this effect can be best appreciated in the top-right panel, which shows the distribution of common haloes, that is the ones assigned to filaments by both NEXUS+ and NEXUS_velshear. The common filament haloes have almost the same appearance, although thinner and sharper, as the ones residing in the NEXUS_velshear filaments. This clearly illustrates that NEXUS+ finds the NEXUS_velshear filaments and that it assigns them a smaller thickness.

To have a more detailed comparison between the filament haloes identified by the two web finders, Fig. 4 zooms in on a $40 h^{-1}$ Mpc region centred on a prominent filamentary network. The figure shows the distribution of filament haloes in and around a junction of many prominent filaments which are found around a concentration of cluster-mass haloes. This region is certainly one of the most dynamically active areas of the cosmic web and is expected to be strongly influenced by the substantial tidal forces resulting from the highly anisotropic distribution of matter in the region.

The contrast between the two web finders is substantial. NEXUS+ includes small filaments and tendrils whose minor dynamical impact on the velocity shear field eludes detection by the NEXUS_velshear method. The top row of Fig. 4 provides a telling visualization of this effect, with + pointing out many thin low-density filaments around the main filamentary mass concentrations. This can also be observed in the bottom row of Fig. 4, which shows the exclusive filament haloes, that is the haloes assigned to filaments by only one of the two methods. NEXUS_velshear misses the halo population of minor filaments while identifying thicker prominent filaments, which may even include haloes that NEXUS+ assigns to underdense void regions.

The directions of NEXUS+ and NEXUS_velshear filaments are illustrated in the top two panels of Fig. 4. This shows that the orientations assigned by the two web finders match well with the visually inferred local direction of the filamentary network. The NEXUS+ and NEXUS_velshear filament orientations are nearly parallel as can be seen from Fig. 5. The figure shows the misalignment angle between NEXUS+ and NEXUS_velshear filament axes, which was calculated at the position of each halo that is assigned to both filament types. The NEXUS+ and NEXUS_velshear filaments are well aligned over the entire halo mass range, with a median misalignment of $\sim 20^\circ$.

### Table 1. The population of P-Millennium haloes more massive than $3.2 \times 10^{10} \ M_\odot$ assigned to filaments by the NEXUS+ and NEXUS_velshear web identification methods. The columns specify: (1) method name, (2) the number of haloes assigned to filaments, (3) the fraction of the total halo population, (4) the number of common haloes assigned to filaments by both methods, and (5) the number of exclusive haloes assigned to filaments by only one method.

<table>
<thead>
<tr>
<th>Method</th>
<th>Number ($\times 10^6$)</th>
<th>Fraction (%)</th>
<th>Common ($\times 10^6$)</th>
<th>Exclusive ($\times 10^6$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>NEXUS+</td>
<td>2.80</td>
<td>36.7</td>
<td>2.36</td>
<td>0.43</td>
</tr>
<tr>
<td>NEXUS_velshear</td>
<td>2.47</td>
<td>32.6</td>
<td>1.66</td>
<td>0.10</td>
</tr>
</tbody>
</table>
The alignment shows a small dependence on halo mass, with higher mass haloes having slightly lower alignment between the two filament types.

### 3.2 Halo mass function

A first aspect of the connection between web-like environment and the halo distribution concerns how haloes populate the different cosmic web environments. This is shown in Fig. 6, where we present the (cumulative) mass function of haloes segregated according to the environment in which they reside. Here we show the population of main haloes with at least 100 particles, i.e. $M_{200} > 1.1 \times 10^{10} \, h^{-1} M_{\odot}$, however, for the rest of the paper, we limit the analysis to objects at least three times as massive. The halo mass function represents the number density, $n(> M)$, of haloes with a mass in excess of $M$,

$$n(> M) = \int_{M}^{\infty} \frac{dn}{d \log M} \frac{dM}{M},$$

where $dn/d \log M$ denotes the specific mass function, that is the number density of haloes of mass $M$ per logarithmic mass bin. Fig. 6 shows the halo mass function split according to web environments for both the NEXUS+ (top panel) and the NEXUS_velshear (middle panel) methods. We note that the identifications of node environments using the velocity shear field poses challenges (Cautun et al. 2013), which are due to the presence of a substantial level of vorticity in these highly multistream regions that is not accounted by the velocity shear field. To deal with this limitation, following Cautun et al. (2013), we augmented the NEXUS_velshear scheme such that the node identification is done using the density field, which is the procedure used by NEXUS+.

Fig. 6 shows that the halo mass function depicts a substantial difference between environments (also see e.g. Cautun et al. 2014; Libeskind et al. 2018): the most massive haloes reside at nodes of the web while lower mass objects are predominantly found in filaments. While there are some differences in details, in particular concerning the higher mass tails of the void and wall halo mass functions, overall the halo populations segregated by environment are very similar in both the NEXUS+ and NEXUS_velshear web finders.

Except for the most massive objects, we find that the majority of haloes are found in filaments. The exception concerns the objects with masses in excess of $M \approx 10^{13.5} M_{\odot}$, which are almost exclusively found in nodes. The mass function for void haloes is strongly shifted to lower masses, and has a significantly lower amplitude than that for filament or wall haloes. This is to be expected, since voids represent the lowest density regions and are mostly populated by low-mass haloes. This agrees with observations which reveal that most void galaxies are typically faint and have low stellar masses (see e.g. Kreckel 2011; Kreckel et al. 2012). A similar trend is seen for haloes residing in the membranes of the cosmic web, i.e. walls, though less extreme than for void galaxies. Haloes more massive than $10^{12.0} M_{\odot}$ are hardly found in walls, nearly all of them residing in filaments. It explains, amongst others, why walls are so hard to trace in magnitude-limited galaxy surveys (see also Cautun et al. 2014). Overall, the halo mass functions in NEXUS+ environments are the same as in their NEXUS_velshear equivalents, with only minor differences. In the second panel of Fig. 6, we can notice that the NEXUS_velshear allocates somewhat more haloes of all masses to voids and walls, and thus slightly fewer haloes to filaments. The bottom panel of Fig. 6 compares in detail the filament mass function identified by the two web finders. The common sample represents the majority of the filament halo population. This is the case in particular for NEXUS_velshear, for which the exclusive sample is nearly a factor of ten less numerous at all masses. The NEXUS+ exclusive sample is more sizeable, consisting of ~30 per cent of the low-mass haloes found in NEXUS+ filaments. This is a direct reflection of the fact that NEXUS+ identifies the small and tenuous filamentary tendrils, which are largely ignored by NEXUS_velshear. These less prominent features contain mostly low-mass haloes (Cautun et al. 2014), which explain why the differences between NEXUS+ and NEXUS_velshear are mostly seen for low-mass haloes.
3.3 Halo shape

We determine the shape of a halo by calculating its moment of inertia tensor, $I_{ij}$ (van Haarlem & van de Weygaert 1993; Bett et al. 2007; Araya-Melo 2008). For a halo that contains $N$ particles, the moment of inertia with respect to the centre of mass is defined as

$$I_{ij} = \sum_{k=1}^{N} m_k r_{k,i} r_{k,j},$$

where $m_k$ is the mass of the $k$-th particle, and $r_{k,i}$ is the particle position along the $i$-th coordinate axis with respect to the halo centre of mass.

The inertia tensor is a $3 \times 3$ symmetric matrix that can be diagonalized to calculate its eigenvalues, $s_a \geq s_b \geq s_c$, and eigenvectors, $v_a$, $v_b$, and $v_c$. The shape of the halo is commonly described in terms of the axes ratios $b/a$ and $c/a$, where $a = \sqrt{s_a}$, $b = \sqrt{s_b}$, and $c = \sqrt{s_c}$ denote the major, intermediate, and minor halo axes, respectively. A perfectly spherical halo has $b/a = c/a = 1$, a prolate one has a major axis significantly longer than the intermediate and minor axis, $c \approx b \ll a$, while an oblate one has a much smaller minor axis than the other two, $c \ll b \approx a$. The orientation of the halo is specified by the corresponding eigenvector, with $v_a$, $v_b$, and $v_c$ pointing along the major, intermediate, and minor axes, respectively.

The top panel of Fig. 7 shows the halo shape distribution in P-Millennium, which is in good agreement with previous studies (e.g. Bett et al. 2007). Overall, the haloes are triaxial, with a clear trend towards a roundish – but never perfectly spherical – shape. Most haloes have $c/a > 0.8$ and $b/a > 0.9$. They also have a slight tendency towards a prolate shape. The halo shapes show a small, but statistically significant, variation with the web environment in which a halo resides. This is clearly indicated in the middle and bottom panels of Fig. 7, which shows the median halo shape axis ratios, $b/a$ and $c/a$, as a function of halo mass and environment. Haloes in nodes and voids are more flattened than haloes residing in filaments and walls (Hahn et al. 2007; Forero-Romero et al. 2014).

3.4 Halo angular momentum

The angular momentum – or spin – of the halo is defined as the sum over the angular momentum of the individual particles that constitute the halo,

$$J = \sum_{k=1}^{N} m_k (r_k \times v_k),$$

where $r_k$ and $v_k$ are the position and velocity of the $k$-th particle with respect to the halo centre of mass.

For each halo, we calculate the angular momentum for the entire virialized halo, as well as for inner halo regions consisting of the inner 10 per cent and 50 per cent of the halo particles. This yields three angular momenta, $J_{100}$, $J_{50}$, and $J_{10}$ for each halo. We are interested in two aspects of the halo angular momenta: its amplitude and its orientation (i.e. the spin direction).

3.4.1 Spin parameter $\lambda$

The angular momentum amplitude, $J = |J|$, is usually expressed in terms of a dimensionless spin parameter, $\lambda_p$, introduced by Peebles (1969),

$$\lambda_p = \frac{J |E|^{1/2}}{GM^{5/2}},$$

where $J$, $E$, and $M$ are the total angular momentum, energy, and mass of the halo, and $G$ is Newton’s constant. The spin parameter
\( \lambda \) quantifies the extent of coherent rotation of a halo (or any self-gravitating system). A value of unity of the parameter means that a self-gravitating system is supported by rotation (Padmanabhan 1993), a value closer to zero would imply that it hardly has coherent rotation and that the system is dispersion-supported.

We use an alternative definition of the spin parameter introduced by Bullock et al. (2001). The Bullock spin parameter \( \lambda \) has a more practical definition, in particular when considering a subvolume of a virialized sphere, and it is also easier to calculate. For a region enclosed within a sphere of radius \( R \), this spin parameter is defined as

\[
\lambda = \frac{J}{\sqrt{2MV^2 R}} \tag{11}
\]

where \( V \) is the halo circular velocity at radius \( R \) and \( J \) the angular momentum within this radius. This spin parameter definition reduces to the standard Peebles parameter \( \lambda_P \) when measured at the virial radius of a truncated isothermal halo. The spin parameters \( \lambda_P \) and \( \lambda \) are in fact very similar for typical NFW haloes (Navarro, Frenk & White 1997; Bullock et al. 2001), having a roughly lognormal distribution with a median value of \( \lambda \approx 0.05 \) (Efstathiou & Jones 1979; Barnes & Efstathiou 1987).

In order to determine if halo spin amplitude is correlated to the web environment in which a halo resides, Fig. 8 shows the probability distribution functions (PDF) of the Bullock spin parameter for halo samples split according to the NEXUS+ environment in which a halo is located. We observe a clear segregation between the rotation properties of haloes in different web environments, with filament and wall haloes having on average the largest spin, while node haloes are the slowest rotation objects. For all environments, the PDF is close to a lognormal distribution, but with its peak value slightly shifted, from \( \lambda = 0.035 \) for filaments and walls, to \( \lambda = 0.030 \) for voids and \( \lambda = 0.020 \) for node haloes.

Fig. 8 clearly reveals the influence of cosmic environment on the spin parameters of haloes, with filament and wall haloes showing a significantly stronger coherent rotation than their counterparts residing in nodes, which have a more prominent dispersion-supported character. Interestingly, this is similar with the morphology–density relation (Dressler 1980) found in observations, with early-type galaxies dominating the galaxy population of clusters while the late-type spirals dominating the filamentary and wall-like ‘field’ regions.

### 3.4.2 Spin orientation

When calculating the alignment of halo spin with the web directions, we make use of the spin direction of each halo, which is defined as

\[
e_f = \frac{J}{|J|}.
\]

We apply this relation for each of the three radial cuts for the radial extent, i.e. for the radii including 10 per cent, 50 per cent, and 100 per cent of the mass of the halo.

### 4 SPIN ALIGNMENT ANALYSIS

Here we study the alignment between the halo spins and the orientation of the filaments in which the haloes are embedded. The filament orientation corresponds to the direction along the filament spine, which is given by the \( e_{f1} \) and \( e_{f2} \) eigenvectors for the NEXUS+ and NEXUS+velshear methods, respectively (for details see Section 2.2.2 and Fig. 9). Furthermore, we limit our analysis to filament haloes, which are the dominant population of objects.

#### 4.1 Alignment analysis: definitions

We define the alignment angle as the angle between the direction of a halo property, which can be spin, shape, or velocity, and the orientation of the filament at the position of the halo. A diagrammatic illustration of the alignment angle \( \theta \) is shown in Fig. 9, with the ellipse representing a halo and the cylinder the local stretch of the filament. For a given halo vector property \( h \), the halo–filament alignment angle is

\[
\mu_{hf} \equiv \cos \theta_{h,e_f} = \frac{h \cdot e_f}{|h||e_f|},
\]

which is the normalized scalar product between the halo and filament orientations. We take the absolute value of the scalar product since filaments have an orientation and not a direction, that is both \( e_1 \) and \( -e_1 \) correspond to a valid filament orientation. Note that the symbol, \( \mu_{hf} \), denotes the cosine of the alignment angle, however, for simplicity, we refer to it both as the alignment parameter and as the alignment angle.

A halo property that is parallel to the filament orientation corresponds to \( \mu_{hf} \approx 1 \), while a property that is perpendicular to the filament orientation corresponds to \( \mu_{hf} = 0 \). A random or isotropic
distribution of alignment angles corresponds to a uniform distribution of $\mu_J$ between 0 and 1, which provides a useful reference line for evaluating deviations from isotropy. In the case of a distribution of alignment angles for a halo population, we refer to that sample as being preferentially parallel if the median alignment angle is larger than 0.5. Conversely, that sample is preferentially perpendicular if the median alignment angle is lower than 0.5. Following this, and somewhat arbitrary, we consider that $\mu_J = 0.5$ marks the transition between a preferentially parallel, median $\mu_J > 0.5$, and a preferentially perpendicular, median $\mu_J < 0.5$, alignment.

We use bootstrapping to estimate the uncertainty in the distribution of alignment angles. For each distribution, we generate 1000 bootstrap realizations and compute the distribution and median values for each realization. These are then used to estimate 1 and 2σ uncertainty intervals. We apply this procedure for estimating PDF uncertainties (e.g. see Fig. 10) as well as for calculating the error in the determination of the median value (e.g. see Fig. 11).

4.2 Halo spin alignment: statistical trends

Fig. 10 gives the distribution of the halo spin alignment angle, i.e. of $\mu_J = \cos(\theta_{J_f})$, between the halo spin directions and the filament orientation at the position of the haloes. The panels of the figure correspond to haloes of different masses. The figure shows the alignment only for NEXUS+velshear filaments, but a nearly identical result is found for NEXUS+ filaments. We study the alignment of the entire halo, as well as for inner radial cuts that contain 50 per cent and 10 per cent of the halo mass. In each case, we require at least 300 particles to determine the halo spin, which is why the spin for the 50 per cent and 10 per cent inner radial cuts is shown only for haloes more massive than 1 and $3 \times 10^{11} h^{-1} M_\odot$, respectively.

For haloes in each mass range, we find that the alignment angle has a wide distribution, taking values over the full allowed range from $\cos \theta = 0$ up to $\cos \theta = 1$ (note that the y-axis only goes from 0.8 to 1.2). None the less, the distribution is clearly different from an isotropic one, which is the case even when accounting for uncertainties due to the finite size of the sample, which are shown as the grey shaded region around the isotropic expectation value. The spin directions of low-mass haloes show an excess probability to have $\cos \theta_{J_f} \simeq 1$, which indicates a tendency to be preferentially parallel to the filament spine. In contrast, high-mass haloes show an opposite trend, with an excess of objects with $\cos \theta_{J_f} \simeq 0$, i.e. tendency to be preferentially perpendicular to the filament axis. To summarize, while we find a wide distribution of halo spin–filament orientations, there is a statistically significant excess of haloes that, depending on mass, have their spin preferentially parallel or perpendicular to their host filaments.

The nature of the spin–filament alignment depends on halo mass. Many low-mass haloes, with masses in the range $M_{200} = (5-9) \times 10^{10} h^{-1} M_\odot$ (top left-hand panel of Fig. 10) have alignment angles, $\cos \theta \gtrsim 0.8$, which indicates their tendency to orient parallel to the filament spine. On the other hand, evaluating the alignment in the subsequent panels, which correspond to increasing halo mass, we observe a systematic shift from preferentially parallel to preferentially perpendicular configurations. For example, haloes with masses of $(3-4) \times 10^{11} h^{-1} M_\odot$ show a considerably weaker parallel alignment excess, while for halo masses of $(1-2) \times 10^{12} h^{-1} M_\odot$ and higher, most haloes have an alignment angle $\cos \theta \lesssim 0.3$.

The spin–filament alignment depends not only on halo mass, but also on the radial extent in which the halo spin direction is calculated. This is illustrated in Fig. 10, which shows the spin–filament alignment calculated using the inner most 10 per cent and 50 per cent of the halo mass. While for high halo masses, $M_{200} > 1 \times 10^{12} h^{-1} M_\odot$, the inner and the entire halo spins are aligned to the same degree with their host filament, at lower masses, $M_{200} < 5 \times 10^{11} h^{-1} M_\odot$, the inner halo spin shows no preferential alignment. This is in contrast to the entire halo spin, which is preferentially parallel to the filament spine. The most remarkable contrast between the inner and outer halo spin orientations is found for objects in the mass range $(3-4) \times 10^{11} h^{-1} M_\odot$ (third panel of Fig. 10). While the inner halo spin has a slight tendency for a perpendicular alignment, the entire halo spin is oriented preferentially along the filament spine.

In summary, the halo spin–filament alignment is mass dependent: low-mass haloes have a preferentially parallel alignment, while haloes of Milky Way mass and more massive have a preferentially perpendicular alignment. The latter fits with the TTT which predicts that halo spin directions are perpendicular on the filament in which the haloes reside (Lee & Pen 2000). However, the spin–filament alignment of low-mass haloes is opposite to the predictions of TTT. The picture is further complicated since the alignment of low-mass haloes depends on the radial extent used for calculating their spin, with the alignment changing from preferentially perpendicular in the inner region, which agrees with TTT predictions, to preferentially parallel in the outer region. The inner region consists of mostly early accreted mass while the converse is true for the outer region. This suggests that the initially induced halo spin during the linear evolution phase (Peebles 1969) is substantially modified by subsequent mass accretion stages. Particularly outstanding in this respect is the contrast between low- versus high-mass haloes, with the spin–filament alignment of the latter being less disturbed by recent accretion.

4.3 The spin flip

We now proceed to study in more detail the dependence on halo mass of the halo spin–filament alignment. This is shown in Fig. 11, where we plot the median spin–filament alignment angle, $\langle \mu_J \rangle = \langle \cos \theta_{J_f} \rangle$, calculated using narrow ranges in halo mass. To assess the statistical robustness of the median alignment angle, we show the $2\sigma$ uncertainty in the median value, which is calculated using bootstrap sampling. The uncertainty range is small, especially at low masses, which is due to the large number of haloes in each mass range. For clarity, we only show the uncertainty in the alignment with NEXUS+velshear filaments, but roughly equal uncertainties are present in the alignment with NEXUS+ filaments. The threshold between preferentially parallel and perpendicular alignments corresponds to $\langle \cos \theta_{J_f} \rangle = 0.5$ and is shown with a horizontal solid line in Fig. 11.

Fig. 11 shows a clear and systematic trend between halo mass and the median spin–filament alignment angle: the alignment angle, $\langle \cos \theta_{J_f} \rangle$ increases with decreasing halo mass. This trend is visible for both NEXUS+ and NEXUS+velshear filaments, although the exact median angles vary slightly between the two methods. Especially telling is the transition from preferentially perpendicular alignment at high masses to a preferentially parallel alignment at low masses, which takes place at $M_{200} = 5.6$ and $3.8 \times 10^{11} h^{-1} M_\odot$ for NEXUS+velshear and NEXUS+ filaments, respectively. This transition is known as spin flip and has been the subject of intense study (Aragón-Calvo et al. 2007b; Hahn et al. 2010; Codis et al. 2012; Trowland et al. 2013). The exact value of the spin flip halo mass varies between studies, and, as
we found here, it varies between the two web finders employed here. In the next subsection we investigate this difference in more detail.

Fig. 11 also shows the spin–filament alignment for the inner halo, whose strength and mass dependence is different from that of the entire halo. The difference between the inner and entire halo spin alignment is most pronounced for low-mass haloes, in line with the conclusions of Fig. 10. For example, the spin of the inner 10 per cent of the halo mass shows little mass dependence for high masses, after which it slowly increases from preferentially perpendicular towards preferentially parallel alignment with the filament spin. However, due to the limited resolution of the simulation (we need at least 300 particles in the inner 10 per cent region of the halo), we cannot probe if there is a spin flip and at what halo mass it takes place. However, for the spin–filament alignment of the inner 50 per cent of the halo mass, we just resolve the spin flip, which takes place at masses a factor of $\sim 3$ times lower than the spin flip of the entire halo.

The systematic nature of the spin flip is a clear indication of the significant role played by additional physical processes not captured by TTT in determining the final angular momentum of haloes. The spin–filament alignment of high-mass haloes is, at least qualitatively, in agreement with TTT, so it is unclear what is the effect, if any, of additional processes not included in TTT. In contrast, the alignment of low-mass haloes is contrary to TTT predictions, suggesting that the spin acquired during the linear evolution phase, which is well described by TTT, gets modified by additional phenomena that result in a gradual transition towards spins aligned with the filament spine. The major keys to the dynamics of this process are to be found in the contrast between the spin of the inner and outer halo regions, as well as in the variation of the alignment strength between different regions of the filamentary network, which is the topic of the next subsection.

### 4.4 Spin alignment and the nature of filaments

Here we investigate how the spin–filament alignment varies with the filament properties, focusing on two crucial aspects. First, we study what explain the small, but statistically significant, variation in spin flip mass between the NEXUS+ and NEXUS_velshear filaments (see...
velshear filaments

discussed in Section 3.1, NEXUS+ filaments include many thin filamentary tendrils, either branching off from more prominent filaments or residing in low-density regions. These tenuous structures, which are mostly populated by low-mass haloes, are not identified by NEXUS_velshear. In contrast, the NEXUS_velshear formalism includes a fair number of haloes far from the ridge of prominent filaments (see Cautun et al. 2014); these haloes would typically be assigned by NEXUS+ to neighbouring low-density areas (see Fig. 4).

Fig. 12 studies the impact of halo population on the spin–filament alignment. It shows the halo mass dependence of the spin–filament alignment for common haloes, which are haloes that are assigned to both NEXUS+ and NEXUS_velshear filaments (see Fig. 3 for an illustration of the spatial distribution of these haloes). For masses, \( M_{200} \leq 10^{12} h^{-1} M_\odot \), the common haloes have the same median spin–filament alignment angle for both web finders, to the extent that the curves almost perfectly overlap each other. This translates into an agreement on the spin flip transition mass, at \( M_{200} = 5 \times 10^{11} h^{-1} M_\odot \). This result demonstrates that there are no fundamental differences between the spin–filament alignment of low-mass common haloes, whether the filaments are identified by NEXUS+ or NEXUS_velshear methods.

The story is different for haloes more massive than \( 10^{12} h^{-1} M_\odot \), where the spin–filament alignment of common haloes is the same as that of the full filament population. In particular, while both web finders find that halo spins are preferentially perpendicular on their host filaments, the spin–filament alignment using NEXUS+ orientations is stronger (i.e. more perpendicular) than that using NEXUS_velshear orientations, and this discrepancy increases at higher halo masses. This is a manifestation of the differences in orientations between NEXUS+ and NEXUS_velshear filaments (see Fig. 5), with NEXUS+ being able to recover better the orientation of filaments around massive haloes. These haloes, due to their high mass, affect the mass flow around themselves and thus locally change the large-scale velocity shear field. In turn, this diminishes the ability of the NEXUS_velshear web finder to recover the orientation of the large-scale filaments. More massive haloes change the velocity flow to a larger extent and to larger distances, which explains why the difference between the two filament finders increases at higher halo masses.

Fig. 13 studies the mass-dependence of the spin–filament alignment of exclusive haloes, that is haloes assigned exclusively to NEXUS+ or to NEXUS_velshear filaments. We focus our discussion on haloes with \( M_{200} \leq 2 \times 10^{12} h^{-1} M_\odot \) since the exclusive halo sample contains a small number of higher mass objects, which is a consequence of the fact that most massive haloes are assigned to

**Figure 11.** Median alignment angle, \( \langle \cos \theta_{J,J_3} \rangle \), between the angular momentum and filament orientation as a function of halo mass. It shows the alignment with the filament orientation identified by NEXUS+ (dotted line) and NEXUS velocity shear (solid line). The various colours correspond to different angular momentum definitions using the entire halo and using the innermost 50 per cent and 10 per cent of the particles. The coloured shaded region around each lines gives the 2\( \sigma \) bootstrap uncertainty in determining the median, which we only show for solid lines. The bottom panel (note the different y-axis) shows the 40–60 percentiles of the \( \cos \theta_{J,J_3} \) distribution, which is indicated via the grey-shaded region.

**Figure 12.** Median alignment angle, \( \langle \cos \theta_{J,J_3} \rangle \), between halo spin and filament orientation for common haloes found to reside in both NEXUS+ and NEXUS velocity shear filaments. Note that for \( M_{200} < 10^{12} h^{-1} M_\odot \) the alignment strength of the entire halo (solid and dashed red curves) is independent of the filament identification method implying that the differences seen in Fig. 11 are due to the two web finders assigning somewhat different haloes to filaments.
filaments by both methods. In contrast to common haloes, which reside typically in the central region of prominent filaments, the exclusive halo population is very different between the two web finders.

The NEXUS+ exclusive sample, which consists of haloes in tenuous filamentary tendrils, shows preferentially perpendicular alignment down to very low masses, with the spin flip mass being \( \sim 1 \times 10^{11} h^{-1} \text{M}_\odot \). This transition mass is much lower than the corresponding mass of all the NEXUS+ filament haloes, which is \( \sim 3 \times 10^{11} h^{-1} \text{M}_\odot \). The spin flip mass for haloes in different filament populations is presented in Table 2. Thus, the spin–filament alignment depends on filament properties, with same mass haloes being more likely to have a preferentially perpendicular configuration if they reside in a thinner filament (the next subsection discusses this trend in more detail).

The NEXUS_velshear exclusive sample, which consists of mostly haloes found at the outskirts of prominent filaments, shows a spin flip mass of \( \sim 6 \times 10^{11} h^{-1} \text{M}_\odot \). This spin flip mass is a factor of six times higher than that of NEXUS+ exclusive haloes, and thus substantiates the hypothesis that the spin alignment depends on the nature of filaments. Furthermore, the spin flip of the NEXUS_velshear exclusive sample has the same value as that of the NEXUS_velshear common sample (see Fig. 12). Both samples reside in the same filaments, but the former is typically found in the outskirts, that is farther from the filament spine. Thus, comparing the two suggests that the spin flip mass does not vary strongly with the distance from the filament spine.

### 4.4.2 Alignment and filament thickness

We now carry out a detailed investigation of the hypothesis proposed in the previous subsection that the spin–filament alignment depends on the nature of filaments. In particular, we study if the alignment of same mass haloes depends on the thickness of the filament in which the haloes are embedded. This is shown in Fig. 14, where we present the mass-dependence of the spin–filament alignment for halo subsamples split according to the diameter of their host filament. The filament diameter was determined following the Cautun et al. (2014) prescription. In a first step, we compress the filaments to their central spine. This involves an iterative procedure where for each iteration step all filament voxels are shifted closer to the filament centre until resulting into a very thin curve, which is the filament spine. In a second step, for each voxel along the filament spine we find the number of neighbouring voxels within a radius of \( R = 2 h^{-1} \text{Mpc} \). Then, the filament diameter, \( D_f \), at that point is given by the diameter of a cylinder of length, \( 2R \), that has the same volume as the total volume of the neighbouring voxels. The filament diameter associated to each halo is the one corresponding to the voxel in which the halo is located. For simplicity, we focus the analysis on the alignment of the entire halo spin.

Fig. 14 shows an immediately obvious trend: over nearly the entire mass range, the spin–filament alignment angle, \( \langle \cos \theta_{J_f} \rangle \), is systematically lower for haloes in thin filaments than for those in thick filaments. Thus, same mass haloes tend to have their spin more perpendicular to the filament spine if they reside in a thinner filament. In particular, it is striking the systematic variation in the spin alignment with filament thickness.

### Table 2. The values of the spin flip mass which determines the transition of the halo spin–filament alignment from preferentially parallel at low halo masses to preferentially perpendicular at high halo masses. We specify the spin flip masses for the two filament population studied here as well as for various halo subsamples. We also give the spin flip mass for NEXUS+ filaments of different thickness.

<table>
<thead>
<tr>
<th>Web finder</th>
<th>Halo subsample</th>
<th>Spin flip mass ( (\times 10^{11} \text{M}_\odot) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>NEXUS+</td>
<td>All</td>
<td>3.3</td>
</tr>
<tr>
<td></td>
<td>Common</td>
<td>5.4</td>
</tr>
<tr>
<td></td>
<td>Exclusive</td>
<td>1.4</td>
</tr>
<tr>
<td>NEXUS_velshear</td>
<td>All</td>
<td>5.4</td>
</tr>
<tr>
<td></td>
<td>Common</td>
<td>5.4</td>
</tr>
<tr>
<td></td>
<td>Exclusive</td>
<td>5.6</td>
</tr>
<tr>
<td>NEXUS+ filament thickness</td>
<td>(0–2)</td>
<td>1.8</td>
</tr>
<tr>
<td></td>
<td>(2–4)</td>
<td>5.2</td>
</tr>
<tr>
<td></td>
<td>(&gt; 4)</td>
<td>18</td>
</tr>
</tbody>
</table>

Figure 13. Median alignment angle, \( \langle \cos \theta_{J_f} \rangle \), between halo spin and filament orientation for exclusive haloes, that is haloes that reside only in NEXUS+ (dashed line) or only in NEXUS_velshear (solid line) filaments. For clarity, we only show the alignment of the entire halo spin. For NEXUS_velshear, the exclusive haloes have roughly the same spin flip mass as the total population of filament haloes. In contrast, for NEXUS+, the exclusive haloes have a \( \sim 4 \) times smaller spin flip mass than the total population of filament haloes.

Figure 14. Median alignment angle, \( \langle \cos \theta_{J_f} \rangle \), between halo spin and filament orientation when splitting the sample according to the filament diameter. The three curves show the alignment signal for haloes in filaments with diameters: (0–2) \( h^{-1} \text{Mpc} \) (solid line with circles), (2–4) \( h^{-1} \text{Mpc} \) (solid line with triangle symbols) and more than \( 4 h^{-1} \text{Mpc} \) (solid line with crosses). The transition halo mass from preferentially parallel to preferential perpendicular alignment increases with increasing filament diameter.
Figure 15. The dependence of the spin flip mass, \( M_{\text{spin-flip}} \), on the filament diameter, \( D_f \), in which the haloes reside. The two symbols correspond to NEXUS+ (circles) and NEXUS_velshear (triangles) filaments. The grey-shaded region shows the 2σ error in the determination of \( M_{\text{spin-flip}} \) for NEXUS_velshear filaments. The spin flip mass dependence on \( D_f \) is well fitted by equation (14), with the solid line showing the best fit.

flip transition mass, which varies by an order of magnitude between different filaments: from \( 1.8 \times 10^{10} h^{-1} M_\odot \) for the thinnest filaments to \( 1.8 \times 10^{12} h^{-1} M_\odot \) for the thickest filaments (see Table 2). This is clearly shown in Fig. 15 where we show the dependence of the spin flip mass, \( M_{\text{spin-flip}} \), on filament diameter. We find that both NEXUS+ and NEXUS_velshear filaments of the same thickness have approximatively the same spin flip mass. This mass increases systematically with filament diameter, \( D_f \), and is well described by the linear functional form

\[
\log_{10} M_{\text{spin-flip}}/(h^{-1} M_\odot) = m D_f + c, \tag{14}
\]

with the best-fitting parameters having the values \( m = 0.32 h \text{ Mpc}^{-1} \) and \( c = 10.8 \).

Thicker filaments are more massive since they typically contain a higher mass per unit length (Cautun et al. 2014), and we expect that they form in regions with a strong tidal field. Thus, we would expect that thicker filaments would host halo spins that are more perpendicular on their filament spine than in the case of thinner filaments. This is opposite to the results of Fig. 14 and suggests that additional processes, like mergers and secondary or late mass accretion, have a substantial impact on the orientation of halo spins.

5 HALO SHAPE ALIGNMENT

The alignment of the halo shape with the large-scale mass distribution represents a complementary aspect to the spin–filament alignment. Here, we focus on two aspects related to the orientation of haloes:

(i) the halo shape–filament alignment, and
(ii) the halo shape–halo spin alignment.

The shape and orientation of a halo is specified in terms of its three principal axes \( a, b, \) and \( c \), and the corresponding eigenvectors (see Section 3.3). Of particular interest are the longest and the shortest axes. The longest axis, \( a \), is the one that specifies the orientation along which the main body of the halo is pointing. The shortest axis, \( c \), is preferentially oriented in the same direction as the halo spin and their mutual misalignment reflects the history of the angular momentum acquisition by the halo. It is also of interest to see in how far the shortest halo axis emulates the halo spin–filament alignment.

5.1 Halo shape–filament alignment

Already in the initial Gaussian field there is a strong correlation between the shape of peaks and the surrounding cosmic matter distribution (van de Weygaert & Bertschinger 1996; de Rossi et al. 2009). For example, an emerging filament is defined by a primordial configuration of the tidal or velocity shear fields with one expanding and two contracting directions, with the former corresponding to the filament axis (see van de Weygaert & Bertschinger 1996; de Rossi et al. 2009). As pointed out by Bond et al. (1996), this identification is the principal reason why prominent filaments form between and connect pairs of massive clusters (see van de Weygaert & Bond 2008, for an extensive theoretical description).

Following the non-linear collapse and build-up of haloes, we wish to see in how far the alignment between the shape of haloes and the filaments in which they reside still reflects the primordial alignment. To this end, we evaluate the angle between the principal axes of haloes, \( v_a, v_b, \) and \( v_c \) (see Section 3.3), and the filament orientation, \( e_f \), which specifies the direction along the ridge of the filament (see Section 2.2.2). Similar to the spin–filament alignment, we characterize the shape–filament alignment in terms of the cosine of the angle between halo shape principal axes and the filament orientation (see equation 13).

Fig. 16 reveals the tendency of the halo shape to be aligned with the filament ridge. The top panel of the figure shows the distribution of alignment angles, \( \cos \theta_{s,a} \), between the halo major axis and the filament orientation. For all halo mass bins, the alignment angle distribution is broad, reflecting the wide range of halo–filament orientations. At the same time, the plot shows an excess of objects with \( \cos \theta_{s,a} \approx 1 \), which reveals the tendency of the major axis of haloes to be aligned preferentially parallel to their host filaments (Hahn et al. 2007; Shao et al. 2016). The alignment is mass dependent, being most pronounced for high-mass haloes. We further investigate the mass dependence in the middle panel of Fig. 16, where we show the median alignment angle, \( \langle \cos \theta_{s,a} \rangle \), as a function of halo mass. It shows how high-mass haloes are strongly aligned with their host filaments, while the lowest mass ones show a much weaker, almost random, alignment with their host filament. The major axis–filament alignment is the largest for the entire halo, and becomes weaker when considering inner halo radial cuts. This is expected, since the outer region of the halo consists of mostly recently accreted mass, which fall in preferentially along the filaments in which a halo is embedded (Aubert, Pichon & Colombi 2004; Libeskind et al. 2005; Rieder et al. 2013). Late time accretion is most anisotropic in higher mass haloes, which explain the mass dependence of the major axis–filament alignment (Kang & Wang 2015; Wang & Kang 2018). Fig. 16 also shows that the haloes are aligned to almost identical degrees to both NEXUS_velshear and NEXUS+ filaments, with the shape–filament alignment being slightly stronger in the latter case, especially at high halo masses.

The bottom panel of Fig. 16 illustrates the alignment between the halo minor axis and the filament ridge. Unsurprisingly, the minor axis of haloes is preferentially perpendicular on their host filament, with the alignment being the strongest for the highest mass objects.

The plots of Fig. 16 show that the level of alignment of halo shapes with the tidal field has increased considerably with respect to that present in the primordial Gaussian field. This is due to non-linear
evolution, which has led to substantial changes in the orientation of haloes (see van Haarlem & van de Weygaert 1993). There is also a rather strong and systematic increase in alignment as a function of halo mass: more massive haloes are more strongly oriented along the filaments in which they reside. This may be partially a reflection of primordial conditions, in which the tidal shear at a given location is more strongly correlated with the orientation of more substantial peaks (Bardeen et al. 1986; van de Weygaert & Bertschinger 1996). More important, however, may be the subsequent anisotropic nature of the accretion of mass and substructure (van Haarlem & van de Weygaert 1993; Shao et al. 2018), which, since it takes place mostly along filaments, amplifies the halo shape–filament alignment.

5.2 Halo shape–halo spin alignment

Several physical effects contribute to a preference of haloes to rotate along an axis that is close to their minor axis. First, the strong correlation between inertia tensor of a peak and the tidal field implies a spin direction that is closely aligned to the peak’s minor axis (see Lee & Pen 2000). Secondly, the peak collapses fastest along its shortest axis (Icke 1973), and, moreover, a rotating self-gravitating isolated object is expected to contract to a larger extent along its rotation axis.

Fig. 17 shows that there is indeed a preference for the minor axis of a halo to be oriented along the spin axis. None the less, this tendency is rather weak (Bailin & Steinmetz 2005; Bett et al. 2007). The distribution of alignment angles between rotation axis and the minor axis is very broad and, although it shows some dependence on halo mass, this variation is neither substantial nor systematic. Furthermore, the strength of the spin–minor axis alignment depends weakly on the radial extent of the halo: the inner 50 per cent of the halo is characterized by a stronger alignment than the inner 10 per cent, while, in the outer regions, the trend reverses, with the entire halo having a lower spin–minor axis alignment (see Bailin & Steinmetz 2005).

6 FILAMENTARY ACCRETION FLOWS AND SPIN FLIPS

Numerical simulations reveal a complex mass dependence of the halo spin-filament alignment, with the spin of high-mass haloes close to perpendicular to their host filament, while the spin of low-mass haloes showing the opposite result, being preferentially parallel to their host filament. The transition halo mass between the two configurations, i.e. preferentially perpendicular at high masses to preferentially parallel at low masses, is known as the spin flip mass. We found that the spin flip mass depends strongly on the nature of filaments, showing more than an order of magnitude variation between the thinnest and thickest filaments (see Section 4.4.2). In other words, same mass haloes are more likely to have perpendicular spin orientations with respect to their host filament if they are embedded in thinner filaments. The conventional TTT (however see the latest predictions of Codis et al. 2015) does not explain this trend, and previous works have argued that the key element for understanding the spin flip phenomenon is the anisotropic accretion of mass and substructures along filaments (see also Libeskind et al. 2013; Welker et al. 2014; Wang & Kang 2017, 2018). Our analysis agrees with this interpretation and, as we discuss shortly, provides additional evidence to support it.

To obtain a detailed picture of the level of mass flow anisotropy in and around filaments, we use haloes as flow tracers and investigate
The slight differences between NEXUS+ and NEXUS seen in flow properties between high-mass and low-mass haloes. dispersion in the filament cross-sectional plane. Also, no bias is substantial level of mass accretion on to the filament and the velocity of the flow, the perpendicular components are a combination of the velocity component along the filament represents the major share parallel along the filament (Forero-Romero et al. 2014). While the orientation of halo velocities with respect to the filaments in which they reside. To this end, we calculate the alignment angles between the halo bulk velocity and the three orthogonal directions that determine the principal axes of filaments: \( e_3 \), which is the orientation of the filament ridge, and \( e_1 \) and \( e_2 \), which give the principal directions perpendicular to the filament.

Fig. 18 shows the median of the alignment angle between halo velocity and the three principal axes of filaments, as a function of halo mass. Overall, we find that the haloes flow preferentially parallel along the filament (Forero-Romero et al. 2014). While the velocity component along the filament represents the major share of the flow, the perpendicular components are a combination of the substantial level of mass accretion on to the filament and the velocity dispersion in the filament cross-sectional plane. Also, no bias is seen in flow properties between high-mass and low-mass haloes. The slight differences between NEXUS+ and NEXUS_\_velshear results may be ascribed to the fact that the NEXUS+ filament population also includes dynamically weaker tendrils, with the haloes inside the tenuous filaments being slightly less likely to flow parallel to the filaments.

Secondary accretion (Bertschinger 1985) represents the key for understanding how the anisotropic filamentary shear inflow is responsible for the observed spin flip of low-mass galaxies (see e.g. van Haarlem & van de Weygaert 1993). Fig. 19 provides an impression of the typical flow patterns along and perpendicular to a filament. It shows the flow-lines in two perpendicular planes centred on a galaxy-sized halo in the COSMOMGRID simulation (Ishiyama et al. 2013). Compared to Fig. 18, which describe the flows of individual tracers, the flow lines characterize the mean flow at each point. The flow in and around the filaments is a combination of shear and divergent flow, which are themselves due to a combination of the outflow from neighbouring voids and the flow along the filament. In general, haloes accreted mass both along the filaments (e.g. see the top panel in Fig. 19) and also perpendicular to their host filament. The former tends to preferentially increase the halo spin component that is perpendicular on the filament, while the latter increase the spin component parallel to the filament. Which of the two dominates depends on the balance between accretion along and perpendicular to the host filament. As we will discuss shortly, this balance depends on a combination of the mass and the local neighbourhood of a halo.

The acquisition of halo angular momentum through secondary accretion results from the transfer of orbital angular momentum, which yields a non-zero residual spin for the halo. It is due to anisotropies in the distribution of accreted mass, such as spatial inhomogeneities (e.g. filamentary infall) as well as mergers with matter clumps. The majority of large and rapid changes in halo spin are caused by mass changes, minor mergers and flyby encounters, and not by major mergers (Bett & Frenk 2012, 2016; Contreras, Padilla & Lagos 2017).

Borzymkowski et al. (2017, see also Romano-Díaz et al. 2017; Garaldi et al. 2018) describes how haloes can be divided in two groups: haloes that are still accreting and those that have stopped most of their mass accretion, so called stalled haloes. The large-scale mass distribution and velocity flow patterns around these two halo types are illustrated in Fig. 20. Accreting haloes typically consists of haloes that are the main perturber in their neighbourhood, they sit at the intersection of several filaments and accrete preferentially along these filaments. Thus, accreting haloes are expected to have their spin preferentially perpendicular on their host filament. The latter
group of stalled haloes are found in regions of strong external tidal field, for example they are embedded in filaments much thicker than the halo size, and mostly accrete from directions perpendicular on their host filament orientation (see fig. 10 of Borzyszkowski et al. for a visualization of the striking contrast between accreting and stalled haloes). Thus, the stalled haloes have spins mostly parallel to their host filament. The fraction of accreting versus stalled haloes is mass dependent, with the fraction of accreting haloes increasing rapidly with halo mass.

The dichotomy in terms of spin–filament alignment between accreting and stalled haloes provides a natural explanation for the trends we found in this work. While accreting haloes dominate the population of high-mass haloes, the converse is true for low-mass haloes. This suggests that the spin–filament alignment should vary...
smoothly from being preferentially perpendicular at high masses to preferentially parallel at low masses, which is exactly the trend we measure in Fig. 11.

The fraction of accreting haloes varies with redshift and, at fixed halo mass, it was larger at higher redshift. It suggest that the spin flip mass should decrease with redshift, which is in very good agreement with previous studies (Codis et al. 2012; Wang & Kang 2018). Furthermore, most of the recently accreted mass settles in the outer regions of the halo (Wang et al. 2011), with the inner regions mostly maintaining the spin of the halo when they were assembled. Thus, the spin of the inner halo regions should be perpendicular to the host filament to a larger degree than the outer halo, which is what we observe in Figs 10 and 11.

The fraction of accreting haloes depends on environment and at fixed halo mass is smaller in regions with strong external tidal fields, such as inside and around massive filaments (the tidal field is what leads to the formation of these filaments). Thus, same mass haloes should have a higher degree of parallel spin–filament configurations if the haloes are embedded in thicker filaments, which is what we find in Fig. 14. This trend also leads to the spin flip mass varying with filament thickness, with the transition mass being higher in thicker filaments.

7 CONCLUSIONS AND DISCUSSION

In this study we have carried out a systematic investigation of the orientation of the spin, shape, and peculiar velocity of haloes relative to the filaments in which they are embedded. Our goal has been to elucidate one of the most outstanding manifestations of environmental influences on halo and galaxy formation, by specifically focussing on the connection between the generation of angular momentum on galactic scales (Lee & Pen 2000; Porciani et al. 2002a; Aragón-Calvo et al. 2007b; Schäfer 2009; Jones et al. 2010) and the dynamics of the large-scale cosmic web (Bond et al. 1996; van de Weygaert & Bond 2008; Cautun et al. 2014). Previous works, starting with Aragón-Calvo et al. (2007b) and Hahn et al. (2007), have shown how cosmological simulations show a complex halo spin–filament alignment, with the mean orientation of halo spin changing from largely perpendicular for high-mass haloes to preferentially parallel for low-mass haloes, with the transition mass, typically $\sim 10^{12}\, h^{-1}\, M_\odot$, known as the spin flip mass.

To study halo–filament alignments, we have used one of the largest cosmological $N$-body simulations available, P-Millennium. It has an impressive dynamic range, combining a large volume with a very high-mass resolution, which makes it ideally suited for investigating the connection between halo formation and the large-scale structure. The halo–filament alignment can be a subtle and mass-dependent effect, even more so for the halo spin–filament alignment, and studying it needs a large number of haloes spanning a wide mass range. P-Millennium fulfils both requirements, having no less than 7.5 million well resolved haloes that span more than three orders of magnitude in halo mass. The large volume of P-Millennium is also critical, since it contains both the large-scale tidal forces responsible for the generation of halo spin and the diversity of environments in which haloes reside.

We have identified the filamentary network using the NEXUS multiscale morphology filter (Aragón-Calvo et al. 2007a; Cautun et al. 2013, 2014). To obtain further insight into the dynamical factors affecting the halo–filament alignments, we have studied the filament populations selected by two different versions of the NEXUS formalism. The first, NEXUS+, extracts filaments on the basis of the density field and identifies a broad range of the filament spectrum, from prominent arteries, which dominate the dynamics of the cosmic web, to tenuous tendrils, which branch off major arteries and reside in underdense regions. The second formalism, NEXUS_velshear, is based on the velocity shear field; it mostly identifies the dynamically dominant filaments and typically assigns them a larger width than NEXUS+. As we discuss shortly, the contrast between NEXUS+ and NEXUS_velshear reveals key information about the processes behind the spin–filament alignment and its dependence on local environment.

In the current study we focus on the orientation of the spin, the shape and the peculiar velocities of the dark matter haloes relative to the filament in which they are embedded at the present epoch, $z = 0$. The properties of the dark component have the advantage of being mostly determined purely by gravitational effects rather than the complex physical processes affecting the baryonic component. In subsequent studies, we will perform a detailed comparison of halo–halo evolution as a function of cosmic web environment, and we will investigate the alignments of the stellar and gas components of galaxies in the EAGLE project (Schaye et al. 2015).

The following points summarize the main results of this paper concerning the alignments of halo spins and shape with their host large-scale filament:

7.1 Halo spin orientation

In this study we have characterized how the spin of haloes is oriented with respect to their host filament to an unprecedented precision and over three orders of magnitude in halo mass. Overall, the orientation of the halo spin follows a wide distribution with a small, but statistically significant, preferential alignment with the direction of the filament (see Figs 10 and 11). There is a clearly discernible systematic trend in the median of the spin orientation: high-mass haloes tend to have their spin perpendicular to their host filament, while low-mass haloes tend to have their spin parallel to their host filament (Aragón-Calvo et al. 2007b; Hahn et al. 2007; Hahn et al. 2010; Codis et al. 2012; Trowland et al. 2013; Forero-Romero et al. 2014). We have found a transition mass of $\sim 5 \times 10^{11}\, h^{-1}\, M_\odot$ between perpendicular and parallel alignments, which is in good agreement with the wide range of ‘spin flip’ masses, around $0.5 \sim 5 \times 10^{12}\, h^{-1}\, M_\odot$, reported by previous studies.

7.1.1 Dependence on web finder

Both the spin–filament alignment as well as the spin flip mass show a small, but systematic dependence on the method used to identify the cosmic web. For same mass haloes, the halo spin tends to be closer to perpendicular on NEXUS+ filaments than on the NEXUS_velshear ones. This is manifested as slightly different values for the spin flip mass, which we have found to be 4 and 6 $\times 10^{11}\, h^{-1}\, M_\odot$ for NEXUS+ and NEXUS_velshear filaments, respectively. At high mass, the discrepancy is explained by the haloes themselves influencing the surrounding velocity shear field and thus limiting the extent to which NEXUS_velshear can recover the direction of large-scale filaments. For masses lower than $10^{12}\, h^{-1}\, M_\odot$, the discrepancy between the two web finders is mostly due to NEXUS+ identifying a population of haloes associated to filamentary tendrils in low-density regions, which tend to have more perpendicular spin orientations.

Interestingly, for haloes with $M_{200} < 10^{12}\, h^{-1}\, M_\odot$, the differences in alignment between haloes in the NEXUS+ and NEXUS_velshear filament populations disappear when we study the common haloes identified by both web finders as residing in filaments (see Fig. 12). This implies that the discrepancy is due to
differences in the halo population associated to filaments. Two outstanding differences are that the NEXUS+ population contains a significant fraction of thin filaments that are either branches of major filaments or tenuous tendrils inside underdense regions. In contrast, the NEXUS_velshear filaments consists of mostly the dynamically dominant arteries. As we discuss shortly, the variation between the two filament populations is mostly due to the dependence of the spin–filament alignment on filament properties. In short, the careful comparison of halo alignments with both filament populations, in relation with the major visual differences between the populations, casts a new light on the processes involved in the evolution of halo angular momentum and its environmental dependence.

7.1.2 Dependence on filament properties

We have also shown that the spin–filament alignment displays a strong systematic variation with the properties of filaments, in particular on the filament thickness. We have found that haloes of the same mass show a stronger trend to have their spin oriented perpendicular to their host filament if they are embedded in thinner filaments (see Figs 14 and 15, and Aragón-Calvo & Yang 2014). The trend is strong enough to result in more than an order of magnitude variation in spin flip mass, from \(0.1 \times 10^{12} h^{-1} M_\odot\) for the thinnest filaments, with diameters below \(1 h^{-1} \text{Mpc}\), to \(3.0 \times 10^{12} h^{-1} M_\odot\) for the thickest filaments. The mass density and diameter of filaments shows a tight correlation (Cautun et al. 2014) and thus we expect that a similar trend would be visible as a function of filament mass density. We note that the multiscale character of NEXUS has been instrumental in identifying this trend, since the multiscale approach allows for the simultaneous identification of both thin and thick filaments.

The strong variation with filament properties explains many puzzling results of previous studies. For example, the discrepancy between alignment strengths and the spin flip values reported by previous studies is due to the variation in the characteristics of filaments identified by different web finders (for a comparison of many web finders see Libeskind et al. 2018). The same holds for the differences between the NEXUS+ and NEXUS_velshear methods which we have studied here. The dependence of spin orientation on filament thickness also explains the variation of spin–filament alignment on the smoothing scales used to identify filaments. For single scale web finders (which is not the case for the NEXUS formalism) increasing the smoothing scale leads to identifying mostly thicker filaments (see e.g. Cautun et al. 2013), and thus results in halo spins that tend to be closer to perpendicular to their host filament, explaining the results of Codis et al. (2012) and Wang & Kang (2018).

7.1.3 Dependence on halo radial extent

We have studied for the first time how the spin–filament alignment depends on the radial position within the halo. For Milky Way mass haloes and below, the inner halo spin is more likely to be oriented perpendicular to filaments than the spin of the entire halo (see Fig. 11). The galaxies are more strongly aligned with the inner halo and thus, when compared to their entire host halo, we expect that galaxy spins are more likely to orient perpendicularly on their host filaments. This hypothesis is in good agreement with an upcoming analysis of galaxy spin–filament alignments in the EAGLE galaxy formation simulation (Ganeshaiah Veena et al., in preparation). For haloes more massive than \(\sim 5 \times 10^{12} h^{-1} M_\odot\), the converse is true and the inner halo spin is less aligned with the host filament than the whole halo spin.

Most of the recent mass accretion of a halo, especially if it is due to smooth accretion and minor mergers, is deposited in the outer regions and leaves the inner halo structure mainly intact (Wang et al. 2011). Thus, by calculating the spin of different inner halo regions we have a window into the time evolution of halo spin. This suggests that the progenitors of haloes with present day mass, \(M_{200} < 2 \times 10^{12} h^{-1} M_\odot\), had spins which were oriented perpendicular to filaments to a larger extent than their present day descendants. Thus, in low-mass haloes, recent accretion leads to a reorientation of halo spins to point preferentially along the filament. This trend is reversed for haloes more massive than \(\sim 5 \times 10^{12} h^{-1} M_\odot\), whose progenitors spins were less likely to be oriented perpendicular to filaments than their present day descendants. Thus, in high-mass haloes, recent accretion leads to an increase in the halo spin tendency to be perpendicular on the host filament.

7.2 Halo shape orientation

When considering the orientation of the halo’s shape, i.e. of the inertia tensor, we find similar alignment results as for the halo spin. While the distribution of orientation angles is broad, we have found clear systematic alignment trends that are stronger than in the case of the halo spin–filament alignment (see Fig. 16). For all mass ranges, the major axis of the halo points preferentially along its host filament ridge. On the other hand, the minor axis tends towards a perpendicular orientation with respect to the host filament. The alignment of both major and minor axes is larger for more massive haloes, which is most likely a manifestation of recent accretion processes that vary with halo mass. When analysing different halo radial ranges, we have found that the shape of the inner halo is less well aligned with the host filament than the shape of the full halo. The different behaviour of the spin–filament and shape–filament alignments is due to the weak alignment between halo spin and halo shape, with the spin showing a surprisingly wide range of orientations with respect to the shape minor axis (see Fig. 17).

7.3 Secondary accretion and filament flows

The results we have presented here reinforce and provide additional evidence that secondary anisotropic accretion is a major driver for the late time acquisition of halo spin and its orientation with respect to the large-scale filaments in which the haloes are embedded (Libeskind et al. 2013; Welker et al. 2014; Codis et al. 2015; Laigle et al. 2015; Wang & Kang 2018). The change in halo spin is a residual effect due to the transfer of orbital angular momentum from accreted clumps and from anisotropies in the smoothly accreted component. Low-mass haloes are more likely to accrete mass along directions perpendicular to their host filament, which results in their spins orienting preferentially along the filament spine. In contrast, high-mass haloes are more likely to accrete mass along their host filament, which ends up enhancing the tendency of their spin to be perpendicular to the host filament. Furthermore, haloes of the same mass are more likely to accrete mass along their host filament if they are embedded in thinner filaments.

This hypothesis is supported by the work of Borzyszkowski et al. (2017) which demonstrated a strong correlation between large-scale environment and the preferential directions of accretion. This is best understood in terms of halo types at opposite sides of the formation path spectrum: accreting versus stalled haloes. The typical mass distribution and velocity flow patterns around these two halo types are
illustrated in Fig. 20. Accreting haloes represent the dominant mass concentration in their neighbourhood, are found at the intersection of several filaments, whose diameters are typically smaller than the halo size, and accrete most of their mass along these filaments. This represents the typical filamentary accretion picture, where filaments transport mass to the haloes at their endpoints. Borzyszkowski et al. refer to these objects as accreting haloes since they have a large growth rate.

Stalled haloes, on the other hand, are embedded in a strong external tidal field, such as inside a massive filament between two clusters, and, as their name suggests, have low growth rates. The growth of these haloes takes place through accretion mainly from directions perpendicular to their host filament, and thus their spin becomes more parallel to the filament as time goes by. To understand this, let us consider a low-mass halo embedded in a prominent filament between two massive clusters. Since the filament acts as a highway for channelling mass into the clusters at its endpoints, it is characterized by a large velocity gradient along its spine. This inhibits the growth of low-mass haloes embedded in the filament since, in the halo reference frame, the velocity gradient manifests itself as mass flowing away from the halo in both directions along the filament. If the halo has a low mass, it cannot overcome the velocity gradient and thus cannot accrete significantly along the filament direction, and can grow only by accreting mass from directions perpendicular to the filament.

This hypothesis matches the results presented in this work as well as those of previous literature. The formation time of haloes depends on their mass, with massive haloes having formed only recently (see e.g. Davis et al. 1985; Hellwing et al. 2016). Thus, the fraction of accreting haloes increases with halo mass: from low-mass haloes that are mostly of the stalled type to high-mass haloes that are mostly of the accreting type (e.g. Ludlow et al. 2013). This explains why the spin–filament alignment changes from preferentially parallel at low masses to preferentially perpendicular at high masses. The fraction of accreting haloes varies with redshift, with haloes of a given mass being more likely to be of the accreting type at high redshift. This describes why the spin–filament alignment changes with redshift, with the spin flip taking place at lower halo masses at high redshift. Furthermore, the fraction of accreting haloes is larger in thin filaments, like filamentary tendrils in underdense regions, since those filaments form in regions without massive haloes (Cautun et al. 2014). This observation reveals why haloes of the same mass are more likely to have their spins oriented perpendicularly when embedded in thinner filaments.

While the present study has concentrated on the present epoch, in an accompanying study we will investigate in detail the build-up of halo angular momentum as haloes form and evolve during their complex hierarchical growth. We will investigate the processes that accompany the accretion on to and along filaments and in how far they augment the angular momentum imparted by tidal torquing during the early phases of structure formation. The redshift evolution will elucidate other aspects likely to affect the spin–filament alignment, such as the impact of the birth location of haloes (e.g. protohaloes formed in voids versus filaments) and the role of their migration path. Tracing the detailed halo history will also reveal any differences in the evolution of haloes in various filament types, e.g. prominent versus minor filaments.

For a full understanding of the impact of the cosmic web on the formation and evolution of galaxies, dark matter only simulations as the one studied here are not sufficient. Gas, radiation, and stellar (evolution) processes determine to a large extent the outcome and morphology of the emerging galaxies, and the rotation properties of their gas and stellar content. For example, some models suggest that a significant fraction of the angular momentum of low-mass galaxies is due to the accretion of cold gas streams, which can penetrate deeper in the halo than dark matter filaments (Dekel & Birnboim 2006; Pichon et al. 2011; Danovich et al. 2015; Stewart et al. 2017). Before infall into the halo, gas and dark matter acquire angular momentum through the same processes, such as torqueing due to the surrounding matter distribution. However, once the gas streams enter the inner fractions of the haloes, their angular momentum can change due to non-linear torques, dissipation, disc instabilities and feedback processes (e.g. see Danovich et al. 2015). Such processes might lead to a different galaxy spin–filament alignment than the one found for the inner region of haloes in dark matter only simulations. In order to assess how far the spin properties of the dark matter haloes are transferred to the gas and stars of the galaxy, we need to analyse galaxy formation simulations. In an accompanying paper, we will study spin–filament alignments in the EAGLE project (Schaye et al. 2015). It will be a step towards understanding how the angular momentum of gas and stars in galaxies is related to that of the parent dark halo, seeking to extend earlier studies along these lines (e.g. Hahn et al. 2010; Dubois et al. 2014; Welker et al. 2014; Zavala et al. 2016).

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