Disordered Nanocrystalline Superconducting PbMo$_6$S$_8$ with a Very Large Upper Critical Field

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Large increases in the upper critical field $B_{c2}(0)$ are reported in bulk superconductors that demonstrate another novel property for nanocrystalline materials. Disordered nanocrystalline PbMo$_6$S$_8$ superconductors were fabricated by mechanical milling and hot isostatic pressing. Conventional PbMo$_6$S$_8$ has $B_{c2}(0) \sim 50$ T. The nanocrystalline materials have higher resistivity ($\rho_N$) and $B_{c2}(0) \sim 100$ T. The disorder produced in these nanocrystalline materials is significantly different from that produced by doping because it increases $\rho_N$ and, hence, $B_{c2}(0)$ without significantly reducing the electronic density of states or superconducting transition temperature ($T_c$). Furthermore, the disorder reduces the electron mean-free path to $\sim 1$ nm which is more than an order of magnitude smaller than the grain size and necessary to achieve the unprecedented increase in $B_{c2}(0)$.

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There is an enormous effort directed at increasing the upper critical field ($B_{c2}$) of the superconducting materials because $B_{c2}$ provides a fundamental limit to the maximum field a magnet system can produce. High-energy particle accelerators and medical resonance imaging body scanners are limited by the $B_{c2}$ for NbTi ( $\sim 10$ T). Gigahertz class nuclear-magnetic-resonance and high field laboratory magnets are limited by $B_{c2}$ for Nb$_3$Sn ( $\sim 23$ T) [1]. According to BCS theory, $B_{c2}(0)$ for a superconductor at zero temperature is given by [2,3]:

$$B_{c2}(0) = R(\infty)/R(\lambda_{Tc})[8.3 \times 10^{34}(\gamma T_c/S)^2 + 3.1 \times 10^3 \gamma T_c \rho_N]^{1/4},$$

(1)

where $R(\infty)/R(\lambda_{Tc})$ is a strong-coupling correction close to unity, $\gamma$ is the Sommerfeld constant, $T_c$ is the critical temperature, $S$ is the Fermi surface area, and $\rho_N$ is the normal state resistivity. Therefore, $B_{c2}(0)$ can be increased by increasing $\rho_N$ as long as any reduction in $T_c$ and $\gamma$ is minimized. Whether the mechanism causing the superconductivity is BCS-like or not, Ginzburg-Landau (GL) theory [4] shows that in the vicinity of a superconducting-insulating barrier, $B_{c2}$ is increased. Hence, there is strong evidence that increasing disorder, either by increasing $\rho_N$ or from reduced-size effects, increases $B_{c2}$ [5].

Chemical doping or alloying has been used as the main route for improving $B_{c2}$ of bulk superconductors by producing disorder from the lattice strain and change in the local electronic properties. Low-level doping increases $\rho_N$, but the enhancements of $B_{c2}$ (4.2 K) have been small, $\sim 0.3$ T in NbTi doped with Ta and Hf [6], $\sim 4$ T in Nb$_3$Sn doped with Ti, Ta, Zr, Mo, and V [7]. Further increases in $\rho_N$ by high-level doping depress $B_{c2}$ rapidly [7,8]. Nevertheless, there are precedents for large increases in $B_{c2}$ that are correlated with large increases in $\rho_N$. In thin films, increases in $B_{c2}(0)$ of $\sim 9$ T have been reported for Nb$_3$Sn [3] and $> 40$ T for MgB$_2$ [9]. These increases were attributed to alloying and strain. In a metal-insulator nanocomposite synthesized by injecting indium into 56 Å pore diameter YcO glass, an increase in $B_{c2}(0)$ by a factor of $\sim 100$ has been found [10]. GL theory implies that the small crystallite size increased $B_{c2}(0)$ by reducing the electron mean-free path and, hence, the Ginzburg-Landau coherence length ($\xi$).

High energy mechanical milling has been used as an effective way to synthesize large quantities of disordered, nanocrystalline and amorphous powders containing large amounts of vacancies, dislocations, and grain boundaries [11,12]. Nanocrystalline bulk materials can then be obtained with different levels of disorder by subsequently compacting and heat treating the milled powder [13,14]. Nanocrystalline materials exhibit unique properties, such as increased strength, improved ductility, enhanced thermal expansion coefficient, and superior soft magnetic properties compared to conventional polycrystalline materials [13].

In this Letter, we report resistive and magnetic data in high magnetic fields and x-ray diffraction (XRD) data on disordered nanocrystalline bulk PbMo$_6$S$_8$. The disorder reduces the electron mean-free path in these materials to only $\sim 1$ nm, which is about an order of magnitude smaller than the grain size and it also has significantly less effect on the bulk electronic density of states than doping. Hence, the superconducting coherence length in these materials is made sufficiently small to produce an unprecedented increase in $B_{c2}(0)$ for PbMo$_6$S$_8$ from 50 T in bulk materials up to $> 100$ T.

The superconducting PbMo$_6$S$_8$ powder used in the present study was mechanically milled for 200 h under an Ar gas atmosphere. The milled powder was consolidated using hot isostatic pressing (HIP) at different temperatures and a pressure of 2000 bars for 8 h and postannealed at 1000 °C for 40 h so as to achieve different levels of disorder and, hence, $\rho_N$. The details of the fabrication have been described previously [15].
The HIP samples were calculated from the XRD data from few nanometers [17]. The grain size and lattice strain of parameters are usually observed when the grain size is just a nanocrystalline sample and the conventional sample, 800 HIP at \(0^\circ\text{C}\) with grain sizes between 20 and 90 nm were obtained, as shown in Table I.

In Fig. 1, the very broad XRD peaks for the powder milled for 200 h are due to the formation of nanocrystalline and amorphous material which has been confirmed using electron diffraction analysis [15]. The average hexagonal lattice parameters \((a, c)\) of the nanocrystalline phase determined from XRD data using a full pattern least squares “Pawley method” are much larger \((a = 9.380 \text{ Å}, c = 12.260 \text{ Å})\) than those of the conventional powder \((a = 9.198 \text{ Å}, c = 11.495 \text{ Å})\). Larger lattice parameters are usually observed when the grain size is just a few nanometers [17]. The grain size and lattice strain of the HIP samples were calculated from the XRD data using the Hall-Williamson method [18] in which \(F \cos \theta / \lambda = 1/d + 4\varepsilon \sin \theta / \lambda\), where \(F\) is the difference of the full width at half maximum (FWHM) between the nanocrystalline sample and the conventional sample, \(d\) is grain size, \(\varepsilon\) is lattice strain, and \(\theta\) is Bragg angle. After HIP at 800 °C, relatively sharp XRD peaks appeared due to crystallization of the amorphous phase and grain growth \((d = 20 \text{ nm}, \varepsilon = 0.07\%\), \(a = 9.220 \text{ Å}, \text{ and } c = 11.455 \text{ Å})\). With increasing temperature of annealing, the XRD peaks became even sharper but still broader than those of the conventional sample (sample 1). Hence, disordered nanocrystalline bulk samples (samples 2 and 3) with grain sizes between 20 and 90 nm were obtained, as shown in Table I.

Table I presents the values of the normal state resistivity at 16 K \(\left[\rho_N\right.\text{ (16 K)}\)), room-temperature resistivity ratios \((RRR)\), and critical temperature \((T_C)\). The values of \(T_C\) determined using the criterion of 0.95\(\rho_N\) systematically decrease from 15.05 K for sample 1 to 12.30 K for sample 3 correlated with a decrease in \(RRR\) and a large increase in \(\rho_N\) (16 K) from 80 to 680 \(\mu\Omega\text{ cm}\).

The magnetization of the samples was measured in magnetic fields up to 12 T at temperatures up to \(\sim15\text{ K}\) using a commercial vibrating sample magnetometer.

Figure 2 shows the magnetization magnetic field \((M-H)\) curves obtained for samples 1 and 3 after subtracting the background. The reversible region of the \(M-H\) loops at the highest fields (typically above 9 T) was extrapolated to zero magnetization at each temperature to obtain experimental values of \(\partial M / \partial B\) at \(T_C\), and \(\partial B_{C2} / \partial T\) at \(T_C\). \(B_{C2}(0)\) was then calculated using Werthamer-Helfand-Hohenberg theory [19]:

\[
B_{C2}(0) = -0.7T_C \partial B_{C2} / \partial T\bigg|_{T_C}.
\]

The Ginzburg-Landau parameter, \(\kappa\), was calculated using the Abrikosov equation [20]:

\[
\mu_0 M = \frac{(B_{C2} - B)}{(2\kappa^2 - 1)\beta_A} \bigg|_{B_{C2}},
\]

where \(\beta_A = 1.16\). The value of the coherence length, \(\xi(0)\), at zero temperature was calculated by employing the Ginzburg-Landau relations:

| No. | Type | \(d\) (nm) | \(\rho_N(16\text{ K})\) (\(\mu\Omega\text{ cm}\)) | \(RRR^a\) | \(T_C^b\) (K) | \(-\partial B_{C2}/\partial T\) (TK\(^{-1}\)) | \(B_{C2}(0)\) (T) | \(\xi(0)^c\) (nm) | \(\gamma\) (JK\(^{-2}\) m\(^{-3}\)) | \(B_C(0)\) (T) | \(J_C^d\) (10\(^8\) Am\(^{-2}\)) |
|-----|------|----------|-----------------|--------|-------------|-----------------|-------------|-------------|----------|-------------|-----------|-----------|
| 1   | Conventional | 2000\(^a\) | 80 | 7.8 | 15.05 | 4.6 | 45 | 125 | 2.2 | 380 | 0.22 | 6.5 |
| 2   | Milled | 90 | 360 | 2.0 | 14.40 | 7.3 | 65 | 240 | 1.9 | 250 | 0.16 | 20 |
| 3   | Milled | 20 | 680 | 1.4 | 12.30 | 14.1 | 110 | 520 | 1.4 | 200 | 0.13 | 19 |
| 4\(^f\) | Doped | 2000\(^a\) | 280 | 3.3 | 14.80 | 5.1 | 50 | 160 | 2.1 | 270 | 0.19 | 12 |
| 5\(^f\) | Doped | 2000\(^a\) | 800 | 1.6 | 13.65 | 5.0 | 45 | 260 | 2.3 | 100 | 0.10 | 6.0 |

\(^a\)\(RRR = \rho_N(290\text{ K}) / \rho_N(16\text{ K})\).

\(^b\)\(T_C\) was determined by resistivity measurement using the criterion of 0.95\(\rho_N\)—all superconducting parameters were calculated with \(T_C\) obtained from the magnetic measurements.

\(^c\)\(\xi(0)\) is the coherence length at zero temperature.

\(^d\)\(J_C\) at 4.2 K and zero magnetic field was calculated from the magnetic hysteresis data using the critical state model [16].

\(^e\)The average grain size was determined using scanning electron microscopy.

\(^f\)Samples 4 and 5 are the Cu doped samples, Pb\(_1-x\)Cu\(_x\)Mo6S8 with \(x = 0.02\) and 0.10, respectively, and HIP at the pressure of 2000 bars and the temperature of 800 °C for 8 h.
$B_{C^2}(T) = \frac{\Phi_0}{2\pi \xi^2(T)} \bigg|_{T_C},$  

$$\xi(T) = \xi(0)(1 - T/T_C)^{-0.5} |_{T_C},$$

where $\Phi_0 = 2.07 \times 10^{-15} \text{ Wb}$ [21].

The Sommerfeld constant ($\gamma$) and the thermodynamic critical field at zero temperature, $B_{C^2}(0)$, were calculated using a Ginzburg-Landau relation and results from microscopic theory in the BCS limit [22]:

$$B_{C^2}(T) = \sqrt{2\kappa(T_C)}B_C(T)|_{T_C},$$

$$(\frac{\partial B_C(T)}{\partial T})|_{T_C} = -1.20\mu_0^{1/2} \gamma^{1/2},$$

$$B_C(0) = 0.69\mu_0^{1/2} \gamma^{1/2}T_C.$$

Table I shows the parameters obtained. Sample 3 has a substantially higher value of $-\partial B_{C^2}/\partial T|_{T_C}$ (14.1 TK$^{-1}$) than sample 1 (4.6 TK$^{-1}$) and a commensurately higher value of $B_{C^2}(0)$ (110 T compared to 45 T). In the nanocrystalline samples, $\kappa$ increases and $\xi(0)$ decreases with increasing $\rho_N$. Importantly, the disorder reduces the value of $\xi(0)$ to a much smaller value than the grain size ($d$), which indicates a high level of intragranular defects and is consistent with the change in lattice parameters determined from XRD data and reported for nanocrystalline materials that have been supersaturated with vacancies [17]. The values of $B_C(0)$ for the nanocrystalline and standard polycrystalline samples are similar and confirm that the higher values of $B_{C^2}(0)$ are bulk properties. Despite the large range of reversible magnetization (see Fig. 2), the value of critical current density ($J_C$) at 4.2 K and zero field is $\sim 2.0 \times 10^9 \text{ Am}^{-2}$ as shown in Table I, the highest reported in bulk materials of PbMo$_6$S$_8$. The high value of $J_C$ is believed to be due to the increase in intragranular defects and grain boundaries acting as pinning centers [23] and improved intergranular connectivity.

Resistive measurements made on samples 1 and 3 in magnetic fields up to 15 T and temperatures 6 to 16 K are shown in Fig. 3. For sample 1, increasing the magnetic field results in a shift of the entire resistive transition to lower temperature, characteristic of conventional low temperature superconductors. In contrast, the high-resistivity nanocrystalline sample 3 has a nearly constant onset temperature for superconductivity with a broadened transition in high fields characteristic of the Y-, Bi-, and Tl-cuprate high-temperature superconductors [24]. If an arbitrary resistive criterion of, for instance, 0.95$\rho_N$ is used, the value of $B_{C^2}(0)$ is $\sim 68 \text{ T}$ for sample 3, much higher than 53 T for sample 1. However, as reported for the high-temperature superconductor YBa$_2$Cu$_3$O$_7$, there was no distinct identifiable feature of $B_{C^2}$ in the resistive data [24].

In order to compare the nanocrystalline samples with doped samples, Table I lists the superconducting parameters of two Cu doped PbMo$_6$S$_8$ samples, Pb$_{1-x}$Cu$_{1.8}$Mo$_6$S$_8$ with $x = 0.02$ (sample 4) and 0.10 (sample 5), respectively. The values of $\rho_N$ (16 K) increase with increasing Cu content. A combination of relatively high $\rho_N$(16 K) = 800 $\mu\Omega\text{cm}$ and $T_C = 13.65 \text{ K}$ were obtained in the Cu doped sample 5. However, sample 4 shows only a slight increase in $B_{C^2}(0)$ to 50 T. Further increasing Cu content to $x = 0.10$ leads to a decrease of $B_{C^2}(0)$ to 45 T (sample 5). A similar behavior with doping has also been found in Nb$_2$Sn [7,8].

The reduction in $\gamma$, shown in Table I, for the milled and doped samples compared to the conventional sample is consistent with a very general consideration of the uncertainty relation $\Delta E \Delta \tau = \hbar$ which suggests that...
they have similar Table I is compared with the nanocrystalline sample 3, by phonon softening [7]. If the Cu doped sample 5 in coupling as found in other superconductors [27] produced materials and possibly an increase in the electron-phonon samples may result from the strong coupling in these materials and possibly an increase in the electron-phonon coupling as found in other superconductors [27] produced by doping. Future research into metastable materials may yet provide a new class of highly disordered superconductors with very high $B_{c2}(0)$.

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**FIG. 3.** Resistive superconducting transitions measured at magnetic fields up to 15 T. (a) Sample 1; (b) sample 3.

increased disorder will tend to smear out and, hence, reduce any peak in the density of states and $\gamma$ [25]. Strong electron-phonon coupling, in which $T_c$ is less sensitive than weak coupling to changes in the electron density of states, is well established in Chevrel phase compounds [26]. Hence, given the effect of disorder on $\gamma$, the relatively small reduction in $T_c$ found in all the samples may result from the strong coupling in these materials and possibly an increase in the electron-phonon coupling as found in other superconductors [27] produced by phonon softening [7]. If the Cu doped sample 5 in Table I is compared with the nanocrystalline sample 3, they have similar $\rho_N$ and $T_c$, but $\gamma$ is different by a factor of $\sim 2$. Hence, nanocrystalline disorder is significantly more effective than doping at increasing scattering without reducing the electronic density of states. Indeed, it can be noted that an enhancement of $\gamma$ has been predicted by theory for some nanocrystalline materials [28,29] and found using low temperature specific heat measurements [13,29].

Intragranular defects found in the disordered nanocrystalline materials produce electron scattering on a smaller scale than the grain size. The disorder in the nanocrystalline materials has a significantly less detrimental effect on the electronic density of states than that produced by doping. Future research into metastable materials may yet provide a new class of highly disordered superconductors with very high $B_{c2}(0)$.

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