Protein Docking Using a Single Representation for Protein Surface, Electrostatics, and Local Dynamics

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Supporting Information

ABSTRACT: Predicting the assembly of multiple proteins into specific complexes is critical to understanding their biological function in an organism and thus the design of drugs to address their malfunction. Proteins are flexible molecules, which inherently pose a problem to any protein docking computational method, where even a simple rearrangement of the side chain and backbone atoms at the interface of binding partners complicates the successful determination of the correct docked pose. Herein, we present a means of representing protein surface, electrostatics, and local dynamics within a single volumetric descriptor. We show that our representations can be physically related to the surface-accessible solvent area and mass of the protein. We then demonstrate that the application of this representation into a protein–protein docking scenario bypasses the need to compensate for, and predict, specific side chain packing at the interface of binding partners. This representation is leveraged in our de novo protein docking software, JabberDock, which can accurately and robustly predict difficult target complexes with an average success rate of >54%, which is comparable to or greater than the currently available methods.

INTRODUCTION

Most functions in an organism are governed by interactions of proteins with specific substrates. To achieve their task, proteins often form homo- and heteromultimeric complexes. A plethora of genetic diseases is connected to mutations altering protein structures and consequently their capacity to interact with their binding partners. Consequently, a great body of research and development focuses on methods for the elucidation of protein structures. In this context, computational techniques devised to predict the complex formed when two proteins bind can be of great help. In silico techniques can often be significantly cheaper and quicker than experimental methods, and their predictive capability can be harnessed to guide subsequent targeted experiments.

Protein–protein docking is a highly complex optimization problem, requiring the generation of a considerable number of candidate arrangements. To accurately discriminate between correct and incorrect docked poses, an accurate scoring function is essential. Typical scoring functions used in this context involve a set of nontrivial physical or empirical terms, combined with custom weightings. An ideal scoring function should feature minimum mathematical uncertainty while accounting for protein structure and dynamics. In order to navigate the landscape of possible conformations in search of the specific arrangements that minimize this scoring function, a highly efficient exploration method is also required. The two are intimately linked, with the scoring function guiding the behavior of the navigator.

The simplest and most widespread approaches for protein–protein docking involve a global, systematic, rigid-body docking search. Typically, a large number of solutions are generated from a pair of static molecular structures, ~4 and a scoring function is then used to identify the most favorable arrangement. Treating proteins as fully rigid objects, while simultaneously using a scoring function that accounts for the specific position of each atom, leads to a modeling process that is excessively sensitive to the specific packing of atoms at the interface. In order to cater to protein dynamics, alterations to how models are built or how the scoring function assesses a protein arrangement are required. Possible strategies include rigid-body docking of ensembles of structures, additional refinement stages that take place after rigid-body docking, scoring functions that feature soft potentials to allow minor molecular overlaps, pseudo-coarse-grained protein representations, docking subunits connected by potentials, matching protein surfaces represented as a collection of patches, using normal modes to account for flexible conformational switches, and relaxing the interface of docking poses using techniques such as molecular dynamics (MD), Monte Carlo (MC), or simulated annealing. Some methods, such as HADDOCK and IMP, feature scoring functions that utilize a combination of terms that describe physical interactions and penalize models that do not recapitulate the available experimental data. Overall, two approaches are used to describe amino acid side chains at the interface. They are either represented explicitly, thus requiring the docking method to determine their correct

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packing, or their presence is described by means of pseudo-coarse-grained representations. The first method requires highly sophisticated optimization procedures that may still yield suboptimal arrangements, whereas the second method usually ignores the uncertainty in the position of the side chains that comes naturally with any time dynamics.

In this work, we describe a new protein volumetric representation, named spatial and temporal influence density (STID) maps, capable of simultaneously describing protein shape, electrostatics, and local dynamics (see Figure 1c). We demonstrate that the complementarity of these isosurfaces can help create suitable solutions in a protein–protein docking scenario. While surface complementarity techniques have been used for many years,19 the representations from STID maps are superior to any surface method used to date. STID maps inherently consider any side chain flexibility by using the general motion of atomic point charges in time as a building block for the model. We demonstrate that the key consequence of this is the retention of accuracy between identified docking models regardless of their difficulty.

Our STID map-based scoring method is embodied in JabberDock, a protein de novo docking software. JabberDock explores the surface complementarity space of two binding partners by means of a particle swarm optimization (PSO) algorithm supplied by the POWer optimization environment.20 POWer features a modified version of the PSO algorithm, explicitly adapted to prevent premature convergence and maximize the diversity of solutions.

Hereafter, we first outline the theory behind our protein representation method and then present a set of benchmarks aimed at testing the accuracy of our protein–protein docking method in line with the CAPRI blind docking competition guidelines.21 Results demonstrate that JabberDock can return models matching the quality of top de novo docking algorithms currently available.

**THEORY**

The following theory is built upon the principle that a volumetric map can consider both the structural and dynamical properties of a protein. It is constructed from the inherent motion of charged atoms via the time-averaged dipoles forming within a localized space. The complete methodology, represented in Figure 1, is summarized as follows:

1. The PDB file of a protein structure is input along with the desired atomistic force field.
2. The protein is immersed in a water box with Na$^+$ or Cl$^-$ acting as counterions and automatically subjected to energy minimization, followed by an MD equilibration and production protocol.
3. A dipole map is derived based on the produced MD trajectory.
4. The dipole map is converted into a three-dimensional grid of points, each containing a pseudo-atom with a characteristic van der Waals radius.
5. Each pseudo-atom is used to define a local Gaussian distribution, with a standard deviation determined by the van der Waals radius of the pseudo-atom.
6. A volumetric map is produced by summing, on each grid point, the value of local and neighboring Gaussians. The resulting map is finally normalized.

**From Protein Structure to Dipole Map.** The overall dynamics of a protein emerge from a combination of slow large-scale motions and fast local rearrangements. We start by sampling the fast motions of the side chains by means of a short MD simulation. Consistent with experimental NMR evidence,22 we have found that 500 ps is enough for this purpose (see the Supporting Information and Figures S1 and S2). We align the resulting protein trajectory according to the center of mass of the molecule and arrange it within a stationary, cubic grid, wherein each voxel is 1 Å across in x, y, and z (a parameter determined quantitatively in a benchmark shown in Figures S3–S5). We use this information to calculate the local dipoles on each grid point. To this end, we are expanding upon the theory laid out by Kirkwood,23 Fröhlich,24 and Neumann et al.,25 which describes the fundamental theory of dielectrics.

Following the Onsager theory of dielectric polarization, we represent each voxel, v, as a spherical solute with volume, $V_v$, with an internal permittivity, $ε_v$, embedded within a uniform dielectric continuum with permittivity $ε_∞$. The charge distribution inside the voxel is that of several point charges, with a dipole associated with the center. Point charges within the neighboring voxels on each Cartesian edge and corner (i.e., a total of 26 neighbors, a quantity determined in a benchmark shown in Figures S3–S5) are also associated with the central voxel. A sliding window is applied spatially such that a point charge at a time, $t$, will contribute to 27 different voxels in total. Given the fluctuations of the dipole moment of the solute, $M_v$, observed over the simulation in a voxel, it is possible to calculate $ε_v$.

The Fröhlich–Kirkwood model states that $ε_v$ is a function of the probability distribution of the total dipole’s second moment, with $M_v$ given by

$$M_v = \sum_{i=0}^{N} q_i r_{i,v}$$  \hspace{1cm} (1)

where $q_i$ is the charge of atom $i$ at distance $r_{i,v}$ from the geometrical center of voxel $v$. $N$ is the number of atoms that contribute to a voxel’s dipole moment. The charges are obtained from the force field used for the simulation. For a solute with a net charge, which most voxels have, $M_v$ is dependent on the origin; thus, the grid is fixed in time and space. Therefore, we can produce a dipole map delivering a representation of local vectorial electrostatic characteristics of a region of space occupied by a molecule (see Figure 1b).

**From Dipole Map to STID Map.** We can now leverage on the obtained dipole map to derive volumetric information on a

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Figure 1. Pipeline for the generation of STID maps. (a) Superimposition of multiple structures from the MDs simulation of ribonuclease A (PDB: 9RSA), clouded by secondary structure (α helices as blue, β$_{10}$ helices as light purple, β sheets as red, unstructured coils as white, and turns as gray). (b) Superimposed dipole map generated from the simulation. For clarity, only dipoles greater than 0.8 D are shown. (c) Final STID map, derived from the dipole map.
molecule, i.e., a quantity that is easy to visualize and to use in a protein–protein docking context. To this end, it is necessary to convert its dipolar vectorial representation into a scalar quantity. Under the Fröhlich–Kirkwood model, we can relate the fluctuations of each dipole moment, \( \mathbf{M}_v \), to the voxel’s dielectric, \( \varepsilon_v \):

\[
\langle \mathbf{M}_v^2 \rangle - \langle \mathbf{M}_v \rangle^2 = \frac{2\varepsilon_{\text{ex}} + 1}{2\varepsilon_{\text{ex}} + \varepsilon_v} \left( \frac{\varepsilon_v - 1}{\varepsilon_v + 1} \right)
\]

where \( T_v \) is the temperature in a voxel, which we approximate as the temperature of the system. Solving for \( \varepsilon_v \):

\[
\varepsilon_v = \frac{1 + \frac{\langle \mathbf{M}_v^2 \rangle - \langle \mathbf{M}_v \rangle^2}{3\varepsilon_{\text{ex}}^2} \frac{2\varepsilon_{\text{ex}} + 1}{(2\varepsilon_{\text{ex}} + 1)^2}}{1 - \frac{\langle \mathbf{M}_v^2 \rangle - \langle \mathbf{M}_v \rangle^2}{3\varepsilon_{\text{ex}}^2} \frac{2\varepsilon_{\text{ex}} + 1}{(2\varepsilon_{\text{ex}} + 1)^2}}
\]

where \( N_v \) is the number density inside the voxel. Because \( N_v \) is derived from the number of pseudo-atoms inside a voxel; that is, \( 1 \), we can simply set it as the inverse of \( V_v \). The \( \alpha_v \) values can then be related to the van der Waals radii \( R_{vdW} \) by a scaling relationship identified by Fedorov et al. based on the quantum Drude oscillator model

\[
R_{vdW} = 2.54\alpha_v^{(1/7)}
\]

where the constant 2.54 is a universal scaling factor between electron density and atomic volume at \( R_{vdW} \) in atomic units. Although Fedorov et al. note that a full derivation of this constant is still incomplete, they demonstrate that the relationship in eq 5 gives theoretical quantities closer to experimental data than previous models based on classical hard-sphere representations.

The electrostatic and dynamic information encapsulated in the local \( R_{vdW} \) values is now suitable to be transformed into a quantity encoding a pseudo-electron density. To this end, we assume that each pseudo-atom radius is equal to the full width at half-maximum of a decaying function, here defined as a three-dimensional Gaussian, with the maximum at the voxel’s center. This allows each pseudo-electron density to “leak” into neighboring voxels, which is reasonable given that a central voxel’s behavior is characterized by the atoms in its neighborhood.

Contributions from any Gaussians with a nonzero value present within a voxel are then summed, and the resulting map is finally normalized (an isosurface example is shown in Figure 1c), yielding a molecular representation called spatial and temporal influence density (STID) maps. Because of this methodology, the regions inside the protein’s conformational space that are visited often or are highly charged will have greater associated STID values. This property makes STID maps a useful representation in a protein–protein docking scenario, with the electrostatics arising from rapid side chain motions, often ignored with other docking software, now accounted for.

### RESULTS

**STID Map Cutoff Values and Solvent-Accessible Surface Area of the Protein Are Related.** The global average STID, \( D_{avg} \), provides us with a direct comparison between the different structural and dynamic characteristics of a protein. The presence of both rigid and highly charged regions within a protein contributes greater STID values to their respective voxels than a flexible or apolar residue. This is shown in Figure 2a, where only the core regions of the protein are observed at greater isosurface cutoffs, but the more flexible regions can be seen at lower isosvalues. Furthermore, we found that, while having a greater relative quantity of charged or polar residues did indeed increase the \( D_{avg} \), time-averaged dynamics and the structure had a considerably larger impact on the maps’ topography.

We sought to determine whether a link exists between the characteristic \( D_{avg} \) of each protein and any of their physical quantities that are easily measurable. For this test, we select 118 proteins with various sizes, shapes, and secondary structures and observed that the ratio between SASA and molecular weight, \( S_{av} \), was anticorrelated with \( D_{avg} \) (see Figure
Figure 3. (a) (1) STID map of two binding partners is calculated using their respective MD simulations. (2) STID map representation of both binding partners is leveraged by JabberDock, our de novo protein docking algorithm, to accurately predict the complex. The image shows the intermediate quality model of ribonuclease A complexed with its inhibitor (PDB: 1DFJ). (b) Quality of best models within the top 10 results for every docking case. For each case, the lowest α carbon rmsd between prediction and crystallized complex is presented, against their associated native residue fraction (f_{nat}). Point colors indicate the case difficulty, while the dark- to light-shaded regions represent the criteria for high, intermediate, and acceptable quality results, respectively. Thus, a point landing in one of these regions indicates that the corresponding success was found within the top 10 ranked JabberDock solutions. The top and right adjoining subplots show, respectively, the distribution of rmsds and f_{nat} across the models. (c) Percentage of test cases yielding an acceptable (top) and intermediate (bottom) success, as a function of the number of ranked structures considered as candidate models. Data are reported independently, in different colors, per case difficulty. The region corresponding to the top 10 models is shaded and magnified in the insets. In this region, JabberDock’s success rate is consistent vs easy, medium, and difficult docking cases. In the larger pool of 300 models, an acceptable solution is always found for the easy cases.

The relationship could be fitted via a linear least-square fit (Pearson correlation coefficient equal to $-0.80$)

$$D_{\text{avg}} = 0.34S_{\text{m}} + 0.59$$

Thus, each STID map is associated with a characteristic cutoff value, determined by the SASA and molecular weight of the protein. Important topographical features of the STID maps are entirely independent of the protein: core secondary structure features are always visible in and around an isovalue of 0.8, and highly charged atoms become isolated from the body of the protein at more stringent isovalue of 0.43. This direct link between the structural characteristics of a protein and its associated volumetric isosurface’s shape makes STID maps an appropriate way of representing how a protein will be perceived by its immediate surroundings, such as a binding partner.

STID Maps are Effective to Score Protein–Protein Interactions. STID maps encapsulate information on the local dynamics of the atomic charges in a protein. This feature is particularly attractive in a protein–protein docking context, as it circumvents the need of determining the specific atomic position of each side chain at the interface between two binding partners. We, therefore, used this representation within a docking protocol, where the scoring function is determined by the surface complementarity of ligand and receptor STID map isosurfaces (see Methods section). Benefitting from the fact that the structural characteristics reported by each STID map isovalue are protein-independent, we determined that an isovalue of 0.43 is the most appropriate to report on all electrostatic and dynamic features of any protein within our surface complementarity scheme (see the benchmark in Figures S6 and S7).

We implemented this calibrated STID map-based scoring into our de novo protein docking algorithm: JabberDock. The program utilized the PSO algorithm within the POW<sup>27</sup> environment to explore the energy landscape associated with the arrangement of two binding partners, in search of the arrangement maximizing our complementarity score. We assessed the performance of JabberDock against all the 230 test cases featured in the most recent iteration of the standard protein–protein interaction benchmark<sup>27</sup> (six cases excluded for the presence of nonstandard amino acids). According to the root-mean-square deviation (rmsd) between unbound and known bound state, 151 of these cases are classified as rigid-body (easy), 45 as medium, and 34 as difficult (see Methods section). To gather further information on the relationship between docking quality and the conformational change proteins undergo upon binding, we selected a diverse subset of 32 cases (20 easy, 7 medium, and 5 difficult) that were also treated as bound cases. In these cases, the subunits used to predict the assemblies were proteins extracted from the known complex. We classified the quality of all our modeling runs according to the three CAPRI categories—acceptable, intermediate, and high (see the definition in Methods section).
Hereon, we qualify a test case as a success if at least one model in the top 10 ranked solutions is at least of acceptable quality.

Against the 32 bound cases, JabberDock was successful in 85.0% of the easy, 71.4% of the medium, and 20.0% of the difficult cases. Challenged with the full unbound benchmark set, JabberDock yielded successful predictions for 56.3% of the easy, 60.0% of the medium, and 54.9% of the difficult cases. Although no high-quality predictions were found for any of the test cases, intermediate quality results were found for 29.2% of the easy, 22.2% of the medium, and 25.8% of the difficult cases. Overall, these results indicate that JabberDock performance is mostly unaffected by the case difficulty (full details are provided in Table S1). These results compare favorably against four of the most commonly used protein–protein docking algorithms: SwarmDock, pyDock, ZDOCK, and HADDOCK. As reported by Vreven et al. while setting the rate for rigid-body cases ranges between 31 and 50%, whereas models, where success rates <6% are reported, that JabberDock intermediate success rates, 13 with more rmsd of models versus the known complex is lower for cases throughout cases of di

least one acceptable pose (Figure 3c). Easy cases, our full data sets of 300 solutions always contain at scoring function, better models may well be available when we most successful models usually rank high according to our

eight model is most likely to be high. Still, by increasing the number of candidate models to 100, results with significantly smaller rmsd and higher f_un can be found (Figure S8). Thus, while most successful models usually rank high according to our scoring function, better models may well be available when we consider a larger pool of solutions. For instance, in 98.6% of easy cases, our full data sets of 300 solutions always contain at least one acceptable pose (Figure 3c).

By aligning each monomeric subunit to their counterpart in the complex and assessing the score achieved by such a pose, we observed that four of the easy and one of the difficult cases yielded scores higher than anything found by JabberDock (see Table S1). One example is the xyloglucan-specific endo-β-1,4-glucanase (PDB: 3VLB), where the two binding partners are highly interlocked. In this case, failure was not caused by an unsuitable scoring function, but by an underperforming optimizer, which was unable to navigate into the complex binding site. Many of the successful unbound cases feature highly interlocked arrangements. In such cases, if the optimizer can identify the narrow set of roto-translation allowing the binding partners to interlock, the resulting model will have a high score. A successful example is that of the β-lactamase TEM1 (PDB: 1BTL)—ribonuclease A (PDB: 9RSA) complex, involving a significantly large and complex contact region, whereby almost the entire circumference of β-lactamase’s STID map is buried (see Figure 3a).

Unsuccessful cases, such as the profilin–β-actin complex (PDB: 2BTF), most often feature a flat binding site. In these cases, the surface complementarity score alone struggles to discriminate between binding and nonbinding regions because of a lack of characteristic surface features, and thus successful models do not rank high. Addressing these cases requires capturing additional properties of protein–protein interactions. To this end, we explored the possibility of reranking JabberDock models accounting to the vectorial alignment of neighboring dipoles at the interface via the dipole maps used to build the STID maps (see the Supporting Information). Preliminary results indicate that such a post-processing reranking, while not increasing the overall success rate, significantly improved the quality of poses for 12% of the data set.

The most flexible model for which we had a successful prediction was the histone chaperone CIA/ASPI1-double bromodomain complex (PDB: 3AAD), with an rmsd between the known unbound and bound state of 4.37 Å. The 46 kDa complex formed by thioredoxin reductase (thioredoxin) and the NADP+ analogue AADP+ (PDB: 1F6M) was more flexible, exhibiting domain movements associated with an rmsd of 4.9 Å. As no top 10 model produced by JabberDock had an rmsd lower than 10 Å from the known bound state, this case was declared unsuccessful. However, a top 10 model featured an f_un of 0.419 (rank 7, see Table S1), indicating that the binding site was partially identified. Thus, while in terms of rmsd several cases were unsuccessful, JabberDock could still identify their binding site (see Figure 3b).

Following from this, an interesting unbound case is that of the UBA domain from Cbl-b ubiquitin ligase (PDB: 2OOA), a small 11 kDa protein. Although it is crystallized as a homodimer, it is its monomer that participates in the formation of a heteromultimer (PDB: 2OOB) with ubiquitin. Simulating a 2OOA monomer and using its associated STID map within JabberDock to predict the 2OOB complex yielded no successful results. On the other hand, generating a STID map using a monomer extracted from the simulation of its dimer gave intermediate quality results. This indicates that the dynamics of a Cbl-b ubiquitin ligase as part of a homodimer or a heteromultimer were similar, and this similarity could be harnessed to improve the predictive power of our surface complementarity scoring. This approach was also tested with the significantly larger integrin I domain of complement receptor 3 complex (PDB: 4M76), but in this scenario, no good pose was found. Thus, protein docking involving small proteins, and possibly very flexible ones, may benefit from the information about their bound dynamics extracted from other known complexes these proteins are part of.

**DISCUSSION AND CONCLUSIONS**

We have presented STID maps, a strategy to represent how a molecule is perceived by its immediate surroundings. Our physical formalism encompasses the localized electrostatic nature of the space occupied by a molecule, and the dynamics of the protein itself, into a series of local dipole vectors, which is ultimately cast into a volumetric representation.

We have demonstrated that the average STID quantity of each protein is linearly anticorrelated with the ratio between protein SASA and molecular weight, S_un and that typical structural elements are always discernible at the same isovalue, independently from the protein under study (Figure 2b). This means that proteins with a similar mass and aspect but a different secondary structure will have a different D_avg value. This is because different secondary structure elements contribute to the STID voxel system in different ways,
determined by their characteristic structure and dynamics. For instance, a greater number of unstructured coils will produce a greater number of occupied voxels as the protein explores a relatively greater region of the available space, but these will have smaller associated nonzero STID values, decreasing $D_{\text{avg}}$. In previous electron density modeling and 3D reconstruction software yielding volumetric representations, the choices of isovalue cutoff to display isosurfaces have been arbitrary.\textsuperscript{29} Their choice is often chosen based on what is deemed by the authors to be most appropriate for the work, with no clear link made between a defining characteristic of a protein and the isosurface shown. In contrast, this work has shown that our STID map-based representations can be directly related to a physical and easily measurable quantity.

We have then shown that STID map representations are suitable for the definition of an accurate protein–protein docking scoring function. To this end, we have performed a comprehensive set of benchmarks to determine the optimal value of each parameter required for the construction and usage of STID maps for protein docking. The results show that JabberDock can provide predicted complexes on par with a competitive range of blind protein–protein docking software and is highly robust across a range of difficult cases—an achievement not observed in other docking algorithms. The strength of JabberDock to yield comparable results across the data set indicates that the ability of the STID maps to encapsulate high-frequency atomic motions accommodates for different amounts of flexibility in interacting proteins. In the case of complexes characterized by flat and relatively featureless binding sites, the surface complementarity function is likely to fail in highlighting a single most suitable docking position. On the other hand, when an interface is exceedingly complex, small perturbations about the docked pose are likely to lead to clashes, hindering the optimizer in its exploration of this region of the energy landscape. These represent JabberDock’s boundary conditions. The successful (and most typical) docking cases feature topographical complexities that enable both the scoring function and the optimizer to work harmoniously and effectively. This is the significant middle ground where the coupling of POW\textsuperscript{30} and STID maps provides excellent results, as indicated by the prediction of accurate protein complexes for most of the benchmark. These observations are expected to hold for any complex not requiring refolding or domain-level movements at the interface between binding partners.

JabberDock utilizes two individual PDB files with a well-parameterized force field to generate STID maps. These are used to guide the docking process, at the end of which all candidate models, typically several thousand, are clustered and returned to the user (in this work, 300 solutions are returned). The models themselves are built using the last snapshot from the pool of conformations explored by the binding partners in their respective MD simulations. Combinations of other conformations within the monomers’ simulations (see Figure S9) and dimeric arrangements within the full collection of candidate assemblies may be closer to that found in the crystallized bound state. In future versions of JabberDock, we will explore the possibility of leveraging on this additional source of structural information to provide the user with more accurate models.

We have observed that using a protein’s STID map reporting on its dynamics when bound to an alternative complex can improve JabberDock’s performance. While our benchmark shows that docking proteins represented by the STID map of their monomeric state yield a good number of successes, more accurate predictions may be obtained by harnessing the dynamics of the bound complex. Other areas of future investigation will include the adoption of different functions as a model for the pseudo-electron density (e.g., a Lorentzian), using JabberDock for rescoring models predicted by other protein docking methods, a reranking process building upon our preliminary results on the usage of a dipole complementarity score, the use of a different atomistic force field (including a polarizable one) to explore the impact on the STID maps, and an additional post-processing step based on MD or MC techniques to refine the best docking poses. In this context, we also foresee that the use of optimization algorithms requiring no weighting could be beneficial.\textsuperscript{30} Overall, enhancements in the scoring function and solutions reranking will help improve the performance of JabberDock against cases with low interface complexity, while refining the optimization engine will reinforce its performance against cases with highly complex ones.

### METHODS

**Molecular Dynamics.** All simulations are run on the GROMACS\textsuperscript{31} MDs engine, with Amber14sb force field.\textsuperscript{32} Systems are prepared by immersing the protein of interest in a TIP3P water box, neutralized with Na$^+$ or Cl$^-$ counterions. The system is then energy-minimized using a steepest descent algorithm, with a tolerance threshold set to 200 kJ mol$^{-1}$ nm$^{-1}$. The initial step size is set to 1 pm, the maximum number of allowed steps to 5 × 10$^5$. The cutoffs for both Coulombic and van der Waals interactions are set to 1.2 nm.

The protein is then equilibrated for 500 ps within a canonical ensemble, with $T$ set to 310.15 K with 2 fs step size and the constraint algorithm LINCS applied to the bonds.\textsuperscript{33} A particle mesh Ewald summation is used to treat long-range interactions and a velocity-rescale temperature coupling method applied separately to protein and nonprotein atoms; the coupling constant is set to 0.1 ps.Velocities are randomly assigned from a Boltzmann distribution of velocities at $T$.

Finally, production occurs over a 500 ps timescale, for reasons shown in Figure S1, in an isothermal–isobaric ensemble. $T$ is set as mentioned above; the pressure is set to 1 bar. Berendsen temperature and pressure coupling methods are used, again keeping the protein and nonprotein groups separate. The temperature coupling is as mentioned above, with the pressure coupling constant set to 10 ps. The compressibility for both is set to $4.5 \times 10^{-5}$ bar$^{-1}$. Atomic coordinates are saved every 5 ps.

**Particle Swarm Optimization.** An initial starting point with the two input monomers’ center of mass centered at the origin is used prior to generating any models. JabberDock uses a seven-dimensional space for implementation comfort when roto-translation the STID maps: three dimensions define ligand translation in the Cartesian space, three dimensions define an axis of rotation for this ligand, and one dimension defines a rotation angle around this axis. The translation values are limited by the size of the receptor, the axis of rotation is normalized (and thus has values ranging from $-1$ to $1$), and the rotation angle in radians ranges between 0 and $2\pi$.

In order to navigate the potential energy surface (PES) associated with the scoring function (see the next section) and produce an ensemble of possible docked poses, JabberDock leverages a distributed heuristic global optimization algorithm.
featured in the POW\textsuperscript{er} optimization environment—PSO “kick and reseed” (PSO-KaR).\textsuperscript{26} PSO-KaR was used to explore the PES over 300 iterations using 80 randomly initialized agents (“particles”). According to the “kick and reseed” procedure, particles converging to a local minimum (i.e., with a velocity decaying to less than 4\% of the search space dimension in each direction) were randomly restarted, and a repulsion potential placed at their convergence location. The whole optimization process was repeated three times, with the memory of previous repulsion potentials retained from one repetition to the next. In sum, this docking procedure requires the evaluation of 72,000 docking poses. To obtain a diverse ensemble of solutions, 300 poses were finally selected as representatives from the pool of poses having a positive score using a K-means clustering algorithm on the seven-dimensional coordinates associated with each model.

JabberDock’s Scoring Function. JabberDock uses a surface complementarity assessment that takes advantage of the STID maps to generate the PES explored by the PSO algorithm implemented in the POW\textsuperscript{er} optimization engine.

Following a roto-translation of a model requested by the optimizer, a quick test is first performed to identify poses featuring no contact or unphysical atomic overlaps between the ligand and the receptor. Suitable poses, featuring a negative Lennard-Jones potential between the carbon atoms of receptor and ligand, are scored according to their surface complementarity S. The shape of the isosurfaces analyzed by JabberDock is determined by an isosurface cutoff, and an appropriate value of 0.43 was chosen based on the benchmark discussed in Figures S6 and S7. The score between the STID of the receptor and that of the ligand is given by

\[ S = \frac{|S_{AB}| + |S_{BA}|}{2} \]

where the curly brackets indicate that we used the median of the score for protein A into B and vice versa, where the scores are given by

\[ S_{AB} = (n_{A} \cdot n_{B}) \exp(-w |x_{A} - x_{B}|^{2}) \frac{\nu_{A}}{V_{A}} \]

where \( n_{A} \) is the normal from a region of interest on A’s surface and \( n_{B} \) the antinormal from the closest point on B to that point on A. \( w \) (0.5 Å\textsuperscript{2}) is an arbitrary weighting found by Lawrence & Coleman\textsuperscript{34} and \( x_{A} - x_{B} \) is the physical distance between the two points. \( \nu_{A} \) is the total number of successful contact points on A in contact with B inside some arbitrary distance cutoff, and an optimal cutoff of 1.6 Å was chosen based on the work discussed in Figures S3–S5. \( V_{A} \) is the total number of points describing the surface of A. These last two terms are used to avoid minor contact points providing good scores. The larger the S, the better the fit; thus, the optimizer is set up to maximize the score. Only positive scores are accepted by POW\textsuperscript{er}. Figure S10 provides examples of how these scores match with a corresponding rmsd and \( f_{\text{nat}} \) for three complexes.

STID Benchmark. Totally, 118 nonredundant proteins (maximum 30\% homology) were extracted from the PDB-REDO databank.\textsuperscript{55} All structures were soluble proteins featuring solely standard amino acids, none required the application of a biomatrix, and all were composed of more than 30 amino acids.

The SASA of each structure in the benchmark set was calculated using the Shpak–Rupley algorithm,\textsuperscript{24} with the solvent probe radius set to 1.4 Å to represent that of water. For each protein, we report the average SASA over 500 ps production cycle (one structure every 5 ps, excluding the first 50 ps). Molecular weights were calculated accounting for all atoms present in the atomic structures.

Case Difficulty Classification. Protein–protein docking cases are classified under three levels of difficulty which is associated with their flexibility and the rmsd difference between the Cα atoms at the interface after superposing the bound and unbound interfaces. Cases can be classified as either rigid-body (or easy), medium difficulty, or difficult. Easy cases are those with minimal difference between the unbound crystalized structures and the bound: usually <1 Å difference. In medium cases, the rmsd difference is between 1 Å and ∼2.5 Å. Finally, difficult cases can be anything greater than 2.5 Å. Thus, the difficult cases are accordingly significantly more difficult than the other two, particularly given that the requirements for an acceptable success are close to the upper boundaries that define the difficult cases.

Assessment of Model Accuracy. We use three metrics to determine the quality of a model: the ratio of correct contact residues (a valid contact defined as an atom within 5 Å of the binding partner) to the number of residues in the predicted complex \( f_{\text{nat}} \) the rmsd between the carbon atoms of the known crystal pose and the predicted pose, and the rmsd of the two poses between the carbon atoms at the interface (defined as within 10 Å of the binding partner). CAPRI guidelines specify four levels of possible success criteria: (1) incorrect, where rmsd > 10.0 Å and interfacial rmsd > 4.0 Å OR \( f_{\text{nat}} < 0 \); (2) acceptable quality, where rmsd ≤ 10.0 Å or interfacial rmsd ≤ 4.0 Å and 0.1 ≤ \( f_{\text{nat}} < 0.3 \) OR \( \text{interfacial rmsd } > 0.3 \) and rmsd > 5.0 Å and interfacial rmsd > 2.0 Å; (3) intermediate quality, where rmsd ≤ 5.0 Å or interfacial rmsd ≤ 2 Å and 0.3 ≤ \( f_{\text{nat}} < 0.5 \) OR \( \text{interfacial rmsd } ≥ 0.5 \) and rmsd > 1.0 Å and interfacial rmsd > 1.0 Å; and (4) high quality, where rmsd ≤ 1.0 Å and interfacial rmsd ≤ 1.0 Å and \( f_{\text{nat}} ≥ 0.5 \). The protocol for applying this list of inequalities follows the order provided, beginning with defining the incorrect predictions. In the text, we qualify the result of a test as of high, intermediate, or acceptable quality if at least one in the top 10 ranked models matches the criteria above.

Software Implementation. Software to generate STID maps is developed in Python, using numpy, scipy, and cython packages. An automated bash script that prepares all the necessary GROMACS files and runs them is used to generate the trajectories. JabberDock is implemented as a POW\textsuperscript{er} Python module. All software is freely available at github.com/degical/JabberDock.

\section*{ASSOCIATED CONTENT}

\section*{Supporting Information}

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.jctc.9b00474.

Analysis of side chain motion convergence during MD simulations; determination of voxel size parameters for STID maps; benchmark on the best choice of isovalue for the STID map and cutoff for the distance between two surfaces during docking; mathematical details for the dipole alignment reranking method that can be employed; information on computational resources used and associated execution times; analysis of the quality of the best docked pose within the top 100 results for each protein; analysis of rmsd variation observed during the MD simulations; comparison of docking score versus
rmid and $f_{\text{nat}}$ for three example protein complex cases; and analysis of relationship between mass of protein complex and time to complete the POW™ optimization search (PDF)

Results for all cases in the protein docking benchmark; for each of the easy, medium and difficult cases (and a subset of bound cases therein): highest ranking acceptable and intermediate results; lowest rmsd in the top 10 poses, with corresponding rank, $f_{\text{nat}}$ and interfacial rmsd; the largest $f_{\text{nat}}$ in the top 10 poses, with corresponding rank, and rmsd and interfacial rmsd (XLSX)

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