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The impact of thermal winds on the outburst lightcurves of black hole X-ray binaries

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\textbf{ABSTRACT}

Context. The observed signatures of winds from X-ray binaries are broadly consistent with thermal winds, which are driven by X-ray irradiation of the outer accretion disc. Thermal winds produce mass outflow rates that can exceed the accretion rate in the disc. Aims. We aim to study the impact of thermal wind mass loss on the stability and lightcurves of black hole X-ray binaries subject to the thermal-viscous instability driving their outbursts. Strong mass loss could stop outbursts early, as proposed for the 2015 outburst of V404 Cyg.

Methods. We used an analytical model for thermal (Compton) wind mass loss as a function of radius, X-ray spectrum, and luminosity that was calibrated against numerical simulations. We also estimated the fraction of the X-rays, emitted close to the compact object, that are scattered back to the outer disc in the wind. Scattering in the thermal wind couples irradiation to the disc size and inner mass accretion rate. The disc evolution equations were modified to include this wind mass loss and the varying irradiation fraction.

Results. Scattering in the strong wind expected of long $P_{\text{orb}}$ systems enhances the irradiation heating of the outer disc, keeping it stable against the thermal-viscous instability. This accounts very well for the existence of persistently bright systems with large discs, such as Cyg X-2, 1E 1740.7–2942, or GRS 1758–258. Mass loss from the thermal wind shortens the outburst, as expected, but it is insufficient in explaining the rapid decay timescale of black-hole X-ray binary outbursts. However, including the wind-related varying irradiation fraction produces lightcurves with plateaus in long $P_{\text{orb}}$ systems like GRO J1655–40. Plateau lightcurves may be a dynamical signature of enhanced irradiation due to scattering in thermal winds.

Conclusions. Mass loss due to thermal winds is not a major driver for the outburst dynamics up to luminosities of 0.1–0.2 $L_{\text{Edd}}$. Higher luminosities may produce stronger mass loss but studying them is complicated since the wind becomes opaque. Magnetic winds, which extract angular momentum with little mass loss, seem more promising to explain the fast decay timescales generically seen in black-hole X-ray binaries. Thermal winds may play an important role in the outburst dynamics through the varying irradiation heating. This may be evidenced by relating changes in wind properties, X-ray spectra, or luminosity with changes in the optical emission that traces the outer disc. Simulations should enable more accurate estimates of the dependence of the irradiation onto the disc as a function of irradiation spectrum, radius, and disc wind properties.

Key words. accretion, accretion disks – binaries: close – stars: black holes – stars: winds, outflows – X-rays: binaries

1. Introduction

Recurring outbursts due to the hydrogen ionisation disc instability provide test beds for constraining key aspects of accretion processes (Lasota 2001). These are seen from compact objects of all types, but the black-hole X-ray binaries (BHXBs) are of particular interest. Their bright X-ray and optical outbursts typically last hundreds of days and recur on timescales of years (Tetarenko et al. 2016). This provides an opportunity to study accretion over astrophisically interesting and observable timescales.

The large change in the mass accretion rate through the disc produces a distinct pattern of spectral change; the system cycles between hard (dominated by Comptonised emission) and soft (dominated by thermal disc emission) accretion states. This is generally interpreted as a change in the nature of the accretion flow from a hot, optically thin, geometrically thick solution (such as an advection dominated accretion flow: ADAF) to a cool, geometrically thin standard disc (McClintock & Remillard 2006; Done et al. 2007).

X-ray irradiation from either the inner disc or the hot inner flow can illuminate the outer disc. This makes a major contribution to the thermal balance at large radii, so the optical emission is dominated by reprocessed X-rays (van Paradijs & McClintock 1994; van Paradijs 1996). This irradiation heating changes the dynamics of the transient outburst as it prevents hydrogen recombing, thus keeping the outer disc in the hot state and prolonging the outburst timescale (King & Ritter 1998; Dubus et al. 2001).

The accretion energy also powers two different types of outflows, which change with accretion state. First, there is a compact, steady jet. This jet is associated with the hot flow, so the collapse of the flow at the spectral state transition leads to strong suppression of the radio jet emission. However, it can restart at higher luminosities, in correlation with the strength of the X-ray corona (very high and steep power law state). Second, there are strong equatorial disc winds that are associated with the disc dominated states, but they seem to disappear in the hard state (Miller et al. 2006; Ponti et al. 2012; Neilsen 2013;
There are a number of possible explanations for the suppression of wind features in the hard state, including: (i) a causal connection, which has the magnetic field configuration changing to power a jet in the hard state and a wind in the soft state (Neilsen & Lee 2009; Miller et al. 2012); and (ii) correlation, where the changing spectral shape during state transitions results in complete ionisation of the wind material in the hard accretion state (Chakravorty et al. 2013; Higginbottom & Proga 2015). The former mechanism assumes that the wind is magnetically launched, in which case, it can also contribute to or even completely control the angular momentum transport in the accretion flow (Blandford & Payne 1982; Ferreira & Pelletier 1995; Scepi et al. 2018). All winds change the disc instability timescales by removing mass from the disc, but magnetic winds should change the disc instability timescales further by enhancing the angular momentum transport as well (Scepi et al. 2019).

However, there are other wind launch mechanisms, such as radiative or thermal driving, which remove matter from the flow without torquing the disc. Radiative driving becomes important only for $L \gg L_{\text{Edd}}$ (assuming no additional opacity beyond electron scattering), but thermal driving inevitably produces “Compton” winds from irradiation of the outer disc. X-ray heating by irradiation from the inner disc forms a dilute, isothermal “Compton” winds from irradiation of the outer disc. X-ray radiative or thermal driving, which remove matter from the flow (Scepi et al. 2019).

This gave quantitative measurements of the $\alpha$ viscosity (Shakura & Sunyaev 1973), the parameter which encapsulates the efficiency of this transport process, in these discs. While numerical simulations of the magneto-rotational instability (Balbus & Hawley 1998), which is thought to be the physical mechanism behind angular momentum transport in accretion discs, yield values of $0.1 < \alpha < 0.2$ with zero net magnetic flux (Hirose et al. 2014; Coleman et al. 2016; Scepi et al. 2018). Tetarenko et al. (2018a) derive values of $\alpha$ that are significantly higher, between 0.2 and 1. As $\alpha$ is directly related to the viscous timescale of the accretion flow through the disc, a higher $\alpha$ during outburst corresponds to a disc that will accrete mass more quickly, resulting in a shorter outburst duration than would normally occur. Tetarenko et al. (2018a) propose that the high values of $\alpha$ derived, and in-turn shorter than expected outburst durations observed, in BHXB discs, may be evidence for significant amounts of mass (and/or angular momentum) being lost from the disc through wind type outflows during these outbursts (Mineshige et al. 1993).

We explore the mass loss possibility by incorporating thermal winds into the disc instability code. We adopt the wind parametrisation described by Done et al. (2018), which gives us the wind mass loss rate in the disc as a function of luminosity. This parametrisation typically predicts that the wind outflow rate $\dot{M}_w$ can be several times the accretion rate through the disc, when the disc is large compared to the Compton radius, in agreement with the latest simulations (Higginbottom et al. 2019; Tomaru et al. 2019) and observations (Shidatsu & Done 2019). We use this wind to scatter the central flux down onto the disc, providing a physical quantitative estimate for the size of this effect to replace the previous ad hoc irradiation parameter (i.e., C; Dubus et al. 1999). The wind strength increases with disc size and luminosity, so the scattered fraction is not constant, but changes during the outburst. We incorporate this effect in addition to the wind mass loss, and calculate the resulting disc instability lightcurves. We find notable differences in the outburst timescales, including the first calculations showing extended plateaus in the lightcurves, a feature often seen in the data, but not reproduced by any previous models. The models do not currently reproduce the apparent high $\alpha$ viscosity values, which could indicate that there is an additional magnetic angular momentum transport mechanism. However, we caution that these simulated outbursts currently only reach moderate luminosities of $0.1-0.2 L_{\text{Edd}}$, so they are not yet directly comparable to many of the observed systems (Yan & Yu 2015; Tetarenko et al. 2016).

The paper is organised as follows. Section 2 provides a description of the model. Section 3 explains how thermal winds change the disc structure and stability. Section 4 presents power law state (Homan et al. 2016) and optical/IR winds are detected via PCygni line profiles in H$\alpha$ and He$\alpha$ in the hard state (e.g., V4641 Sgr and MAXI J1820+070; Muñoz-Darias et al. 2018, 2019).
our results for one short period and one long period system. Section 5 discusses these selected models of outbursting BHXBs. We conclude in Sect. 6.

2. The accretion disc model

2.1. The disc equations

In the presence of mass loss from a wind, the continuity equation is rewritten with an additional loss term

\[
\frac{\partial \Sigma}{\partial t} - \frac{1}{2\pi r} \frac{\partial M}{\partial r} = -\Sigma_w
\]  

(1)

and the specific angular momentum conservation equation becomes

\[
\Sigma \frac{\partial^2 \Omega}{\partial t} - \frac{M}{2\pi r} \frac{\partial^2 \Omega}{\partial r} = \frac{1}{\Omega} \frac{\partial}{\partial r} \left( r^2 \nu \Sigma \frac{\partial \Omega}{\partial r} \right) - j \Sigma_w
\]  

(2)

where \( j = 2 \) is the excess specific angular momentum carried away by the wind (Papaloizou & Lin 1995). Unlike magnetic winds, thermal winds are not expected to drive excess angular momentum loss so we took \( j = 0 \) (Knigge 1999). We also assume a Keplerian rotation profile, as appropriate for thin accretion discs, so the first term of Eq. (2) drops out. Hence, the only change to Dubus et al. (2001) is the continuity equation. We define the wind mass loss rate at a radius \( R \) as

\[
M_w(R) = \int_R^{R_{\text{out}}} 2\pi r \Sigma_w \, dr,
\]

(3)

so that the total mass outflow rate in the wind is \( M_w(R_{\text{out}}) \).

2.2. The disc wind

The \( \Sigma_w \) term due to the thermal wind is the \( \dot{n} \) given by Eq. (4.8) from Woods et al. (1996), using the assumptions appropriate to X-ray binaries set out in Done et al. (2018). We refer to these papers for the complete expression of this term. The wind is all the more important that the disc is large and the luminosity is high. The X-ray irradiation luminosity is taken to be \( L = \epsilon M_\text{in} c^2 \) with the radiative efficiency \( \epsilon \) as defined in Dubus et al. (2001), and \( M_\text{in} \equiv M(R_\text{in}) \).

The thermal wind is effective for radii \( R > 0.2 R_\text{IC} \), with the Compton radius \( R_\text{IC} \) set as

\[
R_\text{IC} \approx 10^{12} \left( \frac{M}{10 M_\odot} \right) \left( \frac{10^7 K}{T_{\text{IC}}} \right) \left( 1 - \sqrt{\frac{L}{L_{\text{Edd}}} \right)} \text{ cm},
\]

(4)

where \( M \) is the compact object mass, \( T_{\text{IC}} \) is the Compton temperature of the impinging radiation, and we include a rough correction to take into account radiation pressure on electrons at luminosities close to Eddington (Proga & Kallman 2002; Done et al. 2018).

We followed the assumptions set out in Done et al. (2018). In particular, a switch in Compton temperature \( T_{\text{IC}} \) occurs between hard and soft state due to the major change in X-ray irradiation spectrum. The state transition is taken to occur at a fixed luminosity \( L \approx L_{\text{Edd}} \approx 0.02 \) with (Eqs. (8) and (9) of Done et al. 2018)

\[
T_{\text{IC}} = \begin{cases} 
\frac{4.2 - 4.6 \log(l/0.02)}{0.36 \left( \frac{L}{L_\odot} \right)^{1/4}} & \text{if } l < 0.02 \text{ (hard state)} \\
\frac{1}{2} \log(l/0.02) & \text{if } l \geq 0.02 \text{ (soft state)}.
\end{cases}
\]

(5)

In the hard state, \( T_{\text{IC}} \) decreases slowly from \( \approx 10^8 \) K at \( l = 10^{-4} \) to about \( 4 \times 10^7 \) K at \( l = 0.02 \), where it abruptly switches to the soft state with \( T_{\text{IC}} \approx 4 \times 10^6 \) K, increasing slowly to \( 10^7 \) K at \( l = 1 \) (see top panel of Fig. 5 in Done et al. 2018). To avoid the discontinuity at \( l = 0.02 \), we smoothly switch \( T_{\text{IC}} \) according to

\[
T_{\text{IC}} = \frac{1}{x + 1} + \frac{8}{1 + x} \left( \frac{l}{0.02} \right)^6.
\]

(6)

\( T_{\text{IC}} \) and \( T_{\text{SS}} \) are the Compton temperature in the hard and soft state, respectively. We verified that this choice, which eases the computations, is of no consequence to the lightcurves.

A thermal wind is more easily produced in the hard state than in the soft state, due to the smaller \( R_\text{in} \) (higher \( T_{\text{IC}} \)), and can be quenched during the transition to the soft state due to the increase in \( R_\text{IC} \). However, the ratio of the mass loss rate in the wind to the mass accretion rate in the inner disc also increases with luminosity up to the critical luminosity,

\[
L_{\text{crit}} \approx 0.09 \left( \frac{10^7 K}{T_{\text{IC}}} \right)^{1/2} L_{\text{Edd}}.
\]

(7)

This critical luminosity is set by the balance between the Compton heating timescale and the dynamical timescale of the disc at the Compton radius (Woods et al. 1996). In practice, the outflow rate in the wind is about two to five times the mass inflow rate in the disc for \( l \gtrsim 0.001 \) (bottom panel of Fig. 5 in Done et al. 2018). We expect thermal wind mass loss to be dynamically important for discs with an outer radius \( R_{\text{out}} \approx 2 \times 10^{11} \) cm for a 10 M_\odot black hole, meaning for long \( P_{\text{orb}} \) binaries. We do not take into account that the forward transition (from the hard to soft state) occurs at a higher luminosity during the outburst rise than the backward transition (from the soft to hard state) because of the hardness – intensity hysteresis.

2.3. Irradiation heating

The irradiation flux heating the accretion disc at a radius \( R \) is defined as

\[
F_{\text{irr}} \equiv \sigma T_{\text{irr}}^4 \approx C \frac{L}{4\pi R^2},
\]

(8)

where \( C \) encapsulates uncertainties in the geometry and albedo of the outer disc irradiation by X-rays (Tuchman et al. 1990; Dubus et al. 1999). Typically, \( C \) is assumed to be a constant of value \( \approx 5 \times 10^{-3} \) (see Tetarenko et al. 2018b and references therein). For comparison, Kimura & Done (2019) considered direct irradiation of an isothermal disc by a central point source

\[
C = (1 - A) \frac{H}{R} \left( \frac{\partial H}{\partial \ln R} - 1 \right) \approx 10^{-3} \left( \frac{R_{\text{out}}}{R_{\text{IC}}} \right)^{2/7},
\]

(9)

assuming \( H/R = f_{\text{full}}(R/R_{\text{out}})^{2/7} \) with \( f_{\text{full}} = 4 \times 10^{-2} \) and (1 – \( A \)) = 0.1 (Cunningham 1976; Vrtilek et al. 1990). This results in \( C \approx R^{2/7} \) while a standard Shakura Sunyaev disc would give \( C \approx R^{1/8} \) (Cunningham 1976), hence the dependency of \( C \) with radius is weak in both cases. We note that \( L = \epsilon M_\text{in} c^2 \) with \( \epsilon \) changing throughout the outburst to reflect the reduced radiative efficiency when an ADAF is present (see Dubus et al. 2001 for details).

In principle, the thermal irradiating the outer disc and the conditions for launching a thermal wind are related not only by \( L \) but also by the underlying irradiation geometry (the \( C \) parameter). The thermal wind may itself provide a medium to scatter X-ray photons to the disc. This is attractive since point...
source irradiation is known to be insufficient to explain the stability of persistent X-ray binaries: the cold, outer region that should be irradiated has a smaller scale height than the hotter, inner region and is thus shadowed from the X-ray source (Meyer & Meyer-Hofmeister 1982; Cannizzo et al. 1995; Dubus et al. 1999; Kim et al. 1999). The irradiation geometry must allow the X-ray flux to irradiate the outer disc, for example because the X-ray source is a "lamp post" above the disc, because the disc is warped, or because the X-ray flux is scattered in a corona or wind above the disc. Kimura & Done (2019) estimated the scattered fraction in the thermal wind to be comparable to or higher than \( f_{\text{out}} \), in agreement with the earlier results of Ostriker et al. (1991) who studied the scattered fraction in a Compton heated corona (i.e. when \( R \lesssim 0.1 R_{\text{IC}} \)) and found that it dominates over direct irradiation when \( L \gtrsim 0.01 L_{\text{Edd}} \) (see their Sect. 7.4). We explored this idea by having \( C \) vary according to

\[
C = \int_0^1 \int_{R_{\text{in}}}^{R_{\text{out}}} \sigma_T n_m \mu \, dm \, dr \approx \frac{\sigma_T \dot{M}_m}{8 \pi R_m n_m m_i} \propto L \log \left( \frac{R_{\text{out}}}{R_{\text{in}}} \right) \tag{10}
\]

with \( n_m \) the wind density, \( \mu \) the mass-weighted wind outflow rate, \( m_i \) is the mean ion mass per electron and \( \mu = \cos i \) (see Eq. 6) in Done et al. 2018, and the wind property dependencies given in Hori et al. 2018). \( C \) is basically the angle-averaged Thomson opacity of the wind, which is \( \ll 1 \) in most cases investigated here. All the major dependencies on \( T_{\text{IC}} \) cancel out, so the scattered fraction correlates directly with \( L \), with the Compton temperature only indirectly contributing via \( R_{\text{in}} = 0.2 R_{\text{IC}} \) in the logarithm.

### 3. Impact of thermal winds on the stability of X-ray binaries

#### 3.1. The radial structure of a stationary disc with a thermal wind

Figure 1 compares the radial structure of stationary solutions \( \dot{M} = 0 \) with and without a thermal wind. The disc size \( R_{\text{out}} = 1.6 \times 10^{12} \text{ cm} \) and the mass transfer rate \( \dot{M}_t = 3 \times 10^{39} \text{ g s}^{-1} \) are large so as to maximise the effect of the thermal wind. The compact object is a \( 12 M_\odot \) black hole so the orbital period of the binary would be around 10 days, implying this is a large system. The accretion luminosity is slightly super-Eddington without a thermal wind (dashed lines in Fig. 1). The irradiation constant is \( C = 0.01 \) so the outer disc is hot and stable. This value of \( C \) was chosen to be close to the value derived from scattering in the wind \( (C \approx 0.05 \text{ using Eq. (10)}) \) while still allowing for the outer disc to be unstable when a wind is included, as we now explain.

With a thermal wind, the mass accretion rate through the disc becomes a function of \( R \) with

\[
\dot{M}_t - \dot{M}(R) = \dot{M}_m(R). \tag{11}
\]

The total mass lost to the wind over the whole disc is \( \dot{M}_m(R_{\text{in}}) \approx 2.3 \times 10^{39} \text{ g s}^{-1} \). The top panel shows that \( \dot{M}(R) \lesssim R^{1/2} \) in the outer regions, becoming constant where \( \Sigma_m = 0 \), which is for \( R < 0.2 R_{\text{IC}} \). The lower panel shows the luminosity of \( \approx 0.35 L_{\text{Edd}} \). The outer regions now reach the critical temperature for hydrogen recombination, signalled by a jump in surface density \( \Sigma \) (the solution is forced to follow the unstable middle branch of the S curve). Another way to see this is to note that Eq. (2) can be rewritten,

\[
\frac{\partial}{\partial r} \left( \Sigma \nu \nu^{1/2} \right) = \frac{M}{6 \pi r^{1/2}} \approx \frac{M}{6 \pi R_{\text{out}}^{1/2}}, \tag{12}
\]

given the scaling with radius of \( M \). This implies that \( \nu \Sigma \approx M/6\pi \), a factor 2 lower than in a standard disc (where \( M \) would be constant with radius). Since \( \nu \approx \Sigma \), the heating is decreased by a factor 2. Thus, the thermal wind destabilises an accretion disc that would otherwise be stable. However, increasing \( C \) to 0.04 would be sufficient to stabilise the disc again. In fact, \( C \approx 0.05 \) when calculated from the scattering in the wind (Eq. (10)). A self-consistent determination would thus have found the disc remained stable even with a thermal wind, as we now explain.

#### 3.2. The stability diagram

The disc instability model separates stable X-ray binaries from transients in the \((P_{\text{orb}}, M_t)\) plane (van Paradijs 1996; Coriat et al. 2012; Tetarenko et al. 2016). Thermal winds can have three effects. First, as demonstrated above, they can destabilise long \( P_{\text{orb}} \) systems accreting at very high rates. Second, they lead to an underestimate of the mass transfer rate \( \dot{M}_t \) if the mean X-ray luminosity is used to estimate it. For example, the mass transfer rate would be underestimated by a factor \( \dot{M}(R_{\text{out}})/\dot{M}(R_{\text{in}}) \approx 4 \) for the disc shown in Fig. 1. Coriat et al. (2012) proposed this to explain why Cyg X-2 is stable although its estimated \( M_t \) places it in the unstable region of the instability diagram. Finally, the value of \( C \) is not constant with the disc size \((P_{\text{orb}})\) and the mass transfer rate anymore, but it depends on the wind properties.

Figure 2 shows the impact on the stability curve of thermal winds, taking into account all these effects. The usual stability criteria are shown as grey lines. For the non-irradiated case, this is,

\[
M_{\text{crit}} \approx 8.07 \times 10^{15} R_{10}^{2.64} M_1^{0.89} \text{ g s}^{-1}, \tag{13}
\]
Equation (14) becomes a non-linear equation to be solved when \( C \) is taken from the scattered fraction, so that it becomes dependent on \( R_{\text{out}} \) and accretion rate \( M_{\text{in}} \). A self-consistent solution gives the \( M_{\text{in}} \) that provides the right \( C \) for the disc to be stable at \( M_{\text{in}} \) when irradiated by a luminosity \( L = \epsilon M_{\text{in}} c^2 \). Here, we assumed \( \epsilon = 0.1 \). We took the solution with the lowest \( M_{\text{in}} \) when two solutions to the equation were possible, one in the soft state and one in the hard state. Two solutions exist in a narrow region close to the transition luminosity. This could lead to a situation in which a system is stable with the hard state \( T_{\text{IC}} \) yet unstable if it switches to the soft state \( T_{\text{IC}} \), due to a weaker wind and \( C \). We have not investigated this further as it depends on the assumed form of the transition between states (Eq. (6)).

The red line shows the resulting self-consistent \( M_{\text{in}} \). The yellow line shows \( M_{\text{f}} M_{\text{in}} + M_{\text{a}}, \) showing that the mass transfer rate from the companion is much higher than the accretion rate at \( P_{\text{orb}} \). The \( M_{\text{in}} \) stability line is flatter than in the case with no wind and constant \( C \). This is because \( C \) increases with longer \( P_{\text{orb}} \) as the disc becomes larger and the wind stronger. The stability curve joins the non-irradiated standard one at short \( P_{\text{orb}} \) because the wind and, correspondingly, \( C \) are weak for small discs. The kink or jump in the curve at \( P_{\text{orb}} \approx 7 \) h is due to the hard to soft switch at \( L = 0.02 L_{\text{Edd}} \). This jump is stronger for black holes than neutron stars because it occurs at a higher absolute luminosity whereas the disc sizes remain similar. The location of the jump and its amplitude depend on the assumptions made on \( T_{\text{IC}} \) and the transition luminosity between states (Eq. (5)). In particular, we use the same assumptions for black holes and neutron stars, which may not be appropriate. A higher \( T_{\text{IC}} \) would move the jump to longer \( P_{\text{orb}} \) and reduce its amplitude.

The data for the different systems are taken from Coriat et al. (2012), supplemented by data from the WATCHDOG catalogue for 6 transient black-hole systems: MAXI J1305−704, Swift J1357.2−0933, V4641 Sgr, MAXI J1836−194, Swift J1745 10.8−262411, XTE J1859+226 (Tetarenko et al. 2016). They calculated the time-averaged average mass accretion rate of each system from their long-term X-ray lightcurves with some assumptions on \( \epsilon \). These values thus do provide an average \( M_{\text{in}} \) to compare to the red line.

Figure 2 shows that the stability line separates extremely well persistent systems from transients with no free parameters. The agreement is improved for long \( P_{\text{orb}} \) sources. Indeed, Cyg X-2 (at \( P_{\text{orb}} = 236 \) h in the left panel) is now above the stability line for neutron stars. For black holes, 1E 1740.7−2942 (\( P_{\text{orb}} = 305 \) h) and GRS 1758−258 (\( P_{\text{orb}} = 443 \) h) are two persistent or long duration outburst sources that are now very close to the stability line. However, we strongly caution that the derived \( C \) become unphysical for long \( P_{\text{orb}} \) since the wind becomes Compton thick: \( C \approx 0.1 \) for \( P_{\text{orb}} \approx 150 \) h (1.4 \( M_{\odot} \) neutron star) and for \( P_{\text{orb}} \approx 500 \) h (10 \( M_{\odot} \) black hole).

There are a few remaining discrepancies for BHXBs (see discussion in Coriat et al. 2012). 4U 1957+115 at \( P_{\text{orb}} = 9.3 \) h is persistent and in the unstable region, close to the jump caused by the change in \( T_{\text{IC}} \). The lower limit on its \( M \) comes from a lower limit on its distance. Cyg X-1 at \( P_{\text{orb}} = 134 \) h is also a persistent system in the unsteady region of the diagram. The leftward arrow on its symbol indicates the actual disc size of this wind-accreting system could be much smaller than the values derived from Roche lobe mass transfer. In both cases, a calculation with the observed \( T_{\text{IC}} \) for this system, rather than generic values, might reduce the discrepancy by moving the red line rightward.

4. Impact of mass loss on outburst lightcurves

4.1. A short orbital period system

First, we consider an unstable accretion disc around a \( M = 9 M_{\odot} \) black hole with a mass transfer rate \( M_{\text{t}} = 10^{16} \) g s\(^{-1}\). The disc has a size \( \approx 10^{14} \) cm, corresponding to an orbital period \( \approx 5 \) h. The disc has a viscosity parameter \( \alpha_{\text{visc}} = 0.2 \) in the hot state and \( \alpha_{\text{cold}} = 0.02 \) in the cold state, typical values that have been used in previous disc instability model calculations (Dubus et al. 2001). The irradiation parameter is assumed constant at \( C = 10^{-4} \).
Fig. 3. Outburst for a short orbital period black hole. Top panel: $\dot{M}(R_{in})$ (black solid line), $\dot{M}(R_{in})$ w (dashed line), $\dot{M}(R_{in})$ no wind mass loss for comparison (grey solid line, nearly superposed to the black solid line). Second panel: $R_{in}$ and $R_{out}$ (solid lines), radius of the heating/cooling front (dotted line), $0.2R_{in}$ (dashed line). Third panel: $L/L_{Edd}$ (solid line) and $L_{crit}/L_{Edd}$ (dashed line). Bottom panel: $C$ (solid line) and $C_{estimated}$ from Eq. (10) (dashed line).

matched to the expected average wind optical depth throughout the bright phase of the outburst. Below, we calculate the self-consistent $C$ as a function of time and see how the outburst changes. Figure 3 shows the outburst lightcurve with mass loss from the thermal wind taken into account. For comparison, the outburst lightcurve without the wind mass loss is shown as a grey line in the top panel of Fig. 3. Both lightcurves are virtually identical and we had to shift this grey line by 0.5 days to make it visible on the plot. The wind has negligible impact on the outburst lightcurve. The total wind mass loss rate peaks near the transition between hard and soft state ($l = 0.02$), where it is comparable to the mass accretion rate onto the black hole (dashed line, first panel). In the hard state, the Compton radius is located within the accretion disc (second panel) but the critical luminosity is above the accretion luminosity $L = \epsilon \dot{M}_{in} c^2$ (third panel), so the wind is mostly in the “gravity-inhibited” regime (regions C in Fig. 25 of Woods et al. 1996). In the soft state, the Compton radius is beyond $R_{out}$ and $L_{crit} > L$, so the wind is actually the very weak outflow from a non-isothermal corona (region D).

Fig. 4. Same as Fig. 3 except that $C$ is calculated self-consistently from scattering in the wind (bottom panel, solid line). Top panel: grey solid line shows $M_{in}$ for a non-irradiated disc, with wind mass loss taken into account. All other line codes as in Fig. 3.
The irradiation parameter $C$ estimated from scattering in the outflowing corona is within an order-of-magnitude of the constant $C$ we used, but shows important fluctuations around $l = 0.02$. These can significantly impact the lightcurves even though the wind mass loss rate is not important dynamically. Indeed, Fig. 4 shows the result of taking $C$ self-consistently from the scattered fraction. The outburst evolution is initially similar to the constant $C = 10^{-4}$ case and starts to differ around $t = 20 d$. The drop in $C$ to values $<10^{-3}$ strongly decreases the irradiation flux and this leads to reflares. Reflares occur when the surface density behind the cooling front becomes higher than the maximum $\Sigma_{\text{max}}$ allowed on the cold branch. Irradiation usually quenches reflares as it inhibits the propagation of the front and leads to smaller $\Sigma$ as more mass is accreted (Dubus et al. 2001). The reflares are clearly identified as a change in the propagation direction of the front as it switches from an inward-going cooling front to an outward-going heating front (dotted line, second panel from top). The four reflare episodes are also apparent as modulations of the lightcurves. This is typical of unirradiated discs. To illustrate this, the grey line in the top panel of Fig. 4 shows the lightcurve for an unirradiated disc (including mass loss from the wind). The lightcurve shows a similar sequence of reflares. This type of lightcurve is not observed so scattering in the wind, as modelled here, is insufficient to provide the required level of sustained irradiation heating during outburst in, for instance, XTE J1118+480.

The outbursts are longer than for the models in Fig. 3. This is not a numerical issue. The outburst cycles that we show are always relaxed, meaning they are independent of the initial conditions, and with 3600 grid points they are resolution independent. The recurrence timescale does change between models but remains around 4700 days. One reason for the longer outburst is that the amount of mass accreted during outburst is small compared to the disc mass (the disc mass varies by $\approx 20\%$ in all these models). Another reason is the presence of reflares. The back and forth movement of the front in a disc that remains massive certainly acts to lengthen the outburst.

4.2. A long orbital period system

We also consider an accretion disc around a $M = 9 M_\odot$ black hole with a mass transfer rate $\dot{M}_f \approx 6 \times 10^{-5} \text{ g s}^{-1}$. The disc has a size $\approx 10^{12}$ cm, corresponding to an orbital period $\approx 6 d$, viscosity parameters $\alpha_3 = 0.2$ and $\alpha_5 = 0.02$, and an irradiation parameter $C = 5 \times 10^{-5}$. The system parameters were chosen to be close to those of V404 Cyg. This is close to the largest disc that our code can handle with the vertical structures we have available at present. The values of $\alpha$ ensured the amplitude of the outburst reached $0.2 L_{\text{Edd}}$, large enough to have a strong wind without entering the optically thick regime. $C$ was chosen to be close to the time-averaged value of the wind $C$.

Figure 5 shows the outburst lightcurve with mass loss from the thermal wind taken into account. For comparison, the outburst lightcurve without the wind mass loss is shown as a grey line in the top panel of Fig. 3. The mass accreted by the black hole is $\approx 40\%$ of the mass lost to the wind when integrated over the outburst duration: most of the mass is ejected from the system. The wind ends the outburst sooner for lack of material to keep the disc in the hot state. It also decreases the peak luminosity since $M_{\text{ff}}$ is lowered by the mass lost in the outer disc (e.g. Fig. 2). Despite the shorter outburst more mass is accreted or ejected when the wind is turned on, so the recurrence time between outbursts accordingly increases from 75 (no wind) to 85 years (wind).

Unlike the short orbital case described above, a bona fide Compton wind develops here because of the large disc. The Compton radius $0.2 R_0$ is always within the accretion disc during the outburst (second panel of Fig. 3) and the luminosity is higher than $L_{\text{Edd}}$, for at least part of the outburst (third panel). Thus, the nature of the outflow evolves during outburst between a “steadily-heated free wind” (region B in Fig. 5 of Woods et al. 1996) and the Compton “isothermal wind” (region A) first described by Begelman et al. (1983). The switch between the hard and soft state is smoother than with the smaller accretion disc described in Sect. 4.1: the wind outflow rate is nearly proportional to $M_{\text{in}}$ throughout the outburst. The decay is close to exponential, even though the front does not reach $R_{\text{out}}$, with a decay timescale decreased by about 30\% compared to the case without wind.

The bottom panel of Fig. 5 shows the estimated $C$ from scattering. Its amplitude reaches $10^{-2}$, a factor 2 higher than the constant value assumed for Fig. 5. The two peaks in $C$ at beginning and end of the outburst are associated with the hard to soft transition at $l = 0.02$. The impact of the transition on $M_{\text{in}}$ is weaker than in Sect. 4.1, as noted above. Figure 6 shows how the outburst is modified by taking the self-consistent value of $C$. The higher value reached by $C$ lengthens slightly the outburst as irradiation maintains the disc in the hot state for a longer time. The evolution of $C$ during the outburst moves the lightcurve to a more flat-top shape than a fast-rise exponential decay, reminiscent for example of the 1996 outburst of GRO J1655–40 (Esin et al. 2000a). GRO J1655–40 has a $7 M_\odot$ black hole with an average accretion rate of $M_{\text{in}} \approx 5 \times 10^{16} \text{ g s}^{-1}$, and a disc size of $5 \times 10^{11}$ cm (Coriat et al. 2012), reasonably close to the parameters of the model shown here.

5. Discussion

5.1. The impact of thermal wind mass loss on lightcurves

The thermal wind shortens the outburst, as expected, but probably not enough to explain the rapid decay timescale of BHXB outbursts measured by Tetarenko et al. (2018a). In the most extreme case that we have explored, shown in Fig. 5, the outburst duration is shortened from 450 days to 300 days in our long orbital period system. The decay timescale that would be inferred from the lightcurve would lead to an effective $\alpha$ about 1.5 times greater than the value deduced from the lightcurve without a thermal wind. Achieving shorter outburst duration would require much more extreme mass loss rates much greater than we have in our model outburst. We show in Fig. 7 the wind efficiency $\eta_w$ as a function of the irradiation luminosity $L$ for our thermal wind model. The wind efficiency is defined as the ratio $\eta_w = M_{\text{w}}/M_{\text{in}}$ with $L = 0.08 M_{\text{in}} c^2$. The different curves correspond to different disc sizes. Figure 7 shows that $\eta_w$ is unlikely to become much greater than $\approx 2$ to 5, except possibly close to the Eddington luminosity as we detail below. The model in Fig. 5 has $\eta_w \approx 3$. In most systems, the effect on the lightcurve is modest or negligible.

An extreme example of a rapid decay is V404 Cyg. The parameters of the long $P_{\text{orb}}$ system were chosen to be close to those of V404 Cyg, whose last outburst lasted only a couple of weeks and showed a pronounced disc outflow, conjectured to be a thermal wind (Muñoz-Darias et al. 2016). The mass in the disc at the onset of the outburst is $\sim 3 \times 10^{-7} M_\odot$ in our models1. Blowing away most of this mass would require a sustained outflow of $\approx 10^{-7} M_\odot$ (Eq. (54) of Lasota 2001) with $\alpha = 0.02$ because $\Sigma$ is much lower than $\Sigma_{\text{max}}$ in the outer disc, where most of the mass is stored. 

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1 This is much less than the maximum allowed mass $\sim 10^{-5} M_\odot$ (Eq. (54) of Lasota 2001) with $\alpha = 0.02$ because $\Sigma$ is much lower than $\Sigma_{\text{max}}$ in the outer disc, where most of the mass is stored.
rate of $\approx 10^{-5} \, M_\odot \, \text{yr}^{-1} \approx 30 \, M_{\text{Edd}}$ over 15 days for a $9 \, M_\odot$ black hole. Such very high mass outflow rates may be reached close to the Eddington luminosity as electron scattering contributes to the driving force of the wind. Figure 7 shows the mass outflow rate in the wind diverges near $L \approx 0.7 \, L_{\text{Edd}}$ due to the estimated radiation driving correction (Eq. (4)). In principle, it might thus be possible to shorten the outburst of V404 Cyg to a couple of weeks by fine-tuning the model parameters to sample this high luminosity region. In support, observations of V404 Cyg do indicate the source likely reached $L_{\text{Edd}}$ (Kimura et al. 2016) and was enshrouded by rapidly varying Compton-thick outflowing material (Sánchez-Fernández et al. 2017) with an estimated $M_w \approx 4 \times 10^{-6} \, M_\odot$ lost to the wind (Casares et al. 2019). The lower effective gravity due to the high radiation should enhance the wind (Proga & Kallman 2002) but the mass loss must saturate at some level as the outflow becomes optically thick. Higginbottom et al. (2019) do not find a significantly enhanced $\dot{M}_w$ near $L_{\text{Edd}}$ in their radiation-hydrodynamic simulations of thermal winds, but these neglect radiative driving by electron scattering. If winds are boosted near Eddington, a puzzle is why GRS 1915+105 has not been affected as much as V404 Cyg despite its luminosity also being close to Eddington and its disc size even greater. If the short duration of the V404 Cyg was due to a thermal wind, then this wind likely required very specific
conditions. Instead, we speculate that the angular momentum transport was instead dominated by the jet. The system likely stayed in the (very) bright hard state during the outburst, where it has a strong jet which is almost certainly coupled to the accretion flow via the magnetic fields and could be responsible for angular momentum transport through the hot flow in this state (e.g. Ferreira et al. 2006).

The parametrisation we used predicts a wind in the hard state. Figure 7 shows that the wind can be stronger in the brightest hard states than in the dimmest soft states due to the higher $T_{IC}$, decreasing $R_{IC}$. The effect on the wind efficiency is particularly pronounced for small discs. This is apparently in contradiction with observations since wind outflow signatures are mostly seen during the soft state (see Sect. 1). It is usually argued that the wind is highly ionised due to the high radiation temperature, erasing potential spectral line signatures. Another possibility is that the wind is quenched in the hard state. Irradiation does not produce a smooth heated atmosphere as it becomes optically thick along the disc, self-shielding the outer radii from irradiation (Dubus et al. 1999). A wind, or a corona, such as one that can be provided by irradiation heating, can help scatter X-ray irradiation from the inner regions back to the outer disc. The launching of a thermal wind and the geometry of X-ray irradiation are thus directly connected. This scattered fraction can in principle be calculated self-consistently from simulations and may lead to interesting interplay, such as the suppression of the hard state thermal wind discussed above. It may supplement or dominate over direct irradiation of the flaring disc.

5.2. The X-rays scattered in the wind

The most important effect of thermal winds on the lightcurves is rather that they might change the fraction of X-rays scattered onto the disc. Compton winds are driven by X-ray heating of the upper layers of the outer disc, which must see the X-rays from the inner disc. The energy deposited by irradiation in the outer disc is also necessary to explain the optical luminosity of BHXB, their stability properties, and their outburst lightcurves (Sect. 1). It has now long been known that disc flaring is insufficient to geometrically capture a sufficient amount of the (point-like) inner X-ray luminosity. In an unstable disc undergoing outbursts, the cold outer disc necessarily has a smaller scale height than the hot inner disc, which self-shields the outer disc from the X-ray irradiation (Dubus et al. 1999). A wind, or a corona, such as one that can be provided by irradiation heating, can help scatter X-ray irradiation from the inner regions back to the outer disc. The launching of a thermal wind and the geometry of X-ray irradiation are thus directly connected. This scattered fraction can in principle be calculated self-consistently from simulations and may lead to interesting interplay, such as the suppression of the hard state thermal wind discussed above. It may supplement or dominate over direct irradiation of the flaring disc.

Following Kimura & Done (2019), we find that a very simple order-of-magnitude estimate of the scattered fraction $C$ leads to values that can be dynamically significant, more so than the wind mass loss. Our stationary model (Sect. 3.1) shows strong outflows are required to change the disc temperature. This can be easily compensated by a relatively small change in $C$ due to a slight change in wind density or geometry. Our short $P_{orb}$ model demonstrates that our rough self-consistent evolution of $C$ impacts the lightcurve much more than the wind outflow (Sect. 3.2). The outburst is very different than what is predicted when $C$ is assumed to be constant. Although the scatter $C$ can reach high values, the wind is not strong enough to maintain these high values and the lightcurve is essentially that of an unirradiated disc (Fig. 4). In the long $P_{orb}$ system, the estimated $C$ becomes somewhat higher than the typical values usually assumed and changes the lightcurve to a plateau-like state (Fig. 6). The order-of-magnitude estimate clearly breaks down for higher $L$ since the wind becomes opaque.

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Fig7.png}
\caption{Compton wind efficiency $\eta_w = M_w/M$. The mass accretion rate is related to luminosity by $L = 0.08 M_c^2$. The compact object is a 9 $M_\odot$ black hole. The outer disc radius goes as (from top to bottom) 32, 16, 8, 4, 2, $1 \times 10^3$ cm, representative of the variations in X-ray binary disc sizes from short to long $P_{orb}$.}
\end{figure}

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{Fig8.png}
\caption{Same as Fig. 7 with $T_{IC}$ multiplied by a factor 10.}
\end{figure}

2 Figure 8 also shows the drop in wind efficiency at the state transition is much smaller when a higher $T_{IC}$ is assumed. This would lead to a smaller jump in the stability line (see Sect. 3.2).
Changes in C are directly related to variations in $M_{\text{in}} R_{\text{in}}^{-1/2}$ if the wind speed is roughly proportional to the escape velocity at the inner edge of the thermal wind launching region (Eq. (10), see also Figs. 4 and 6). Other mechanisms may also lead to changes in C, such as warps (Esin et al. 2000a,b). Tracking the time series evolution of C throughout an outburst using a combination of X-ray and optical data might thus identify times of important changes in wind properties, possibly relating them to changes in the spectrum, luminosity, column density, ionisation etc (Tetarenko et al., in prep.).

6. Conclusion

Compton winds are a natural outcome of X-ray irradiation of large accretion discs in BHXBs. The mass outflow rate in the wind is typically several times the accretion rate, which does shorten somewhat the outburst in long $P_{\text{orb}}$ binaries. We do not find substantially new behaviour in the lightcurves due to the thermal wind mass loss, such as glitches or re-brightenings, at least under the assumptions used here to parametrise the wind. However, we do find that the lightcurves and stability properties are significantly affected when X-ray irradiation heating is derived from the scattered lighted light in the thermal wind. Scattering in the thermal wind couples the irradiation constant C to the disc size and the mass accretion rate. Stability can be achieved at lower mass accretion rates because C is then very high (Fig. 2). There are no remaining free parameters once $T_{\text{K}}$ is specified. The resulting stability curves separate persistent and transient systems very well in the $(P_{\text{orb}}, M_{\text{in}})$ plane, arguably better than so irradiated discs with C fixed at some identical value for all systems.

We find that Compton wind mass loss is unlikely to be high enough to explain the rapid decay of a variety of BHXB outbursts in different spectral states (Tetarenko et al. 2018a), though we cannot yet simulate the brightest outbursts. Instead, an alternative explanation of those fast decays is angular momentum losses from a magnetic wind threading the disc and/or hot flow. This is a very effective way to change the outburst dynamics as shown for dwarf novae by Scepi et al. (2019), even when a negligible amount of matter is lost to the magnetic wind. Whereas thermal winds extract matter but no angular momentum, magnetic winds do exactly the opposite. Waters & Proga (2018) find strong magnetic fields tend to inhibit thermal winds since the outflowing material, channelled by the field, is not able to be accelerated. One or the other may dominate at different times depending on where magnetic fields originate and diffuse through the disc in outburst. Understanding the latter is a difficult but an increasingly pressing issue.

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