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Variations in the initial mass function in early-type galaxies: a critical comparison between dynamical and spectroscopic results

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ABSTRACT

I present a comparison between published dynamical (ATLAS3D) and spectroscopic (Conroy & van Dokkum) constraints on the stellar initial mass function (IMF) in early-type galaxies, using the 34 galaxies in common between the two works. Both studies infer an average IMF mass factor α (the stellar mass relative to a Kroupa-IMF population of similar age and metallicity) greater than unity, i.e. both methods favour an IMF which is heavier than that of the Milky Way, *on average* over the sample. However, on a galaxy-by-galaxy basis, there is no correlation between α inferred from the two approaches. I investigate how the two estimates of α are correlated systematically with the galaxy velocity dispersion, σ , and with the Mg/Fe abundance ratio. The spectroscopic method, based on the strengths of metal absorption lines, yields a correlation only with metal abundance ratios: at fixed Mg/Fe, there is no residual correlation with σ . The dynamical method, applied to exactly the same galaxy sample, yields the *opposite* result: the IMF variation correlates only with dynamics, with no residual correlation with Mg/Fe after controlling for σ . Hence, although both methods indicate a heavy IMF on average in ellipticals, they lead to incompatible results for the systematic trends, when applied to the same set of galaxies. The sense of the disagreement could suggest that one (or both) of the methods has not accounted fully for the main confounding factors, i.e. element abundance ratios or dark matter contributions. Alternatively, the poor agreement might indicate additional variation in the detailed shape of the IMF, beyond what can currently be inferred from the spectroscopic features.

Key words: galaxies: elliptical and lenticular, cD – galaxies: stellar content.

1 INTRODUCTION

The stellar initial mass function (IMF) is a key quantity in astrophysics, both intrinsically, as a constraint on the physics of star formation, and also for its importance in converting observed galaxy luminosities into physically meaningful stellar masses, star formation rates, etc. In recent years, several largely independent methods have found evidence for a different IMF in early-type galaxies, compared to the Milky Way (MW), and for systematic variation among elliptical galaxies as a function of their mass (Auger et al. 2010; Treu et al. 2010; van Dokkum & Conroy 2010; Conroy & van Dokkum 2012b; Smith, Lucey & Carter 2012; Spiniello et al. 2012; Cappellari et al. 2013; La Barbera et al. 2013).

One method to constrain the IMF uses measurements of spectral features that are sensitive to surface gravity at fixed stellar temperature, and hence reveal the presence of low-mass stars in integrated light spectra (Conroy & van Dokkum 2012a). Dwarf-star-sensitive features are found to increase in strength in higher mass galaxies, beyond what is expected from element abundance trends, accord-

ing to spectral synthesis models. This behaviour is interpreted as due to an increasingly bottom-heavy IMF in higher mass galaxies. As noted by Conroy & van Dokkum (2012b), the signature of bottom-heavy IMFs appears more strongly correlated with Mg/Fe abundance ratios than with velocity dispersion, suggesting that IMF could be linked to star formation intensity, with more low-mass stars being produced in rapid bursts.

Another technique is to infer the total mass in galaxies from gravitational tracers, such as stellar dynamics (e.g. Cappellari et al. 2013) or strong lensing (e.g. Treu et al. 2010). After accounting for the dark matter halo contribution, this leads to an estimate of stellar mass-to-light ratio Υ . Comparing this to the ‘reference’ mass-to-light ratio (Υ_{ref}) expected from the spectrum of the galaxy assuming a MW-like IMF, this yields a mismatch factor $\alpha = \Upsilon/\Upsilon_{\text{ref}}$. Lensing and dynamical studies both find a trend of increasing α with galaxy mass, which can be attributed to an increasing contribution of low-mass stars, i.e. a more bottom-heavy IMF.

It should be stressed that these two approaches to constraining the IMF measure fundamentally different quantities: gravitational tracers strictly measure mass (which could be dominated by very low mass dwarfs, or by remnants from massive stars), while the spectroscopic method is sensitive only to low-mass stars.

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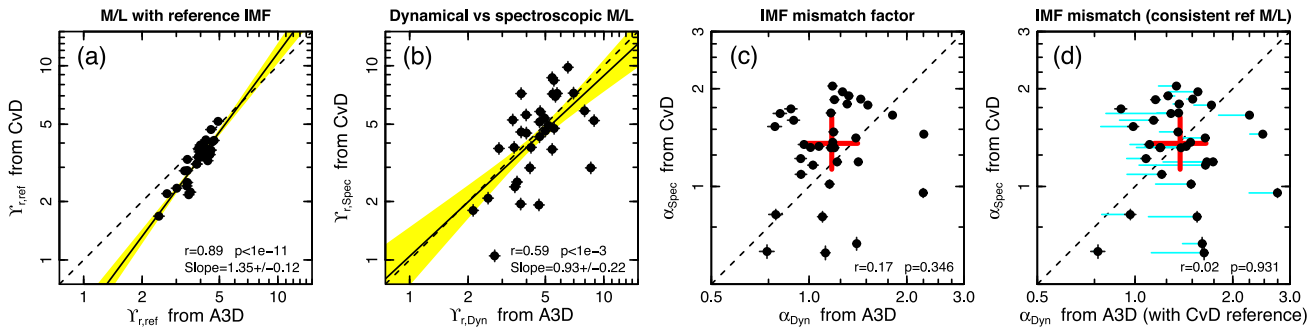


Figure 1. Comparison of the mass-to-light ratios, Υ , used by CvD and A3D, and the derived mismatch parameters, α . Panel ‘a’ compares the reference mass-to-light ratios, i.e. those derived from stellar population fitting assuming a standard (Kroupa 2001) IMF. Panel ‘b’ compares the derived spectroscopic and dynamical mass-to-light ratios. Panel ‘c’ compares the ratios $\alpha = \Upsilon/\Upsilon_{\text{ref}}$, which indicate the inferred deviations from the standard IMF. In panel ‘d’, the A3D value of α is modified by using the same Υ_{ref} as used by CvD, for greater consistency (cyan lines show the effect of this change). The red cross in panels ‘c’ and ‘d’ shows the median value for the two data sets. The quoted slopes and correlation coefficients r are for comparisons in $\log \Upsilon$ or $\log \alpha$; p is the probability of a larger r under the null hypothesis of no correlation. In panels ‘a’ and ‘b’, the solid line and yellow shading show a linear fit with errors. While the mass-to-light ratios are well correlated between the studies, the ratio α shows essentially no correlation on a galaxy-by-galaxy basis.

When mass-to-light ratios are quoted from spectroscopy, as by CvD, the values depend on a model assumed for the shape of the IMF. Since spectroscopy and dynamics/lensing each measures a differently weighted integral over the IMF, comparing the two methods yields a test for the correctness and universality of the assumed IMF model, as well as a test for the systematic errors inherent to each method. For example, La Barbera et al. (2013) emphasize that although single- and broken-power-law IMFs can fit their spectroscopic data equally well, the best-fitting single-power-law model can be excluded, since it would imply an excessively high Υ for the most massive galaxies.

At face value, the recent spectroscopic and dynamical/lensing results do appear to agree, at least at a qualitative level: massive early-type galaxies have IMFs which, on average, are more bottom heavy than that of the MW, and there is a trend of increasing deviation from the MW IMF at larger mass. This apparent consensus between largely independent methods has understandably led to increased confidence in these results.¹ In this Letter, I present a critical evaluation of results obtained by Conroy & van Dokkum (2012b) and by Cappellari et al. (2013) (hereafter CvD and A3D), where comparisons can be made for exactly the same set of galaxies. I start by directly comparing the spectroscopic and dynamical mass-to-light ratios, the reference mass-to-light ratios, and the IMF mismatch factors, on a galaxy-by-galaxy basis (Section 2). Section 3 investigates the systematic correlations of mismatch factor with velocity dispersion and Mg/Fe ratios. In Section 4, I highlight the very different systematic trends obtained from CvD and A3D for this common sample of galaxies and discuss possible resolutions. Brief conclusions are drawn in Section 5.

2 MASS-TO-LIGHT RATIOS AND IMF FACTORS

The data employed in this Letter are all taken from the published sources (table 2 of CvD and table 1 of A3D). The key parameters are the stellar mass-to-light ratios Υ derived from spectral fitting by CvD and those inferred by A3D from dynamical modelling, and the

‘reference’ mass-to-light ratios, Υ_{ref} , derived by fitting the spectra with models of fixed IMF. For clarity, the Υ_{ref} from A3D is converted to a Kroupa (2001) reference IMF (rather than Salpeter 1955), to match the convention used by CvD, multiplying by 1.55. The A3D Υ and Υ_{ref} values refer to an aperture of $\sim 1R_{\text{eff}}$ (the effective radius), while the CvD quantities are for an aperture of $R_{\text{eff}}/8$. (The typical metallicity gradient implies an ~ 0.2 dex difference in Z/H between these apertures, causing only ~ 10 per cent difference in mass-to-light ratio.) Additionally, I use the velocity dispersion and Mg/Fe ratios from CvD to test how the IMF correlates with other key galaxy parameters. These quantities are as measured within the central aperture of $R_{\text{eff}}/8$. From the tabulated parameters, the IMF mismatch factor α is derived by dividing the spectroscopic and dynamical mass-to-light ratios by the corresponding reference values, i.e. $\alpha_{\text{Spec}} = \Upsilon_{K,\text{Spec}}^{\text{CvD}}/\Upsilon_{K,\text{ref}}^{\text{CvD}}$ and $\alpha_{\text{Dyn}} = \Upsilon_{r,\text{Dyn}}^{\text{A3D}}/\Upsilon_{r,\text{ref}}^{\text{A3D}}$. The difference in passband (r and K subscripts) in these definitions does not significantly affect the α factor because the additional mass implied by a bottom-heavy IMF (which does not depend on bandpass) greatly exceeds the additional light (which does).

I begin by comparing the reference mass-to-light values used in the two studies, in Fig. 1a. A version of this comparison was presented by Cappellari et al. (their fig. 10), but they compared the K -band mass-to-light ratio from CvD with the r -band ratio from A3D, applying a constant offset (value unstated) to account for the difference in bandpass and reference IMF adopted. Here, I use the r -band Υ_{ref} from CvD, which can be derived from parameters in their table 2, since α is independent of bandpass: $\Upsilon_{r,\text{ref}} = \Upsilon_{r,\text{Spec}}(\Upsilon_{K,\text{ref}}/\Upsilon_{K,\text{Spec}})$. Whereas A3D found a slope consistent with unity, Fig. 1(a), using the r -band quantities consistently, shows a significant tilt, with CvD finding progressively smaller Υ_{ref} for lower Υ_{ref} (younger or more metal-poor) galaxies. The comparison also indicates a zero-point shift: the reference mass-to-light ratios used by CvD are on average 20 per cent smaller than those from A3D (the ~ 10 per cent offset due to metallicity gradients would act in the opposite direction). The scatter around a linear trend line is only 12 per cent in Υ_{ref} . The formal errors are quoted as 7 and 2 per cent in A3D and CvD, respectively;

Fig. 1(b) shows the equivalent comparison for the best derived stellar mass-to-light ratios from the two works, i.e. $\Upsilon_{r,\text{Dyn}}^{\text{A3D}}$ versus $\Upsilon_{r,\text{Spec}}^{\text{CvD}}$. A similar figure was shown in CvD (their fig. 11), but using the *total* dynamical mass-to-light ratio from Scott et al. (2009), i.e. including dark matter. By contrast, Fig. 1(b) employs the more recently published mass-to-light ratios from Cappellari et al. (2013),

¹ But note that some other works have favoured MW-like IMFs even in very massive ellipticals, using lensing (Smith & Lucey 2013) and dynamics (Thomas et al. in preparation, see http://www.mpa-garching.mpg.de/halo2013/pdfs/day5/11_thomas.pdf).

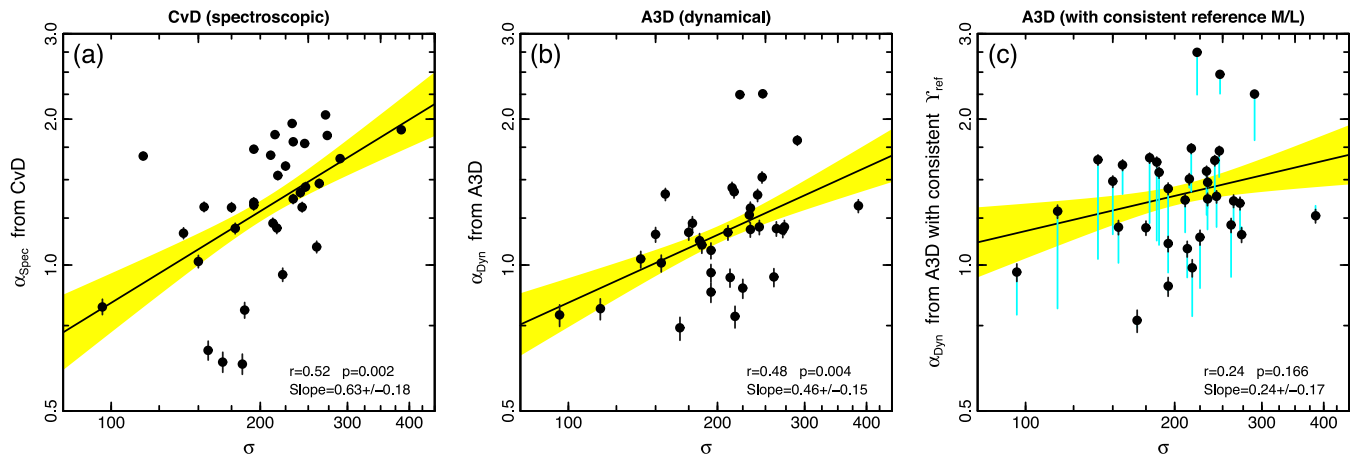


Figure 2. The relationship between IMF mismatch factor α and velocity dispersion σ , as derived from spectroscopy by CvD and from dynamics by A3D, for the same sample of galaxies. Panel ‘c’ shows A3D adjusted to use the CvD-derived reference mass-to-light ratio, for consistency. Slopes and correlation coefficients are for $\log \alpha$ versus $\log \sigma$. The solid line and yellow shading show the linear fit with errors to the data in each panel.

which refer to the *stellar* component alone, and hence are directly comparable with CvD. The clear correlation seen in Fig. 1(b) is an impressive achievement, since there are essentially no common ingredients between the A3D dynamical masses and the CvD spectroscopic estimates. The scatter in this comparison is ~ 50 per cent, greatly in excess of the formal statistical errors of ~ 7 per cent reported by each study, but supporting the statement by CvD that systematic errors in Υ_{Spec} are no more than 50 per cent.

Of course, the measured mass-to-light ratios reflect not only the IMF but also depend on the metallicity and star formation history. To isolate the IMF effects, Fig. 1(c) shows the comparison between the mismatch factors α_{Dyn} and α_{Spec} . This test does not support any correlation between the IMF constraints obtained from the two methods, at a galaxy-by-galaxy level (correlation coefficient $r = 0.17$, exceeded with probability 0.34 under the null hypothesis of no correlation). Since the two studies used reference mass-to-light ratios Υ_{ref} which differ systematically, it is also helpful to construct a ‘hybrid’ quantity $\alpha_{\text{Dyn,hyb}}$ by dividing the dynamical mass-to-light ratio from A3D by the reference value obtained by CvD, i.e. $\alpha_{\text{Dyn,hyb}} = \Upsilon_{r,\text{Dyn}}^{\text{A3D}} / \Upsilon_{r,\text{ref}}^{\text{CvD}}$. This parameter isolates the differences between dynamical and spectroscopic mass-to-light ratios, keeping a consistent treatment of the reference mass-to-light. Fig. 1(d) repeats the α comparison using $\alpha_{\text{Dyn,hyb}}$ in place of α_{Dyn} . This shifts A3D to larger α on average, because the average CvD Υ_{ref} is smaller, but again there is no significant correlation between the IMF parameters derived from the two studies ($r = 0.02$).

3 SYSTEMATIC IMF TRENDS

Although the galaxy-by-galaxy comparison in the previous section found no correlation between dynamical and spectroscopic α , some statistical similarity may still appear when analysing the sample as a whole. For example, it is clear that the average mass-to-light ratios in both cases are generally larger than the average reference values, i.e. both methods indicate a heavier-than-MW IMF, on average. This section compares the data at an intermediate level of detail, through the correlations of α with velocity dispersion and $[\text{Mg}/\text{Fe}]$, i.e. do the two methods yield similar systematic *trends*, when pooling information over the whole sample?

Fig. 2 shows the α versus σ relation derived from the spectroscopic and dynamical methods. The results from both methods, indicate a significant increase in α with increasing velocity dispersion, at the $\sim 3\sigma$ level. The A3D relation is marginally shallower

($\Delta \log \alpha / \Delta \log \sigma = 0.4 \pm 0.15$, compared to 0.63 ± 0.18 for CvD) and is offset to slightly lower α . Using $\alpha_{\text{Dyn,hyb}}$ (i.e. forcing the same reference mass-to-light ratio in both studies) shifts A3D to higher normalization and reduces the derived slope further to 0.24 ± 0.17 : consistent with zero, and marginally inconsistent with the CvD slope. (The slope determined by Cappellari et al. for the *full* A3D sample of 260 galaxies is 0.26 ± 0.05 .)

Fig. 3 shows the equivalent comparison for the α versus $[\text{Mg}/\text{Fe}]$ relation. As noted by CvD this is a much stronger correlation for their data set than the α – σ relation; the trend is significant at $>7\sigma$. Notably, however, the same is *not* true for the A3D measurements in the same sample: the trend of α_{Dyn} with Mg/Fe is consistent with zero ($\Delta \log \alpha / \Delta [\text{Mg}/\text{Fe}] = 0.34 \pm 0.34$, which can be compared to 1.95 ± 0.25 for CvD). Using $\alpha_{\text{Dyn,hyb}}$ flattens the A3D slope further (to -0.00 ± 0.35).

Since Mg/Fe and σ are mutually correlated in early-type galaxies, it is helpful to separate the effects of the two parameters using a simultaneous regression. Fitting a model of the form $\alpha = c_0 + c_1 \log(\sigma/200 \text{ km s}^{-1}) + c_2([\text{Mg}/\text{Fe}] - 0.2)$, I obtain the coefficients and error ellipses which are displayed in Fig. 4. Because Mg/Fe and σ are positively correlated, the errors on their coefficients are anti-correlated; none the less, there is sufficient scatter around the Mg/Fe – σ relation to identify the dominant statistical (though not necessarily causal) ‘driver’ of the correlations. For CvD, the bivariate fit confirms that Mg/Fe is the *only* informative predictor of α : at fixed Mg/Fe , there is *no* residual correlation with velocity dispersion. By contrast, the A3D measurements show a marginally *negative* correlation with Mg/Fe after controlling for the trend with σ . Despite being based on the same sample of galaxies, the trends derived from A3D and CvD are different at the $>4\sigma$ level, based on the error ellipses in Fig. 4. Using $\alpha_{\text{Dyn,hyb}}$ makes little difference to the slopes obtained from the bivariate fit.

4 DISCUSSION

Comparing the A3D and CvD determinations of the IMF mismatch factor α , for an identical sample of 34 galaxies, I have shown that there is no correlation between dynamical and spectroscopic α , at a galaxy-by-galaxy level, and that the systematic trends with ‘mass’ are quite different for the two studies. Specifically, although both studies superficially find a correlation of α with velocity dispersion, this trend in CvD merely reflects an underlying correlation with Mg/Fe , while for A3D the correlation is only with σ .

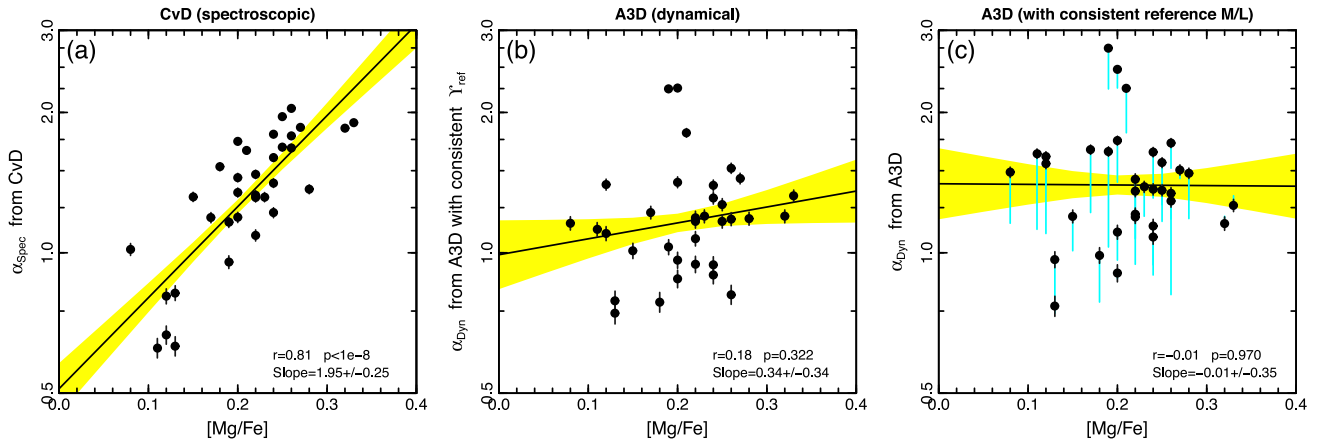


Figure 3. Equivalent to Fig. 2 but now for correlations of IMF mismatch factor α with abundance ratio $[\text{Mg}/\text{Fe}]$. Slopes and correlation coefficients are for $\log \alpha$ versus $[\text{Mg}/\text{Fe}]$. Note how, compared to the previous figure, the correlation is strengthened for CvD but weakened for A3D.

A sceptical interpretation of these results would be to conclude that possible confounding factors have not been completely accounted for in one or both of the two methods. When the IMF is constrained using the strengths of metal lines, it is found to be correlated only with metal abundances. When dynamical models are used, the IMF is found to correlate only with a dynamical quantity. Of course, the IMF *could* be intrinsically related either to the velocity dispersion or to the abundance ratios; the problem is that the two methods, applied to an identical sample, yield incompatible conclusions. Both CvD and A3D take great care to account for the degeneracies in their methods: For the dynamical estimates, Cappellari et al. (2012) explored a wide range of plausible dark matter halo models, with and without baryonic ‘contraction’, and found that the requirement for a heavy IMF at high σ was robust with respect to the halo prescription. For spectroscopy, CvD used detailed stellar atmosphere calculations (Conroy & van Dokkum 2012a) to disentangle the IMF from effects of different abundance mixtures on the integrated spectra, and fit the abundance pattern (and other nuisance parameters) simultaneously with the IMF model. Hence, if the discrepancies highlighted in this Letter do arise from incomplete resolution of either IMF/dark matter or IMF/abundance degeneracies, the mechanism must be rather subtle.

Alternatively, it is possible that both methods correctly measure different aspects of the IMF. Recall that α refers to a ratio of mass-to-light ratios, but only the dynamical method strictly measures mass. CvD instead measure the contribution of cool dwarf stars to the integrated luminosity. The mass-to-light ratio Υ_{Spec} is obtained by fitting a three-part power-law IMF model, and computing the mass and luminosity from this model, integrating from 0.1 to 100 M_{\odot} . The result can depend quite sensitively on the form of the shape of the adopted model, as shown in Fig. 5. Since the features used by CvD do not constrain the IMF shape in detail, their Υ_{Spec} are inevitably dependent, to some extent, on the form of the model imposed. This point has also been emphasized by La Barbera et al. (2013), who note that different prescriptions for IMF models (single-slope versus two-part power laws), which fit galaxy spectra similarly well, can have very different mass-to-light ratios. Potentially, then, the dynamical measurements of α , probing the total stellar mass, are measuring variation in the very low mass end of the IMF (or even perhaps the contributions of stellar remnants) while spectroscopic α are measuring a different ‘moment’ of the IMF. Barnabè et al. (2013) have used this argument to constrain jointly the slope and cut-off mass for a power-law IMF in lensing ellipticals. In this scenario, the large scatter observed

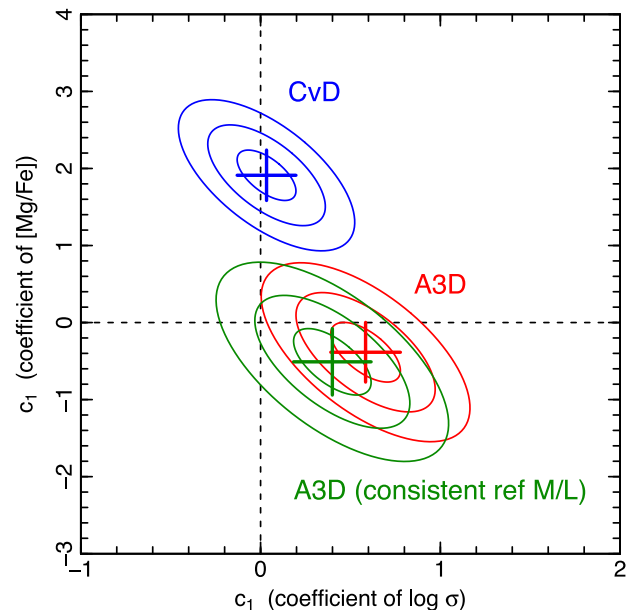


Figure 4. Coefficients of bivariate fits to the IMF mismatch factor α , as derived for an identical sample of galaxies by CvD (spectroscopic method) and ATLAS3D (dynamical). The contours show the $1-3\sigma$ confidence regions for the coefficients of velocity dispersion and $[\text{Mg}/\text{Fe}]$, i.e. c_1 and c_2 in a model of the form $\alpha = c_0 + c_1 \log(\sigma/200 \text{ km s}^{-1}) + c_2([\text{Mg}/\text{Fe}] - 0.2)$. The dynamical method finds α correlated only with σ , while the spectroscopic method has α correlated only with abundance ratios.

between spectroscopic and dynamical α would imply a galaxy-to-galaxy variation in the IMF *in excess* of what can be constrained by spectral features, ruling out one-parameter forms for the IMF. Moreover, the separate parameter dependences for α_{Spec} and α_{Dyn} could then indicate that different aspects of the IMF correlate with different properties, e.g. slope varying with Mg/Fe but low-mass cut-off dependent on σ .

A further possibility is that the IMF varies substantially *within* galaxies, so that the $R_{\text{eff}}/8$ spectroscopic aperture probes populations with a significantly different degree of dwarf enrichment compared to the $\sim R_{\text{eff}}$ scale probed by the dynamics. Spatially resolved spectroscopic IMF constraints (e.g. Martín-Navarro et al. 2014; Pastorello et al. 2014) should soon be able to test whether this explanation is viable.

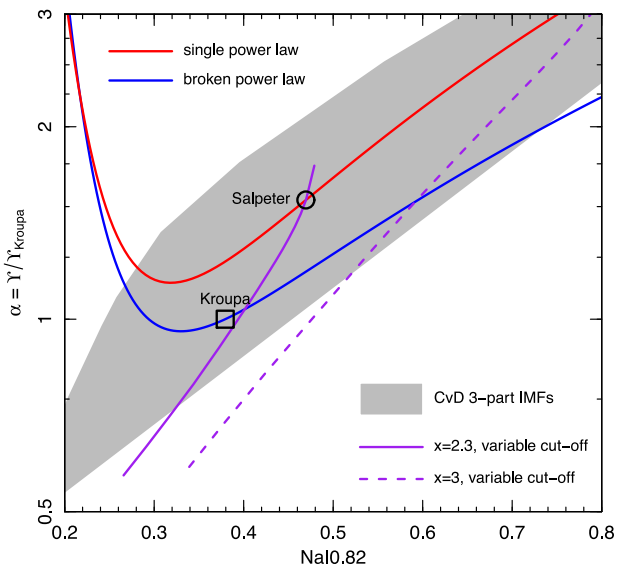


Figure 5. Effect of different assumed IMF models in the conversion from spectroscopic constraints (here represented by the NaI0.82 index defined by Conroy & van Dokkum 2012a), to mass-to-light factor $\alpha = \Upsilon/\Upsilon_{\text{ref}}$. One-parameter models (e.g. in which a single slope, or a single cut-off mass, is varied) imply a one-to-one mapping from spectroscopic information to α . The blue line shows calculations for a broken power law IMF as used by Barbera et al. (2013), with a varying slope above $0.4 M_{\odot}$, but a fixed slope of $x = 1$ at low mass. Models in which the high-mass slope is varied can become dominated by remnant mass (upper left). The three-part IMFs used by CvD have fixed high-mass slope (so are never remnant dominated), but two free parameters for the low-mass slopes, hence a broader range in α for given spectroscopy. The purple lines show power-law IMFs with fixed slope but varying low-mass cut-off ($M_{\text{low}} = 0.08\text{--}0.5 M_{\odot}$). All other models are integrated over a mass range $0.1\text{--}100 M_{\odot}$. The quantities shown here were computed using a 13.5 Gyr solar-composition isochrone from the BaSTI data base (Pietrinferni et al. 2004), including low-mass tracks from Cassisi et al. (2000), and an approximate fitting function for NaI0.82 derived from fig. 7 of Conroy & van Dokkum (2012a).

Finally, I note that the strong dependence of α on Mg/Fe found by CvD (and supported by Smith et al. 2012) is apparently *not* seen in the study of stacked spectra from the Sloan Digital Sky Survey (SDSS) by La Barbera et al. (2013). They found little correlation of IMF-dependent features against Mg/Fe at fixed σ after correcting for age and metallicity effects (their fig. 8). Fitting a broken power-law IMF to composite spectra binned as a function of both σ and Mg/Fe, they obtain a very strong dependence on σ and only a weak correlation with Mg/Fe, the latter simply reflecting the Mg/Fe versus σ relation (La Barbera, private communication).

5 CONCLUSIONS

I have presented a comparison between spectroscopic (CvD) and dynamical (A3D) results on the IMF in elliptical galaxies, using a common sample of 34 galaxies with measurements in both studies.

The analysis shows that ‘consensus’ between dynamical and spectroscopic measurements is present only at the most rudimentary level: both approaches find that a heavier-than-MW IMF is required, on average, for the common sample, but there is no correlation between the mass-excess factors derived from the two methods, on a galaxy-by-galaxy level. The two studies apparently find a correlation of α with some quantity related to galaxy mass. When plotted only against σ , there is reasonable agreement in slope, but this treatment obscures a clear discrepancy between the results:

the correlation found by CvD is not a trend with σ , but entirely with the Mg/Fe abundance ratio. By contrast, A3D finds no correlation of α with Mg/Fe and is hence in significant conflict with the spectroscopic method.

The sense of this disagreement could indicate that confounding factors such as dark matter contributions (A3D) or unusual abundance patterns (CvD) have not been correctly separated from the IMF effects in one or other of the methods. Alternatively, since the two methods are sensitive to different aspects of the IMF, further comparison between dynamical and spectroscopic estimates of α might lead to a more detailed understanding of the *shape* of the IMF and its possible variation in elliptical galaxies.

Work is ongoing to derive spectroscopic IMF constraints for more galaxies in the A3D sample, and to improve the treatment of element abundance treatment in the CvD models (Conroy, private communication). Hence, an enlarged and updated comparison between the two methods should be possible in the near future.

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NOTE ADDED IN PROOF

In Fig. 5 the blue line shows calculations for a broken power law IMF as used by La Barbera et al. (2013), with a varying slope above $0.4 M_{\odot}$, but a fixed slope of $x = 1$ at low mass.

REFERENCES

- Auger M. W., Treu T., Bolton A. S., Gavazzi R., Koopmans L. V. E., Marshall P. J., Moustakas L. A., Burles S., 2010, *ApJ*, 724, 511
 Barnabè M., Spiniello C., Koopmans L. V. E., Trager S. C., Czoske O., Treu T., 2013, *MNRAS*, 436, 253
 Cappellari M. et al., 2012, *Nature*, 484, 485
 Cappellari M. et al., 2013, *MNRAS*, 432, 1862
 Cassisi S., Castellani V., Ciarcelluti P., Piotto G., Zoccali M., 2000, *MNRAS*, 315, 679
 Conroy C., van Dokkum P., 2012a, *ApJ*, 747, 69
 Conroy C., van Dokkum P., 2012b, *ApJ*, 760, 71 (CvD)
 Kroupa P., 2001, *MNRAS*, 322, 231
 La Barbera F., Ferreras I., Vazdekis A., de la Rosa I. G., de Carvalho R. R., Trevisan M., Falcón-Barroso J., Ricciardelli E., 2013, *MNRAS*, 433, 3017
 Martín-Navarro I., La Barbera F., Vazdekis A., Falcón-Barroso J., Ferreras I., 2014, preprint ([arXiv:1404.6533](https://arxiv.org/abs/1404.6533))
 Pastorello V., Forbes D. A., Foster C., Brodie J. P., Usher C., Romanowsky A. J., Strader J., Arnold J. A., 2014, *MNRAS*, in press ([arXiv:1405.2338](https://arxiv.org/abs/1405.2338))
 Pietrinferni A., Cassisi S., Salaris M., Castelli F., 2004, *ApJ*, 612, 168
 Salpeter E., 1955, *ApJ*, 121, 161
 Scott N. et al., 2009, *MNRAS*, 398, 1835
 Smith R. J., Lucey J. R., 2013, *MNRAS*, 434, 1964
 Smith R. J., Lucey J. R., Carter D., 2012, *MNRAS*, 426, 2994
 Spiniello C., Trager S. C., Koopmans L. V. E., Chen Y. P., 2012, *ApJ*, 753, L32
 Treu T., Auger M. W., Koopmans L. V. E., Gavazzi R., Marshall P. J., Bolton A. S., 2010, *ApJ*, 709, 1195
 van Dokkum P., Conroy C., 2010, *Nature*, 468, 940

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