Matching next-to-leading order predictions to parton showers in supersymmetric QCD

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Abstract

We present a fully automated framework based on the FeynRules and MadGraph5_aMC@NLO programs that allows for accurate simulations of supersymmetric QCD processes at the LHC. Starting directly from a model Lagrangian that features squark and gluino interactions, event generation is achieved at the next-to-leading order in QCD, matching short-distance events to parton showers and including the subsequent decay of the produced supersymmetric particles. As an application, we study the impact of higher-order corrections in gluino pair-production in a simplified benchmark scenario inspired by current gluino LHC searches.

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1. Introduction

The LHC has been designed with the aim of exploring the electroweak symmetry breaking mechanism and to possibly shed light on phenomena beyond the Standard Model. During its first run, both the ATLAS and CMS Collaborations have extensively investigated many different channels in order to get hints for new physics. However, no striking signal has been found so that limits have been set on popular models, such as the Minimal Supersymmetric Standard Model (MSSM) [1,2], or on simplified models for new physics [3,4]. All these searches will nevertheless be pursued during the next LHC runs, benefiting from larger statistics and higher center-of-mass energy. In this work, we focus on MSSM-inspired simplified new physics scenarios in which gluino pairs can be copiously produced at the LHC. As in many related experimental searches [5-8], we consider the case where both produced gluinos decay into a pair of jets and an invisible neutralino, and then revisit the phenomenology of such models.

Experimental gluino analyses are currently based on Monte Carlo simulations of the signals where leading-order (LO) matrix elements of different partonic multiplicities are matched to parton showers and merged. The predictions are then normalized to resummed total rates combined with the next-to-leading order (NLO) result [9-13]. More sophisticated differential theoretical predictions are however always helpful for setting more accurate exclusion limits, possibly refining the search strategies, and measuring the model free parameters in case of a discovery [14]. In this context, it has been recently demonstrated that the MadGraph5_aMC@NLO framework [15] can provide a general platform for computing (differential) observables within many beyond the Standard Model theories [16]. This approach relies in particular on the use of the FeynRules [17] and NLOCT [18] packages for (automatically) generating a UFO library [19] containing the vertices and the needed counterterms for NLO computations.

Within this framework, we match for the first time NLO QCD matrix-element-based predictions to parton showers for gluino pair-production. Virtual contributions are evaluated following the Ossola–Papadopoulos–Pittau (OPP) formalism as implemented in MadLoop [20–22] and combined with real emission contributions by means of the FKS subtraction method as embedded in MadFKS [23,24]; these two modules being fully incorporated in MadGraph5_aMC@NLO. The matching to parton showers is then achieved by employing the MC@NLO method [25]. After accounting
for (LO) gluino decays, we study the impact of both the NLO contributions and the parton showers in the context of LHC physics.

2. Theoretical framework

Our study of gluino pair-production and decay is based on an MSSM-inspired simplified model. We complement the Standard Model with three generations of non-mixing left-handed and right-handed squark fields \( q_{L,R} \) of mass \( m_{q_{L,R}} \) and with a Majorana fermionic field \( \tilde{g} \) of mass \( m_\tilde{g} \). The dynamics of the new fields is described by the following Lagrangian,

\[
\mathcal{L}_{\text{SQCD}} = D_\mu \tilde{q}^+_i D^\mu q_i + D_\mu \bar{q}^+_R D^\mu q_R + \frac{1}{2} m_{\tilde{g}} \bar{\tilde{g}} \tilde{g} - \frac{1}{2} m_q \bar{q}^+_q q_q + \bar{\tilde{g}} T (\tilde{g} P_L q) + (\bar{q} P_L \tilde{g}) T q_R + \text{h.c.}
\]

that contains all interactions allowed by QCD gauge invariance and supersymmetry, as well as squark and gluino kinetic and mass terms. In our notation, \( T \) stands for the fundamental representation matrices of SU(3), \( P_L \) (\( P_R \)) for the left-handed (right-handed) chirality projector and \( g_\ast \) is the strong coupling constant. Flavor and color indices are left understood for brevity.

In addition, we enable the (possibly three-body) decays of the colored superpartners by including \((s)\)quark couplings to a gauge-singlet Majorana fermion \( \chi \) of mass \( m_\chi \) that is identified with a bino,

\[
\mathcal{L}_{\text{decay}} = \frac{i}{2} \bar{\chi} \gamma^\mu \chi - \frac{1}{2} m_\chi \bar{\chi} \chi + \sqrt{2} g_\ast \left[ -\tilde{q}^+_q Y_q (\bar{\chi} P_L q) + (\bar{q} P_L \tilde{q}) (\bar{\chi} q_R) + \text{h.c.} \right]
\]

In this Lagrangian, \( Y_q \) denotes the hypercharge quantum number of the \((s)\)quarks and \( g^\ast \), the hypercharge coupling.

At the NLO in QCD, gluino pair-production receives contributions from real emission diagrams as well as from the interferences of tree-level diagrams with virtual one-loop diagrams that exhibit ultraviolet divergences. These must be absorbed through a suitable renormalization of the parameters and of the fields appearing in \( \mathcal{L}_{\text{SQCD}} \). To this aim, we replace all (non-)fermionic bare fields \( \Psi \) (\( \Phi \)) and bare parameters \( y \) by the corresponding renormalized quantities,

\[
\Phi \rightarrow [1 + \frac{1}{2} \delta \Phi_0] \Phi, \quad \Psi \rightarrow [1 + \frac{1}{2} \delta \Psi_0] P_L \Psi + \frac{1}{2} \delta \Psi_0 P_R \Psi, \quad y \rightarrow y + \delta y,
\]

where the renormalization constants \( \delta \Phi \) and \( \delta y \) are truncated at the first order in the strong coupling \( \alpha_s \).

The wave-function renormalization constants of the massless quarks (\( \delta Z_{q_i}^{LR} \)), of the top quark (\( \delta Z_T^{LR} \)), of the gluon (\( \delta Z_\tilde{g} \)), and the top mass renormalization constant (\( \delta m_t \)) are given, when adopting the on-shell renormalization scheme, by

\[
\delta Z_q = -\frac{g_\ast^2}{24 \pi^2} \left[ -\frac{1}{3} + B_0 (m_q^2, m_t^2) + 2 m_t^2 B_0 (m_t^2, m_q^2) \right]
\]

\[
= \frac{n_c}{3} + n_c B_0 (m_q^2, m_t^2) + 2 n_c B_0 (m_t^2, m_q^2) + \sum_q \left[ \frac{1}{6} + B_0 (0, m_q^2, m_t^2) + m_t^2 B_0 (0, m_q^2, m_t^2) \right]
\]

where

\[
\delta Z_T^{LR} = \frac{g_\ast^2 C_F}{16 \pi^2} \left[ 1 + \frac{1}{3} + 2 B_1 (m_t^2, m_q^2, m_{t,R}^2) + 2 B_1 (m_t^2, m_q^2, 0) + 8 m_t^2 B'_0 (m_t^2, m_q^2, 0) + 2 m_t^2 \sum_{i=L,R} B'_1 (m_t^2, m_q^2, m_{t,i}^2) \right]
\]

\[
\delta m_t = \frac{g_\ast^2 C_F}{16 \pi^2} \left[ \frac{1}{2} + 4 B_0 (m_t^2, m_q^2, 0) + 2 B_1 (m_t^2, m_q^2, 0) \right]
\]

\[
\delta Z_\tilde{g} = \frac{g_\ast^2 C_F}{16 \pi^2} \left[ n_c + 2 m_t B_1 (m_q^2, m_t^2, 0) + 8 m_t^2 B'_0 (m_q^2, m_t^2, 0) + 4 n_c B'_1 (m_q^2, m_t^2, 0) + \sum_{q=\bar{q}, \tilde{q}} B_1 (m_q^2, m_{t,R}^2, m_{t,R}^2) + 2 m_t^2 B'_1 (m_q^2, m_{t,R}^2, m_{t,R}^2) \right]
\]

while the squark wave-function (\( \delta Z_{\tilde{q}} \)) and mass (\( \delta m_{\tilde{q}} \)) renormalization constants read,

\[
\delta Z_{\tilde{q}} = \frac{g_\ast^2 C_F}{8 \pi^2} \left[ - B_0 (m_{\tilde{q}}^2, m_{\tilde{q}}^2, m_{\tilde{q}}^2) + B_0 (m_{\tilde{q}}^2, m_{\tilde{q}}^2, 0) + \left( m_{\tilde{q}}^2 - m_t^2 - m_q^2 \right) B'_0 (m_{\tilde{q}}^2, m_{\tilde{q}}^2, m_{\tilde{q}}^2) + 2 m_t^2 B'_0 (m_{\tilde{q}}^2, m_{\tilde{q}}^2, m_{\tilde{q}}^2) \right]
\]

\[
\delta m_{\tilde{q}} = \frac{g_\ast^2 C_F}{8 \pi^2} \left[ A_0 (m_{\tilde{q}}^2) - A_0 (m_{\tilde{q}}^2) - 2 m_t^2 B_0 (m_{\tilde{q}}^2, m_{\tilde{q}}^2, 0) + \left( m_{\tilde{q}}^2 - m_t^2 - m_q^2 \right) B_0 (m_{\tilde{q}}^2, m_{\tilde{q}}^2, 0) - A_0 (m_{\tilde{q}}^2) \right]
\]

with (\( -1^q = 1 \) and (\( -1^R = -1 \), and with \( m_{\tilde{q}} \neq 0 \) for top squarks only. As a result of the structure of the gluino–squark–quark interactions, squark mixing effects proportional to the corresponding quark masses are generated at the one-loop level and must be accounted for in the renormalization procedure. In our simplified setup, we consider \( n_f = 5 \) flavors of massless squarks so that these effects are only relevant for the sector of the top squarks. In this case, matrix renormalization is in order,

\[
\left( \begin{array}{c} \tilde{t}_L \\ \tilde{t}_R \end{array} \right) \rightarrow \left( \begin{array}{c} \tilde{t}_L \\ \tilde{t}_R \end{array} \right) + \frac{1}{2} \left( \begin{array}{c} \delta Z_{\tilde{t}}_{li} \\ \delta Z_{\tilde{t}, LR} \end{array} \right) \left( \begin{array}{c} \tilde{t}_L \\ \tilde{t}_R \end{array} \right)
\]

and we impose that the stop sector is renormalized so that left-handed and right-handed stops are still defined as non-mixed states at the one-loop level. In the MSSM, this is made possible
by stop couplings to the Higgs sector that generate an off-diagonal mass
counterterm.

\[ \delta \mathcal{L}_{\text{off}} = -\delta m^2_{\text{LR}} (\tilde{t}^\dagger L \tilde{t} + \tilde{t}^\dagger R \tilde{t} L) \, . \]

These Higgs couplings being absent in our simplified model, we therefore introduce \( \delta \mathcal{L}_{\text{off}} \) explicitly. The off-diagonal stop wavefunction \( \delta \mathcal{Z}_{\text{LR}} \) and mass \( \delta m^2_{\text{LR}} \) renormalization constants are then found to be

\[ \delta \mathcal{Z}_{\text{LR}} = \frac{g^2 C F m_\tilde{g}}{4 \pi^2 (m^2_{\tilde{g}} - m^2_{\tilde{t}})} \sum_{i=L,R} (-1)^i B_0(m^2_{\tilde{t} i}, \mu_L^2, \mu_R^2), \]

\[ \delta m^2_{\text{LR}} = \frac{g^2 C F m_\tilde{g}}{8 \pi^2} \sum_{i=L,R} B_0(m^2_{\tilde{t} i}, \mu_L^2, \mu_R^2), \]

where \( \delta \mathcal{Z}_{\text{LR}} \) has been symmetrized. In this way, it incorporates the renormalization of the stop mixing angle (taken vanishing in our model) which does not need to be explicitly introduced [27].

In order to ensure that the running of \( \alpha_s \) solely originates from gluons and not \( n_f \) active flavors of light quarks, we renormalize the strong coupling by subtracting at zero-momentum transfer, in the gluon self-energy, all massive particle contributions. This gives

\[ \frac{\delta \alpha_s}{\alpha_s} = \frac{\alpha_s}{2 \pi \epsilon} \left[ \frac{n_f}{3} - \frac{11 n_c}{6} \right] + \frac{\alpha_s}{6 \pi \epsilon} \left( \frac{1}{\epsilon} \log \frac{m^2_{\tilde{g}}}{\mu_R^2} \right) \]

\[ + \frac{\alpha_s n_c}{6 \pi} \left( \frac{1}{\epsilon} \log \frac{m^2_{\tilde{t}}}{\mu_R^2} \right) - \frac{\alpha_s}{24 \pi} \sum_{q} \left( \frac{1}{\epsilon} - \log \frac{m^2_{\tilde{q}}}{\mu_R^2} \right) \, . \]

The ultraviolet-divergent parts of \( \delta \alpha_s / \alpha_s \) are written in terms of the quantity \( \frac{\epsilon}{\epsilon} = 1 - 2 \gamma_e + 4 \log 4 \pi \) where \( \gamma_e \) is the Euler–Mascheroni constant and \( \epsilon \) is connected to the number of space–time dimensions \( D = 4 - 2 \epsilon \).

Finally, the artificial breaking of supersymmetry by the mismatch of the two gluino and the \( (D - 2) \) transverse gluon degrees of freedom must be compensated by finite counterterms. Imposing that the definition of the strong coupling \( \alpha_s \) is identical to the Standard Model one, only quark–squark–gluino vertices and four-scalar interactions have to be shifted [28],

\[ \mathcal{L}_{\text{SCT}} = \frac{\sqrt{2} g}{3 \pi} \frac{\alpha_s}{\epsilon} \left[ \tilde{q}_L \gamma \tilde{g} P_L q \right] + \left( \tilde{q}_L \gamma \tilde{g} P_L q \right) \tilde{t}^\dagger \tilde{q}^\dagger R + \text{h.c.} \]

\[ + \frac{g^2}{4 \pi} \frac{\alpha_s}{\epsilon} \left[ \tilde{q}_L \gamma \tilde{t}^\dagger \tilde{q}^\dagger R + \tilde{t}^\dagger \tilde{q}^\dagger R + \tilde{q}_L \gamma \tilde{t}^\dagger \right] \tilde{q} \]

\[ \times \left[ \tilde{t}_R^\dagger (T^a, T^b) \tilde{q}^\dagger R + \tilde{t}_R^\dagger T^a \tilde{q}^\dagger R + \tilde{t}_R^\dagger T^b \tilde{q}^\dagger R \right] \]

\[ - \frac{g^2}{4 \pi} \frac{\alpha_s}{\epsilon} \left[ \tilde{t}_R^\dagger \tilde{q} \tilde{q}_L - \tilde{q}_L \tilde{q} \tilde{t}_R \right] \]

where we have introduced adjoint color indices for clarity.

In our phenomenological study, loop-calculations are performed numerically in four dimensions by means of the MadGraph package and therefore require the extraction of rational parts that are related to the \( \epsilon \)-pieces of the loop-integral denominators \( (R_1, \ldots) \), which are automatically reconstructed within the OPP reduction procedure) and numerators \( (R_2) \). For any renormalizable theory, the number of \( R_2 \) terms is finite and they can be seen as counterterms derived from the bare Lagrangian [29]. In the context of the \( \mathcal{L}_{\text{SCT}} \) Lagrangian, all necessary \( R_2 \) counterterms can be found in Ref. [30].

The setup described above has been implemented in the FeynRules package and we have made use of the NLOCT program to automatically calculate all the ultraviolet and \( R_2 \) counterterms of the model. The specificity of the renormalization of the stop sector has been implemented via a new option of NLOCT, SupersymmetryScheme->"OS", that allows to treat all scalar fields that mix at the loop-level as described above. We have validated the output against our analytical calculations, and these results represent the first validation of NLOCT in the context of computations involving massive Majorana colored particles. We have finally generated a UFO version of the model that can be loaded into MADGRAPH5_aMC@NLO and which we have made publicly available on http://feynrules.irmp.ucl.ac.be/wiki/NLOModels. We have further validated the model, together with the numerical treatment of the loop-diagrams by MadLoop, by comparing MadGRAPH5_aMC@NLO predictions to those of the code PROSPINO [31], using a fully degenerate mass spectrum due to the limitations of the latter.

3. LHC phenomenology

In Table 1, we compute gluino pair-production total cross sections for proton–proton collisions at a center-of-mass energy of \( \sqrt{s} = 13 \) TeV and for different gluino masses. Squarks are decoupled \((m_{\tilde{q}} = 16 \text{ TeV}, m_{\tilde{g}} = 17 \text{ TeV} \text{ and } m_\chi = m_{\tilde{q}} = 15 \text{ TeV})\) so that any resonant squark contribution appearing in the real-emission topologies is off-shell and therefore suppressed. The latter production modes can be seen as the associated production of a gluino and a squark that subsequently decays into a gluino and a quark. Including these contributions as parts of the NLO QCD corrections for gluino pair-production would hence result in a double-counting when considering together all superpartner production processes inclusively. Moreover, these resonant channels require a special treatment in the fully-automated MADGRAPH5_aMC@NLO framework, that is left to future work [32]. Our choice for the squark spectrum corresponds to the one made by ATLAS and CMS Collaborations in their respective gluino searches [5–8].

<table>
<thead>
<tr>
<th>( m_\chi ) [GeV]</th>
<th>( \sigma_{\text{LO}} ) [pb]</th>
<th>( \sigma_{\text{NLO}} ) [pb]</th>
</tr>
</thead>
<tbody>
<tr>
<td>200</td>
<td>2104 ± 35.0 ± 14.0</td>
<td>3183 ± 10.8 ± 1.8</td>
</tr>
<tr>
<td>210</td>
<td>2105 ± 34.0 ± 14.0</td>
<td>3180 ± 10.6 ± 1.6</td>
</tr>
<tr>
<td>220</td>
<td>15.46 ± 34.75 ± 19.55</td>
<td>24.90 ± 12.5 ± 3.72</td>
</tr>
<tr>
<td>240</td>
<td>21.06 ± 35.05 ± 23.55</td>
<td>2.009 ± 13.5 ± 5.55</td>
</tr>
<tr>
<td>260</td>
<td>1.068 ± 10.11 ± 36.41 ± 26.46</td>
<td>2.743 ± 10.41 ± 44.45 ± 7.31</td>
</tr>
<tr>
<td>280</td>
<td>6.264 ± 11.01 ± 36.41 ± 26.46</td>
<td>1.056 ± 10.11 ± 36.41 ± 11.3</td>
</tr>
<tr>
<td>300</td>
<td>4.217 ± 11.04 ± 35.01 ± 29.83</td>
<td>6.327 ± 10.11 ± 10.72 ± 11.3</td>
</tr>
</tbody>
</table>

Our results are evaluated both at the LO and NLO accuracy in QCD and presented together with scale and parton distribution (PDF) uncertainties. For the central values, we set the renormalization and factorization scales to half the sum of the transverse mass of all final state particles and use the NNPDF 3.0 set of parton distributions [33] accessed via the LHAPDF 6 library [34]. Scale uncertainties are derived by varying both scales independently by factors \( 1/2, 1 \text{ and } 2 \), and the PDF uncertainties have been extracted from the cross section values spanned by all NNPDF distribution replicas following the NNPDF recommendations [35]. We observe a significant enhancement of the cross section of about 50% due to genuine NLO contributions, as well as a sizable reduction of the uncertainties. In particular, the apparent drastic reduction of the PDF uncertainties is related to the poor quality of the LO NNPDF fit when compared to the NLO fit [33].

In order to achieve realistic simulations of LHC collisions, we first handle gluino decays into two colored partons and a neutralino via an off-shell squark by using tree-level decay matrix elements. For the fixed-order results presented below, we have
Fig. 1. First five leading jet and gluino-pair transverse-momentum spectra for the production of a pair of gluinos decaying each into two colored partons and a neutralino. We consider two mass configurations and show results at the NLO (red) and LO (blue) accuracy in QCD, at the fixed-order (dashed, fLO and fNLO) and after matching to the Pythia 8 parton-shower description (solid). Theoretical uncertainties related to the fixed order calculations are shown as blue (LO) and gray (NLO) bands. The lower insets of the figure present ratios of NLO results to LO ones, both at fixed order (dashed) and after matching to parton showers (solid). (For interpretation of the references to color in this figure legend, the reader is referred to the web version of this article.)
analytically calculated those decay matrix elements and integrated them over the phase space, after checking our results with the MadSpin [36] and MadWidth [37] programs. These latter two programs have been used in the computation of the NLO predictions matched to parton showers. Due to the three-body nature of the gluino decays, spin correlations are here omitted as MadSpin can only handle them for two-body decays. We then interface the partonic events obtained in this way to a parton showering and hadronization description as provided by the PyTHIA 8 package [38], and use the anti-$k_T$ jet reconstruction algorithm [39] with a radius parameter set to 0.4, as implemented in FastJet [40], to reconstruct all final state parton-level and hadron-level jets for fixed-order and parton-shower-matched calculations respectively. Finally, the phenomenological analysis of the generated events is performed with MadAnalysis 5 [41].

Key differential distributions particularly sensitive to both NLO and shower effects are presented in Fig. 1. We show the transverse-momentum ($p_T$) spectra of the first five leading jets (first five subfigures) for two benchmark scenarios featuring either a light ($m_{\tilde{g}} = 1$ TeV) or a heavy ($m_{\tilde{g}} = 2$ TeV) gluino, as well as a rather light bino ($m_{\tilde{b}} = 50$ GeV). We compare fixed-order predictions (dashed) to results matched to parton showers (solid) and consider both LO (blue) and NLO (red) accuracy in QCD. We observe that most of the differential $K$-factors (i.e. the bin-by-bin ratios of the NLO result to the LO one) both with and without parton-shower matching strongly depend on the jet $p_T$ in the considered $p_T$ range. The NLO effects therefore not only increase the overall normalization of the distributions, but also distort their shapes. The $K$-factor is indeed greater at low $p_T$ than at high $p_T$, so that the traditional procedure of using LO predictions scaled by inclusive $K$-factors cannot be used for an accurate gluino signal description.

Fig. 1 also underlines the effects of matching LO and NLO matrix elements to parton showers. Since most parton-level jets originate from the decay of very massive gluinos, the fixed-order $p_T$ distributions peak at large $p_T$ values. In addition, the low-$p_T$ region of these spectra is depleted, with the exception of the fourth and fifth jet $p_T$ spectra where radiation effects are non-negligible. As a result of the matching to parton showers, the fixed-order NLO distributions are distorted and softened. While the change is milder in the large-$p_T$ tails whose shapes are controlled by the hard matrix element, the low-$p_T$ regions are mostly sensitive to effects due to multiple emissions and hence become populated. The parton shower emissions from hard partons are indeed often not reclustered back with the jet they are issued from, hence distorting the jet $p_T$ spectra. For this reason, resummation effects become significant below the peak of the various $p_T$ distributions. This effect is also illustrated on the last subfigure of Fig. 1, where we show the $p_T$ spectrum of the gluino pair in the small $p_T$ range. We have verified that the matched results agree with the fixed-order ones for very large $p_T$ values of the order of the gluino mass.

4. Conclusions

We have performed the first calculation of NLO supersymmetric QCD corrections to gluino pair-production matched to parton showers and have studied the impact of both the NLO contributions and of the parton showers. We have shown that observable effects could be induced on quantities typically used to obtain exclusion limits and that more accurate calculations are crucial for extracting model parameters in case of a discovery. Our calculation has been performed fully automatically and we have applied it to the case of a simplified model similar to one of those used by the ATLAS and CMS Collaborations for their respective gluino searches. In addition, we have publicly released the UFO model associated with our computation, that is sufficiently general to be readily used to explore the phenomenology associated with any supersymmetric QCD process.

Finally, our results also show that all technical obstacles for automating the matching of fixed-order calculations for inclusive supersymmetric particle production at the NLO in QCD to parton showers have been cleared, up to the ambiguity issue of the double counting arising in real emission resonant contributions [32].

Acknowledgements

We are grateful to R. Frederix, S. Frixione, F. Maltoni and O. Mattelaer for enlightening discussions. This work has been supported in part by the ERC grant 291377 LHCtheory: Theoretical predictions and analyses of LHC physics: advancing the precision frontier, the Research Executive Agency of the European Union under Grant Agreement PITN-GA-2012-315877 (MCNet) and the Theory-LHC-France initiative of the CNRS (INP/IN2P3). C.D. is a Durham International Junior Research Fellow, V.H. is supported by the SNF grant PBELP2 146525 and J.P. by a PhD grant of the Investissements d’avenir, Labex ENIGMASS.

References


