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# Black hole growth in hierarchical galaxy formation

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## ABSTRACT

We incorporate a model for black hole growth during galaxy mergers into the semi-analytical galaxy formation model based on  $\Lambda$ CDM proposed by Baugh et al. Our black hole model has one free parameter, which we set by matching the observed zero-point of the local correlation between black hole mass and bulge luminosity. We present predictions for the evolution with redshift of the relationships between black hole mass and bulge properties. Our simulations reproduce the evolution of the optical luminosity function of quasars. We study the demographics of the black hole population and address the issue of how black holes acquire their mass. We find that the direct accretion of cold gas during starbursts is an important growth mechanism for lower mass black holes and at high redshift. On the other hand, the re-assembly of pre-existing black hole mass into larger units via merging dominates the growth of more massive black holes at low redshift. This prediction could be tested by future gravitational wave experiments. As redshift decreases, progressively less massive black holes have the highest fractional growth rates, in line with recent claims of ‘downsizing’ in quasar activity.

**Key words:** galaxies: bulges – galaxies: formation – galaxies: nuclei – quasars: general – galaxies: starburst.

## 1 INTRODUCTION

In the local Universe, luminous, dusty, merger-driven starburst activity has long been suspected to have quasar activity associated with it (Sanders & Mirabel 1996). Some authors find that the most powerful Seyfert II active galactic nuclei (AGN) are usually found in galaxies which have had a starburst in the past 1–2 Gyr and use this observation to argue that the brightest quasars are associated with galaxy mergers (Kauffmann et al. 2003), whilst others claim that the brightest quasars are hosted in elliptical galaxies which are indistinguishable from the general elliptical population (Dunlop et al. 2003). At high redshift, sources detected in the submillimetre are thought to be starbursts (Chapman et al. 2004), many are associated with galaxy mergers (Swinbank et al. 2004) and many show evidence of active nuclei when probed deeply in the X-rays, although it appears that the AGN makes a much smaller contribution to the powerful submillimetre flux than the starburst (Alexander et al. 2003).

Black holes (BH) display strong correlations with the properties of their host galaxy, particularly those of the galactic bulge (Kormendy & Richstone 1995; Magorrian et al. 1998; Novak, Faber & Dekel 2006). BH mass is observed to scale with the bulge’s *B*-band luminosity (Magorrian et al. 1998; Kormendy & Gebhardt 2001), *K*-band luminosity (Marconi & Hunt 2003; Häring & Rix 2004), stellar mass (Marconi & Hunt 2003; Häring & Rix 2004) and velocity dispersion (Ferrarese & Merritt 2000; Gebhardt et al.

2000). We refer to these collectively as the ‘ $M_{\text{BH}}-M_{\text{bulge}}$ ’ relations. It has long been theorized that galactic bulges form through galaxy mergers (Toomre & Toomre 1972), so it is natural to speculate that these events also drive the strong correlation between the properties of the bulge and the mass of the BH.

There is strong evidence for a link between galactic star formation and accretion on to central BHs. The evolution with redshift of the global star formation rate (SFR) and the luminosity density of optical quasars are strongly correlated (Boyle & Terlevich 1998). At low redshift, the ratio of the global SFR to the global BH accretion rate for bulge dominated galaxies,  $\text{SFR}/M_{\text{BH}}$  is  $\sim 1000$ , which is remarkably similar to the ratio of  $M_{\text{BH}}/M_{\text{bulge}}$  (Heckman et al. 2004). However, it is still an open question whether BH growth is correlated with all star formation equivalently, or whether its strongest relationship is with star formation in bursts.

The physical conditions in mergers and starbursts are amenable to fuelling the accretion of material on to a central supermassive BH. Numerical simulations of galaxy mergers have shown that the asymmetrical gravitational potential present during the merger is responsible for driving gas to the centres of the merging galaxies and of their remnant in both major mergers (Mihos & Hernquist 1994b) and minor mergers (Mihos & Hernquist 1994a). The enhanced supply of gas to the centre of the galaxy leads to rapid star formation and is also available to fuel an AGN (Norman & Scoville 1988; Di Matteo, Springel & Hernquist 2005; Springel, Di Matteo & Hernquist 2005b). Furthermore, the formation of a dense stellar system with a steep  $R^{1/4}$ -law potential well during a gas-rich merger may help to funnel gas to the AGN at the very centre. Starbursts

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appear to be required in the high-redshift Universe to explain observations of various galaxy populations (Somerville, Primack & Faber 2001; Baugh et al. 2005). The increased prevalence of starbursts at early epochs may be responsible for the accelerated growth of the most massive BHs towards high redshift (e.g. Granato et al. 2004, 2006).

Theoretical calculations of the growth of BHs in the cold dark matter (CDM) cosmology in which structures grow through gravitational instability have tended to fall into one of three classes: (i) calculations based on the rate at which dark matter haloes are assembled, either without any treatment of galaxy formation (e.g. Efstathiou & Rees 1988; Haehnelt & Rees 1993; Haiman & Loeb 1998; Percival & Miller 1999; Wyithe & Loeb 2003; Haiman 2004; Koushiappas, Bullock & Dekel 2004; Yoo & Miralda-Escudé 2004; Mahmood, Devriendt & Silk 2005) or with very simple estimates of the supply of gas accreted on to the BH (Islam, Taylor & Silk 2003; Volonteri, Haardt & Madau 2003; Bromley, Somerville & Fabian 2004; Libeskind et al. 2006); (ii) numerical simulations of galaxy mergers, which use a mixture of smoothed particle hydrodynamics and simple recipes to follow the fuelling of a supermassive BH (Cattaneo et al. 2005a; Di Matteo et al. 2005; Hopkins et al. 2005; Springel et al. 2005b; Hopkins et al. 2006; Robertson et al. 2006); (iii) semi-analytical modelling of the formation of galaxies and BHs (Kauffmann & Haehnelt 2000; Cattaneo 2001; Enoki, Nagashima & Gouda 2003; Granato et al. 2004; Menci et al. 2004; Cattaneo et al. 2005b; Monaco & Fontanot 2005). Recently, the semi-analytical approach has been extended to produce models in which the evolution of galaxies and BHs are coupled, with energy released by accretion on to the BH either truncating ongoing star formation or suppressing the rate at which gas can cool in more massive haloes (Granato et al. 2004; Monaco & Fontanot 2005; Bower et al. 2006; Croton et al. 2006).

In this paper, we incorporate a model for the growth of BHs into the Durham semi-analytical galaxy formation code GALFORM (Cole et al. 2000; Benson et al. 2003b). Our prescription for growing BHs is tied to galaxy mergers and is similar to the first implementation of BH growth in semi-analytical models by Kauffmann & Haehnelt (2000). Our starting point is the galaxy formation model introduced by Baugh et al. (2005). This was the first model to match the observed properties of galaxies in both the low- and high-redshift Universe, following the whole of the galaxy population and incorporating a self-consistent calculation of the reprocessing of starlight by dust. In particular, the model reproduces the number counts of Lyman-break galaxies and submillimetre sources, which are both dominated by starbursts. The success of the model is primarily due to an increased level of star formation in bursts at high redshift compared with previous models, and the adoption of a flat initial mass function (IMF) for stars produced in starbursts. The same model also accounts for the metal content of the hot gas in clusters and stars in ellipticals (Nagashima et al. 2005a,b) and the numbers of Lyman  $\alpha$  emitters (Le Delliou et al. 2005, 2006). Since the Baugh et al. model has been tested extensively, and, in particular, in view of the success of this model in reproducing aspects of the galaxy population which are associated with starbursts (and hence bulge formation), we have chosen to focus on the predictions for BH growth and quasar activity.

The use of a semi-analytical model allows us to follow a much wider population of objects than is accessible by direct numerical simulation. This means that we can follow the demographics of the BH population and explore how BHs acquire their mass. The latter is of great importance in view of the recent observational evidence suggesting that the most massive BHs acquired the bulk of their mass at early epochs and that it is the lower mass BHs

which are being built up most rapidly today. This phenomenon has been termed ‘downsizing’ (Cowie et al. 2003; Steffen et al. 2003; Ueda et al. 2003; Barger et al. 2005; Hasinger, Miyaji & Schmidt 2005). At first sight, downsizing appears to imply that the growth of BH mass is ‘antihierarchical’ and thus incompatible with the CDM cosmological framework (Marconi et al. 2004; Merloni 2004; Shankar et al. 2004). We will examine here whether or not such downsizing is really a problem for hierarchical models of galaxy formation.

The paper is organized as follows. We provide a description of the model in Section 2. The model contains one free parameter, which we set by matching the  $z = 0$   $M_{\text{BH}}-M_{\text{bulge}}$  relations in Section 3, where we also show that our model is consistent with the evolution of the quasar luminosity function. In Section 4, we study the growth histories of BHs, separating the contributions from BH mergers and direct gas accretion, and show how the relative importance of these channels varies with BH mass. We predict the evolution of the  $M_{\text{BH}}-M_{\text{bulge}}$  relations and compare this to data in Section 5. We demonstrate that we are able to produce downsizing in the AGN population in Section 6. We summarize our main results, discuss their context and outline future improvements to the model in Section 7.

## 2 METHOD

In this section we first give a brief overview of our galaxy formation model (Sections 2.1 and 2.2), before explaining how the model has been extended to follow the formation of BHs (Section 2.3). We discuss the sensitivity of our model predictions to the mass resolution of the dark matter merger trees in Section 2.4. We end this section with a brief description of how a quasar luminosity is assigned to an accreting BH, and present some illustrative results for the quasar luminosity function at selected redshifts (Section 2.5).

### 2.1 The semi-analytical galaxy formation model

Our starting point is the model for galaxy formation in the CDM cosmology described by Baugh et al. (2005). As we have already pointed out in Section 1, in addition to giving a reasonable match to the properties of galaxies in the local Universe, this model also reproduces the counts of submillimetre sources and the luminosity function of Lyman-break galaxies at high redshift. In both cases, the model associates these high-redshift objects with galaxies which are undergoing merger-driven starbursts. The success of the Baugh et al. (2005) model in reproducing observations linked with vigorous starbursts and the formation of spheroids is important for the current analysis. Here we will follow the proposal of Kauffmann & Haehnelt (2000) and assume that BH growth is driven by galaxy mergers. For a more exhaustive description of the physics and methodology behind the semi-analytical model, we refer the reader to Cole et al. (2000) and Benson et al. (2003b). A gentler introduction to hierarchical galaxy formation may be found in Baugh (2006).

We will review the aspects of the model which control the outcome of galaxy mergers in the next subsection, and will limit ourselves here to more general aspects of the cosmological and galaxy formation models. We assume a standard  $\Lambda$ CDM cosmology, with a flat geometry, a matter density  $\Omega_0 = 0.3$ , a baryon density  $\Omega_b = 0.04$ , a Hubble constant of  $H_0 = 70 \text{ kms}^{-1} \text{ Mpc}^{-1}$  and a fluctuation amplitude specified by  $\sigma_8 = 0.9$ . The break in the local galaxy luminosity function is reproduced by invoking a superwind which drives cold gas out of galaxies (Benson et al. 2003b; Nagashima et al. 2005a); an alternative physical mechanism to produce this break is

AGN feedback in quasi-hydrostatically cooling haloes (Bower et al. 2006; Croton et al. 2006). Gas cooling is prevented below  $z = 6$  in low circular velocity haloes ( $v_c = 60 \text{ km s}^{-1}$ ), to mimic the impact of the presence of a photoionizing background on the intergalactic medium (IGM) (Benson et al. 2002). Baugh et al. (2005) adopt a time-scale for quiescent star formation in galactic discs which is independent of the dynamical time, which results in gas-rich mergers at high redshift (see their fig. 1). They assume that stars which form in bursts are produced with a top-heavy IMF; this choice has no impact on the predictions presented in this paper beyond the high fraction of cold gas forming stars that is recycled into the IGM.

The parameters of the Baugh et al. (2005) galaxy formation model are held fixed in this paper; we do not adjust these parameters in any way when generating predictions for BHs and quasars. This is a clear strength of our approach and choice of galaxy formation model. Thus, our results are to be viewed as genuine predictions of the model. The properties of the quasars and active nuclei in our model can easily be related to the properties of their host galaxies; such comparisons are deferred to future papers.

## 2.2 Galaxy mergers

Mergers between galaxies play an important role in building up the mass and determining the morphology of galaxies. When dark matter haloes merge in our model, the galaxies they contain are ranked in mass. The most massive one is designated as the ‘central’ or ‘primary’ galaxy in the new dark halo and the remaining galaxies become its satellites. The satellites lose any hot gas reservoir that they may have had prior to the merger and any subsequent accretion of cooling gas is funnelled into the central galaxy. The orbits of the satellite galaxies decay through dynamical friction. If the time-scale for a satellite to sink to the centre of the halo is shorter than the lifetime of the halo, then the satellite is merged with the central galaxy at the appropriate time (see e.g. Cole et al. 2000).

The result of a galaxy merger is determined by two principal quantities: (i) the ratio of the mass of the accreted satellite to the mass of the primary,  $f_{\text{merge}} = M_{\text{smaller}}/M_{\text{larger}}$  and (ii) the fraction of the mass of the primary disc which is cold gas,  $f_{\text{gas}} = M_{\text{cold,primary}}/M_{\text{disc,primary}}$ , where  $M_{\text{disc}} = M_{\text{stars}} + M_{\text{cold}}$ . If the mass ratio exceeds a threshold  $f_{\text{ellip}}$ , the merger is termed ‘violent’ or ‘major’. In this case, all stars present are rearranged into a spheroid, with a radius determined by arguments based on the conservation of energy and the virial theorem (see Cole et al. 2000; Almeida, Baugh & Lacey 2007). In addition, any cold gas in the merging galaxies is assumed to undergo a star formation burst and the stars thus produced are added to the new spheroid. In this paper, we use the parameters set by Baugh et al., who defined major mergers by the threshold  $f_{\text{ellip}} = 0.3$ .

In cases where  $f_{\text{merge}} < f_{\text{ellip}}$ , the merger is termed ‘minor’. In this case, the stars in the accreted satellite are added to the spheroid of the primary, leaving intact any stellar disc present in the primary. In minor mergers, the fate of the gas in the merging galaxies depends upon the gas fraction in the primary disc and on the value of  $f_{\text{merge}}$ . If the primary disc is gas-rich (if  $f_{\text{gas}} > f_{\text{gas,burst}}$ , where, following Baugh et al., we take  $f_{\text{gas,burst}} = 0.75$ ), and if  $f_{\text{merge}} > f_{\text{burst}}$  (where Baugh et al. adopted  $f_{\text{burst}} = 0.05$ ), then we assume that the perturbation introduced by the merging satellite is sufficient to drive all the cold gas, from both the primary and the satellite, into the spheroid, where it takes part in the burst. Otherwise, if in a minor merger the gas fraction in the primary disc is small, no burst occurs. Alternatively, if the secondary galaxy is very much less massive than the primary (i.e. if  $f_{\text{merge}} < f_{\text{burst}}$ ) then the primary disc remains unchanged, the accreted stars are added to the spheroid and there

is no burst, irrespective of  $f_{\text{gas}}$ . The refinements of the Cole et al. (2000) model relating to minor mergers were described by Baugh et al. (2005), who also set the values of  $f_{\text{burst}}$ ,  $f_{\text{ellip}}$  and  $f_{\text{gas,burst}}$ .

During a starburst, we assume that all of the cold gas available at the start,  $M_{\text{cold}}$ , is processed by the burst and suffers one of three fates. (i) It is reheated by supernova feedback and returned to the hot interstellar medium (ISM). (ii) It is ejected from the dark matter halo by a superwind. (iii) It forms long-lived stellar remnants. The mass of gas which forms long-lived stellar remnants in the burst,  $\Delta M_{\text{stars}}$ , depends on the feedback prescription used, and is calculated as follows:

$$\Delta M_{\text{stars}} = \frac{(1 - e^{-\text{efold}})(1 - R_{\text{burst}})}{(1 - R_{\text{burst}}) + \beta_{\text{burst}} + f_{\text{sw,burst}}} M_{\text{cold}}. \quad (1)$$

For completeness, we now define the parameters in this equation (for further details see Cole et al. 2000; Granato et al. 2000; Baugh et al. 2005).

(i)  $\beta_{\text{burst}} = (V_{\text{circ,bulge}}/200 \text{ km s}^{-1})^{-2}$ , where  $V_{\text{circ,bulge}}$  is the effective circular velocity of the bulge. This quantity gives the rate at which cold gas is reheated by supernova feedback in units of the SFR. This reheated gas is returned to the hot gas reservoir and is allowed to recool once a new halo forms (i.e. when the halo has doubled in mass).

(ii)  $f_{\text{sw}}$  gives the rate of ejection of cold gas by superwinds, in units of the SFR. This gas is ejected from the dark halo and is not allowed to recool. This parameter has the following dependence on the effective circular velocity of the bulge:

$$f_{\text{sw}} = f_{\text{sw0}} \quad \text{for} \quad V_{\text{circ}} < V_{\text{sw}}, \quad (2)$$

$$f_{\text{sw}} = f_{\text{sw0}} \left( \frac{V_{\text{sw}}}{V_{\text{circ}}} \right)^2 \quad \text{for} \quad V_{\text{circ}} > V_{\text{sw}}. \quad (3)$$

The superwind feedback model was introduced by Benson et al. (2003b). Baugh et al. (2005) set  $f_{\text{sw0}} = 2$  and  $V_{\text{sw}} = 200 \text{ km s}^{-1}$ .

(iii)  $R_{\text{burst}}$  is the fraction of the mass turned into stars which we assume is instantaneously recycled into high-mass supernovae and returned to the cold phase of the ISM. For the flat IMF used in bursts,  $R_{\text{burst}} = 0.41$ .

(iv)  $\text{efold}$  is the number of e-foldings over which star formation (assumed to have an exponentially declining rate) is allowed to take place in a burst. We follow Baugh et al. (2005), taking  $\text{efold} = 3$ .

## 2.3 The growth of black holes in galaxy centres

The observed correlation between the inferred mass of galactic central BHs and the properties of their host spheroids suggests a common origin for these two classes of object (e.g. Magorrian et al. 1998; Ferrarese & Merritt 2000; Gebhardt et al. 2000). We adopt a model of BH growth similar to that implemented for the first time in a fully fledged semi-analytical galaxy formation by Kauffmann & Haehnelt (2000).

We assume that any contribution to the BH mass from processes other than galaxy mergers (e.g. the end products of Population III stars, primordial BHs or accretion on to BHs from galactic discs or from the hot gas within a halo) is negligible compared with the change in BH mass which occurs during merger-driven starbursts or through BH mergers following a galaxy merger. Hence, the first galaxies to form in our model, when gas first cools into galactic discs, do not contain a significant BH mass. The first important growth of BH mass is assumed to occur during the first merger-triggered starburst. Our reason for this choice is that the physics of BH seeding is very uncertain, and many mechanisms of BH seeding

have been proposed, with widely varying associated seed masses (see Volonteri 2006, and references therein). The largest mass of seed BHs suggested by models in the current literature is  $\sim 10^5$ – $10^6 M_\odot$  (e.g. Bromm & Loeb 2003; Volonteri & Rees 2005; Lodato & Natarajan 2006). These models typically apply only to metal-free and highly biased regions at high redshift and probably therefore only to the seeding of the most massive BHs (they are motivated by the difficulty in producing  $\sim 10^9 h^{-1} M_\odot$  BHs at  $z \sim 6$  from smaller seeds, since at high redshifts the age of the Universe is not long compared to the Salpeter time). Other models for seed BHs predict seeds which are less massive than  $10^5 h^{-1} M_\odot$ , which is our BH mass resolution limit. Therefore, it is reasonable for us to neglect the role of seed BHs in our calculations. In practice, we assume that if a pre-existing seed is indeed required for supermassive BH formation, then the mass is small enough that it only makes a negligible contribution to the mass of the final BH. Furthermore, theoretical considerations (e.g. Begelman 1978, 2002; King 2002) and observations (e.g. Collin & Kawaguchi 2004) suggest that super-Eddington accretion of mass is possible, and we assume that this occurs during the early stages of BH growth, so that the mass of any seed does not affect the final mass by Eddington limiting of mass accretion.

The mass of BHs is assumed to grow during galaxy mergers via two channels, accretion of gas during merger-driven starbursts and mergers with other BHs. (Note that in the recent model by Bower et al. 2006, additional modes of BH growth are considered: accretion during starbursts triggered by disc instabilities, and accretion of cooling gas from quasi-hydrostatically cooling haloes.) As discussed in Section 2.2, we allow starbursts, and thus accretion, in both major and minor mergers. (In contrast, Kauffmann & Haehnelt 2000 only allowed starbursts and BH accretion during major galaxy mergers.) The two channels for BH growth are as follows.

First, in starbursts triggered by galaxy mergers, we assume that a fraction,  $F_{\text{BH}}$ , of the gas mass which is turned into stars is accreted on to the BH:

$$\Delta M_{\text{BH}} = F_{\text{BH}} \Delta M_{\text{stars}}, \quad (4)$$

where  $\Delta M_{\text{BH}}$  is the mass added to the BH and  $\Delta M_{\text{stars}}$  is the mass of stars produced in the burst *after* taking into account feedback processes that may expel gas from the galaxy and the recycling of mass from stars (equation 1; see Cole et al. 2000; Granato et al. 2000). Typically, we use  $F_{\text{BH}} < 0.03$  (this is explained in Section 3.1), and so for simplicity we ignore the depletion of the cold gas reservoir by BH growth when we calculate star formation. We assume that the growth of BH mass is not limited to the Eddington accretion rate appropriate to our chosen radiative efficiency.

Secondly, if the merging galaxies already host BHs, then we assume that these BHs merge when the host galaxies merge. In reality, BHs do not merge instantaneously, but gas-dynamical processes are likely to speed up BH coalescence in gas-rich mergers (Armitage & Natarajan 2002) and circumstantial observational evidence exists to suggest that most binary BHs do merge efficiently, even in gas-poor mergers (Merritt & Milosavljević 2005). Since we only consider binary galaxy mergers with instantaneous central BH merging, all BH–BH mergers in our model are binary, and we ignore slingshot ejection of BHs from the galactic centre (Saslaw, Valtonen & Aarseth 1974). We also ignore the recoil of the merger products of unequal-mass BHs due to the anisotropic emission of gravitational waves, which may lead to the resultant BH being ejected from the galaxy nucleus (Fitchett 1983; Volonteri et al. 2003; Libeskind et al. 2006). Recent calculations suggest that most recoil velocities are likely to

be in the range  $10$ – $100 \text{ km s}^{-1}$  (Favata, Hughes & Holz 2004), and thus unimportant except in very low-mass galaxies.

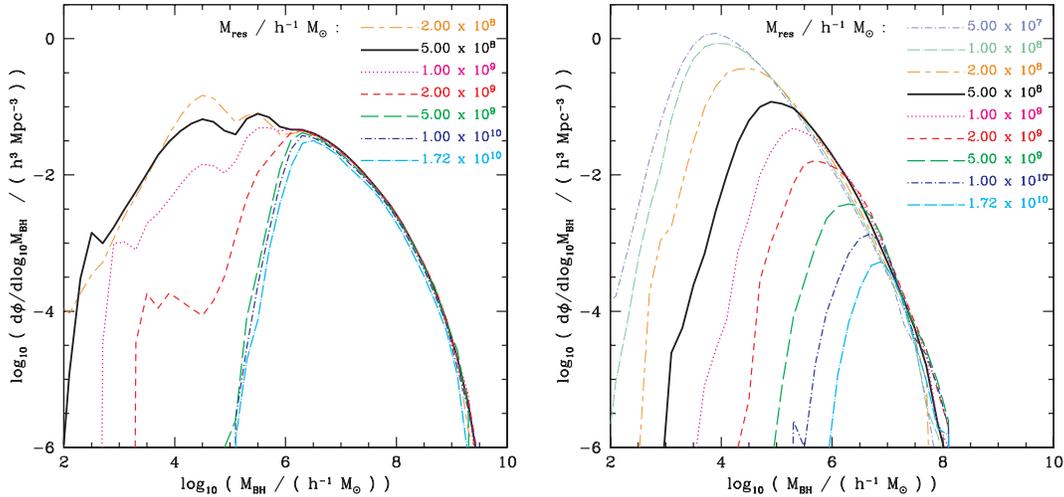
Note that we neglect any loss of mass arising from the radiation of gravitational waves during the merger of two BHs. Such radiation could result in the mass of the merger product being less than the sum of the masses of the BHs from which it formed (Yu & Tremaine 2002). This effect is very uncertain, but is maximal for equal-mass BHs, and even then it is likely to be small – approximately 3 per cent or less of the initial mass energy for equal-mass non-spinning or Kerr BHs (Baker et al. 2002, 2004). Since most BH–BH mergers in the Universe have unequal mass ratios, the cumulative mass-loss by gravitational radiation is unlikely to be more than the figure of 20 per cent predicted using the most extreme models for gravitational wave loss in individual BH–BH mergers (Menou & Haiman 2004). Therefore, we assume that the final BH mass is the sum of the mass accreted plus the mass of the two progenitors.

## 2.4 Resolution tests

The BH mass down to which our predictions for the properties of BHs can be trusted depends upon two factors: the accuracy of our prescriptions for handling the physical ingredients of our galaxy formation model and the mass resolution of the dark matter halo merger trees. The semi-analytical galaxy formation model gives a reasonable match to the field galaxy luminosity function, including its faint end (Benson et al. 2003b). Further tests of the modelling of the phenomena operating in low-mass systems are deferred to future work. This leaves the mass resolution of the halo merger trees as a numerical parameter that directly influences the properties of low-mass BHs.

In this paper, we use dark matter halo merger trees generated using the Monte Carlo scheme described by Cole et al. (2000). Merger trees extracted from  $N$ -body simulations are, in some respects, more accurate (e.g. Kang et al. 2005; Nagashima et al. 2005c). However, a major limitation of the trees extracted from simulations is their finite mass resolution. Unpublished work by one of us (CGL) and work in preparation by Helly et al. show that the merger trees in the Durham semi-analytic model agree well with the merger trees in  $N$ -body simulations. Monte Carlo generated trees can have far superior mass resolution, because the whole of the computer memory is devoted to one tree at a time, rather than to a large ensemble of haloes within a cosmological volume. This also means we are able to extend our merger trees to high redshifts (we use  $z_{\text{start}} = 20$ ). Also, Monte Carlo trees typically have superior time resolution to those taken from  $N$ -body simulations. On the other hand, Monte Carlo trees tend to become less accurate as the time interval over which the trees are grown is increased (Somerville et al. 2000).

Putting this caveat aside, we have performed extensive tests of the impact of the choice of resolution of the dark matter merger trees on our predictions for the mass function of BHs. The results of this convergence study are presented in Fig. 1 for  $z = 0$  and 6. With improved mass resolution in the merger tree, we are able to trace more of the gas which cools in low-mass haloes before reionization. This is the reason for the odd-looking ‘bumps’ at low BH masses in the  $z = 0$  panel. Our fiducial choice of halo mass resolution is  $5 \times 10^8 h^{-1} M_\odot$ . This is an order of magnitude better than the resolution used in our standard galaxy formation calculations, and 30 times better than the resolution of the best  $N$ -body merger trees currently available within a cosmological volume [the Millennium Simulation of Springel et al. (2005a) which can resolve haloes of mass  $1.72 \times 10^{10} h^{-1} M_\odot$ ]. With our fiducial halo mass resolution,



**Figure 1.** The mass function of BHs, computed using different resolutions for the merger trees of dark matter haloes, as indicated by the legend in each panel. Our fiducial resolution is shown by the thick solid line. The left-hand panel shows the results for  $z = 0$  and the right-hand panel shows  $z = 6$ .

our predictions for the mass function of BHs have converged for masses of  $10^5 h^{-1} M_{\odot}$  and above.

### 3 DEFINING THE MODEL: COMPARISON WITH OBSERVATIONAL DATA

We first fix the value of the main parameter in our BH model,  $F_{\text{BH}}$ , which determines the mass accreted on to the BH during a starburst (see Section 2.3). In Section 3.1, we set  $F_{\text{BH}}$  by requiring that the model should reproduce the local observed relationship between BH mass ( $M_{\text{BH}}$ ) and the stellar mass of the bulge ( $M_{\text{bulge}}$ ) in which it resides. We also show the model predictions for how BH mass scales with other properties of the bulge. Any viable model of BH growth should also be consistent with the observed quasar population. In Section 3.2, we briefly describe how a quasar luminosity can be assigned to accreting BHs, and present some illustrative results for the quasar luminosity function at selected redshifts.

#### 3.1 Setting the model parameter: predictions for the present-day bulge–BH relation

The main parameter of our BH model is the fraction,  $F_{\text{BH}}$ , of the mass of stars formed in a starburst which is accreted on to the central BH (after taking into account gas ejected from the galaxy by feedback processes and the recycling of mass in supernova explosions and stellar winds, as described in Section 2.1). We fit the value of  $F_{\text{BH}}$  by comparing the model predictions to the observed correlation between the mass of galactic central BHs and the stellar mass of the bulge component,  $M_{\text{BH}}-M_{\text{bulge}}$ , as inferred by Häring & Rix (2004). Häring & Rix make a dynamical estimate of the stellar mass of the bulge. They compile from the literature BH mass estimates made using a variety of techniques (stellar, gas or maser dynamics). A review of these techniques and their uncertainties can be found in Kormendy & Gebhardt (2001).

We find that a value of  $F_{\text{BH}} = 0.022$  is required for the model to match the zero-point of the observed  $M_{\text{BH}}-M_{\text{bulge}}$  relationship (Fig. 2a). It is important to remember that the normalization of this relationship is set by the choice of  $F_{\text{BH}}$ . However, the slope and scatter are genuine model predictions, and as Fig. 2 shows, these predictions are in good agreement with the observations.

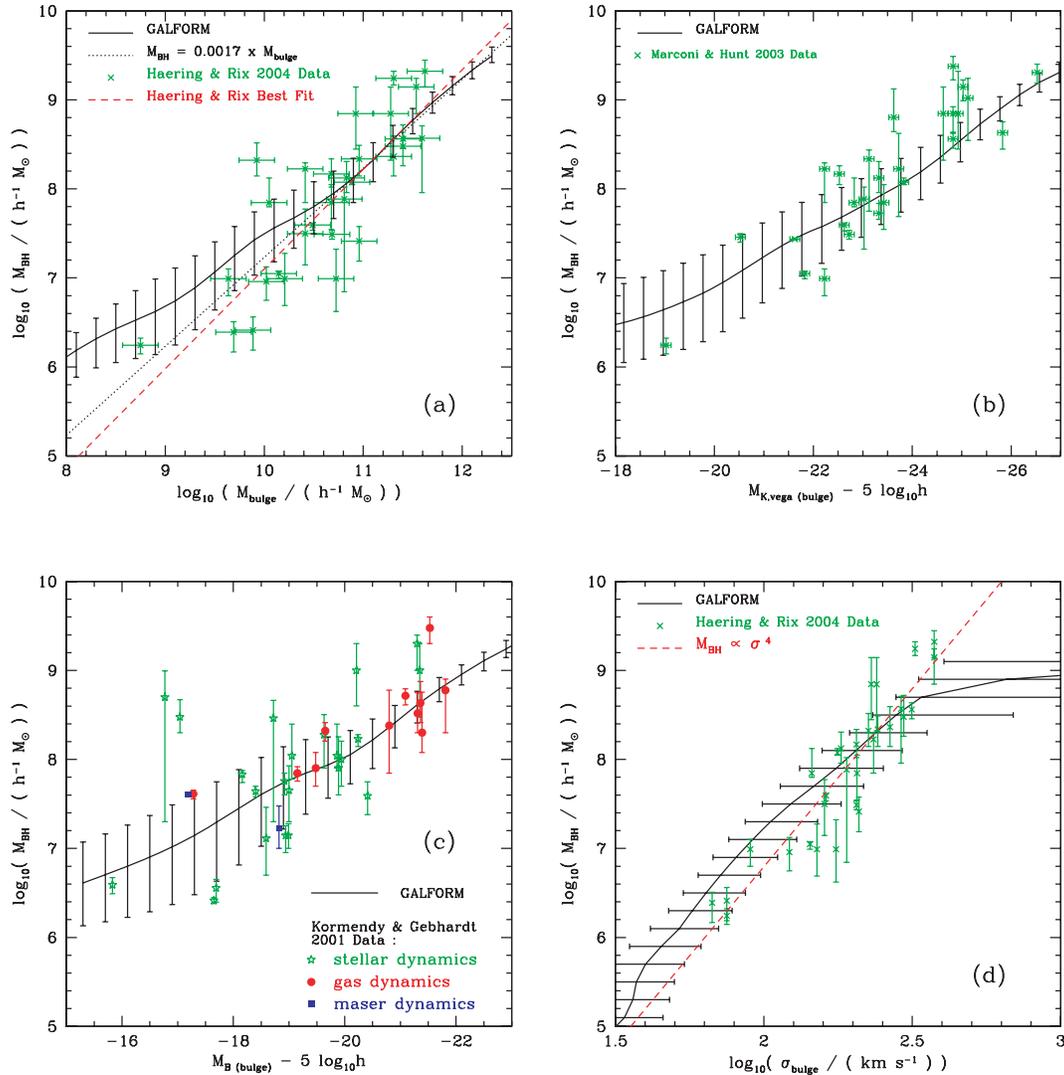
Naïvely one might argue that, since we have assumed that a fixed fraction of the mass of stars formed in a burst is added to the mass of the BH, it is hardly surprising that a tight  $M_{\text{BH}}-M_{\text{bulge}}$  relationship results.

We find in the Baugh et al. model that bursts actually play a fairly minor role in the formation of bulge stars. The dominant channel responsible for building up the mass of present-day spheroids is the re-assembly of pre-existing stellar fragments during mergers, not the burst accompanying the most recent major merger experienced by the galaxy (Baugh, Cole & Frenk 1996). We find that only 15 per cent of the stellar mass in bulges at redshift zero was formed in bursts. The other 85 per cent of the stars in bulges was originally formed quiescently, in discs, and no BH accretion is associated with the formation of these stars. Thus, the slope and scatter of the  $M_{\text{BH}}-M_{\text{bulge}}$  relation are non-trivial predictions of the model. Essentially, the  $M_{\text{BH}}-M_{\text{bulge}}$  relation results from the evolution in bulge star formation (and in particular the fraction of bulge stars which were formed quiescently) in our galaxy formation model. This topic is discussed extensively by Croton (2006). The scatter is due to the variation in the fraction of the stellar mass of a bulge which was formed quiescently in discs, before being rearranged into the spheroid. The slope originates from how this fraction varies with stellar mass – as bulge mass increases, the fraction of stars which formed in starbursts decreases, so that BH accretion is associated with a lower fraction of the stars in the bulge.

Further support for both the galaxy formation model and our new model for the growth of BHs comes from examining the other relationships between BH mass and observable properties of the galactic spheroid, as shown in Figs 2(b)–(d).

In Fig. 2(b), we compare our model predictions for BH mass as a function of the  $K$ -band magnitude of the bulge with the measurements by Marconi & Hunt (2003). Again, the match is very good.  $K$ -band magnitudes correlate well with stellar mass. In the model, the  $K$ -band magnitude depends upon the star formation and merger history of the galaxy, taking into account all of the progenitors of the galaxy, its dust content and linear size. Observationally, this property is completely independent of the bulge stellar mass estimates based on the velocity profile fitting method used by Häring & Rix (2004).

It is notable that the scatter in both the  $M_{\text{BH}}-M_{\text{bulge}}$  and  $M_{\text{BH}}-M_K$  relations decreases significantly as the bulge magnitude gets



**Figure 2.** The relation between BH mass,  $M_{\text{BH}}$ , and a selection of properties of the spheroid of the host galaxy. Each panel shows the correlation with a different bulge property: (a) the stellar mass of the bulge; (b) the bulge rest-frame  $K$ -band magnitude; (c) the rest-frame  $B$ -band bulge magnitude; (d) the velocity dispersion of the bulge. The model predictions are shown by the line with error bars: the line shows the median and the error bars the 10–90 percentile spread of the distribution. The observational measurements are shown by symbols, with sources indicated in each panel.

brighter. A number of factors may contribute to this result. As shown in Section 4, less massive BHs vary far more in their formation histories than do larger BHs. Therefore, for bulges hosting less massive BHs, there is more scatter in the time available for stars to form in progenitor discs before starbursts and BH accretion occur. Stars in larger ellipticals and bulges tend to be formed earlier. Once stellar populations exceed a certain age, scatter in their ages have only a small impact on colour and luminosity.

In Fig. 2(c) we plot BH mass against the  $B$ -band magnitude of the bulge and compare the model with a compilation of data by Kormendy & Gebhardt (2001). The scatter in this relationship is the greatest of all four variations on the  $M_{\text{BH}}-M_{\text{bulge}}$  relations shown in Fig. 2. This is due to the sensitivity of the  $B$ -band magnitude to the details of the recent star formation history of the bulge which can vary considerably between galaxies with similar mass BHs.

Finally, in Fig. 2(d), we compare the model prediction for the  $M_{\text{BH}}-\sigma_{\text{bulge}}$  relation to data from Häring & Rix (2004). We calculate the velocity dispersion directly from the circular velocity of

the bulge, assuming  $\sigma_{\text{bulge}} = 1.1 V_{\text{circ,bulge}}/\sqrt{3}$  [see Almeida et al. (2007) for an explanation of the pre-factor]. The full details of the calculation of  $V_{\text{circ,bulge}}$  are given in Cole et al. (2000). We obtain a reasonable match to the data, reproducing the tightness of the relationship, except at the largest velocity dispersions. For less massive BHs, our model gives  $M_{\text{BH}} \propto \sigma_{\text{bulge}}^4$ , which compares well with the Tremaine et al. (2002) estimate of the slope of  $4.02 \pm 0.32$ . However, for BHs more massive than  $M_{\text{BH}} = 10^{7.5} h^{-1} M_{\odot}$ , the slope is shallower than observed, closer to  $M_{\text{BH}} \propto \sigma_{\text{bulge}}^3$ . Direct accretion of cooling gas from a hot reservoir may help to bring the slope of the  $M_{\text{BH}}-\sigma_{\text{bulge}}$  relation closer to that observed (Bower et al. 2006).

The slope of the  $M_{\text{BH}}-\sigma_{\text{bulge}}$  relation should perhaps be regarded as one of the less robust predictions of the model, because of the complexity of calculating  $\sigma_{\text{bulge}}$ . This quantity depends upon the accuracy of the calculation of the radius of the spheroid. Cole et al. (2000) introduced a prescription for computing the size of merger remnants, by applying the virial theorem and the conservation of energy to the progenitor galaxies and the remnant. The resulting size

of the spheroid is adjusted to take into account the self-gravity of the disc and bulge and the reaction of the dark matter to the presence of condensed baryons. This step is carried out using an adiabatic contraction model. The assumptions behind this approach are likely to become less valid as the mass of the spheroid increases in relation to the mass of the halo. Almeida et al. (2007) tested this prescription against the properties of spheroids in the Sloan Digital Sky Survey (SDSS). Whilst the agreement between the observed and predicted Faber–Jackson relation (velocity dispersion–luminosity) is encouraging, the predicted slope is somewhat steeper than is observed and the brightest galaxies in the model will perhaps have too large a velocity dispersion.

The level of agreement with observations that we find between different bulge properties and BH mass is encouraging and suggests that, overall, our model of galaxy and BH formation is on a firm footing.

### 3.2 Predictions for the luminosity function of quasars

In order to establish further the credentials of our model, we present some illustrative predictions for the evolution of the quasar luminosity function. Further assumptions and model parameters are required to assign a luminosity to the quasar phase which occurs when the BH accretes gas during a galaxy merger. In this section, we give a brief outline of our model for calculating the luminosity of the quasar and present some results for the quasar luminosity function at different redshifts. These predictions are included here for completeness and to allow comparison with previous work (e.g. Kauffmann & Haehnelt 2000). We will explore the form and evolution of the quasar luminosity function in more detail in a future paper.

There are two basic parameters in our model for quasar luminosity: the lifetime of the quasar,  $t_Q$ , and the fraction of the accreted mass energy that is turned into the bolometric luminosity of the quasar,  $\epsilon_Q$ . We assume that the gas available for accretion on to the BH in a galaxy merger is accreted at a constant rate,  $\dot{M}(t)$ , over the quasar lifetime:

$$\dot{M}(t) = \frac{\Delta M_{\text{BH}}}{t_Q} \quad \text{for } t < t_Q. \quad (5)$$

(Recall that  $\Delta M_{\text{BH}}$  is defined by equation 1.) We note in passing that if we had instead assumed an exponentially decaying mass accretion rate, with a time-scale given by  $t_Q = 0.5t_{\text{bulge}}$ , giving a mass accretion rate of  $\{\text{i.e. } \dot{M}(t) = \Delta M \exp[-t/(0.5t_{\text{bulge}})]\}$ , this would lead to very similar results to those we obtain for a constant mass accretion rate.

The quasar lifetime,  $t_Q$ , is assumed to be directly proportional to the dynamical time of the bulge,  $t_{\text{bulge}}$ . In the simplest case, without imposing any further conditions on the luminosity of the quasar, this assumption results in a top-hat light curve:

$$L_Q(t) = \epsilon_Q \dot{M}(t) c^2 \quad \text{for } t < t_Q. \quad (6)$$

When computing the luminosity of quasars, the Eddington limit may play an important role. A quasar is said to be radiating at its Eddington limit when the pressure of the radiation emitted following accretion on to the BH balances the gravitational force exerted by the BH on new material that is being accreted. The Eddington limit depends upon the mass of the BH. Physical mechanisms have been proposed which permit mass to be accreted at rates which exceed the Eddington limit (see e.g. Begelman 1978). Here, we show the impact of the Eddington limit on the luminosity of quasars. We consider four different cases.

Case 1: No Eddington limit is applied to the bolometric luminosity of the quasar.

Case 2: The bolometric luminosity is limited by the Eddington luminosity corresponding to the BH mass at the *end* of the accretion episode:

$$L_Q(t) = \max(\epsilon_Q \dot{M}(t) c^2, L_{\text{Edd}}(M_{\text{final}})). \quad (7)$$

Case 3: The bolometric luminosity is limited by the Eddington luminosity corresponding to the BH mass at the *start* of the accretion episode:

$$L_Q(t) = \max(\epsilon_Q \dot{M}(t) c^2, L_{\text{Edd}}(M_{\text{start}})). \quad (8)$$

Case 4: The bolometric luminosity is limited by the Eddington luminosity corresponding to the BH mass calculated *during* the accretion episode:

$$L_Q(t) = \max(\epsilon_Q \dot{M}(t) c^2, L_{\text{Edd}}(M(t))). \quad (9)$$

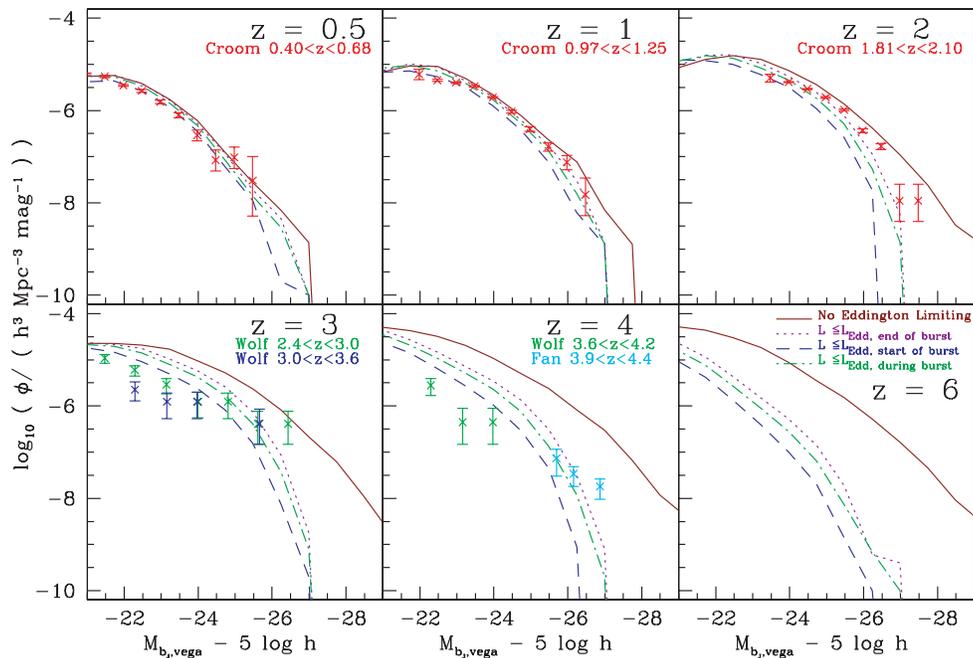
Case 4 is the most realistic estimate of the luminosity after applying Eddington limiting. However, there is some uncertainty in the evolution of the Eddington limit *during* the burst, as we do not know in detail how the mass of the BH changes from its initial value to the final value. Case 2 corresponds to the maximum possible Eddington limit during the accretion episode, being set by the final BH mass. Case 3 is the minimum possible Eddington limit during the accretion episode, corresponding to the initial BH mass. We find little variation in the quasar luminosity function between these three cases, suggesting that the precise growth of the BH over the accretion episode is unimportant.

We assume that all visible quasars have identical, flat spectra over the range of wavelengths of interest, and that a fraction,  $f_{b_j}$ , of the bolometric luminosity is emitted in the  $B$  and  $b_j$  bands. We adopt  $f_{b_j} = 1/15$ , which agrees well with Elvis et al. (1994). Taking into account the  $b_j$ -band filter profile, we can calculate a magnitude for a quasar from its bolometric luminosity:

$$M_{b_j, \text{vega}} = 13.2 - 2.5 \log_{10} (f_{b_j} L_{\text{bol}} / 10^{40} \text{ erg s}^{-1}). \quad (10)$$

Finally, we assume that only a fraction  $f_{\text{visible}}$  of quasars are detected in optical surveys; the remainder are obscured in the optical. We first set  $f_{\text{visible}} = 0.25$ , i.e. only a quarter of quasars are visible in optical surveys. This is roughly in line with the results of X-ray surveys, which typically find that 20–30 per cent of quasars are unobscured in soft X-rays (and we presume that this is the same fraction visible in the optical visible in optical) (Ueda et al. 2003; La Franca et al. 2005; Shinozaki et al. 2003; Gilli, Comastri & Hasinger 2007), although this fraction is still somewhat uncertain, and furthermore is likely to vary with intrinsic quasar luminosity. We then set the parameters  $t_Q$  and  $\epsilon_Q$  in order to produce a reasonable match to the Croom et al. (2004) measurement of the  $b_j$ -band luminosity function over the redshift interval  $0.5 \leq z \leq 2$ , as shown in Fig. 3. At higher redshifts, we show a comparison between our predicted luminosity functions and the 1450-Å rest-frame quasar luminosity functions from the SDSS survey (Fan et al. 2001) and the COMBO-17 survey (Wolf et al. 2003), using the corrections given in the respective papers to convert to the  $B$  band, and applying a further minor correction to the  $b_j$  band.

To achieve the best fit, we require that the quasar lifetime,  $t_Q$ , be related to the bulge dynamical time,  $t_{\text{bulge}}$ , by  $t_Q = 1.5t_{\text{bulge}}$  and that the fraction of accreted mass energy produced as bolometric luminosity be  $\epsilon_Q = 0.06$ . A typical bulge has a dynamical time of  $t_{\text{bulge}}$  of  $2 \times 10^7$  yr at  $z = 1$ ,  $8 \times 10^6$  yr at  $z = 3$  and  $2.5 \times 10^6$  yr at  $z = 6$ , although within each redshift bin, the distribution in  $t_{\text{bulge}}$  is very broad. As noted by Kauffmann & Haehnelt (2000), this



**Figure 3.** The quasar luminosity function at selected redshifts, as indicated in each panel. The model predictions are shown by lines and the data by symbols, with the source indicated in each panel. The different line styles correspond to different assumptions for how the quasar luminosity depends upon the Eddington luminosity of the BH, as indicated by the legend in the bottom right-hand panel. The data are taken from the following papers: Croom = Croom et al. (2004); Fan = Fan et al. (2001); Wolf = Wolf et al. (2003).

redshift evolution in  $t_{\text{bulge}}$  helps to reproduce the evolution in the quasar luminosity function. Our time-scales agree fairly well with the Martini & Weinberg (2001) estimate of  $t_Q = 4 \times 10^7$  yr at  $z = 2$ , which is a typical value. We also note that our adopted radiative efficiency of 0.06 is consistent with standard disc accretion, which is likely to be required for optically bright emission.

Our simple model does a reasonable job of reproducing the observed quasar luminosity function at  $z \leq 2$ , but overpredicts the luminosity function at higher redshifts. Our basic prediction for the quasar luminosity function (shown by the solid lines in Fig. 3) shows strong evolution with redshift which cannot be described as pure luminosity evolution. If the Eddington limit is taken into account, then the form of the model predictions changes, particularly at bright luminosities, where the abundance of objects is strongly suppressed, with the result that the predictions match the data better. The suppression affects more objects at higher redshifts – the gas supply then is greater for any given mass of BH, and the dynamical time-scales are shorter, leading to higher rates of supply for any given mass of available gas. The predicted luminosity functions are relatively insensitive to the precise details of how the Eddington limit is allowed to influence the quasar luminosity.

#### 4 THE GROWTH OF BLACK HOLES THROUGH ACCRETION AND MERGERS

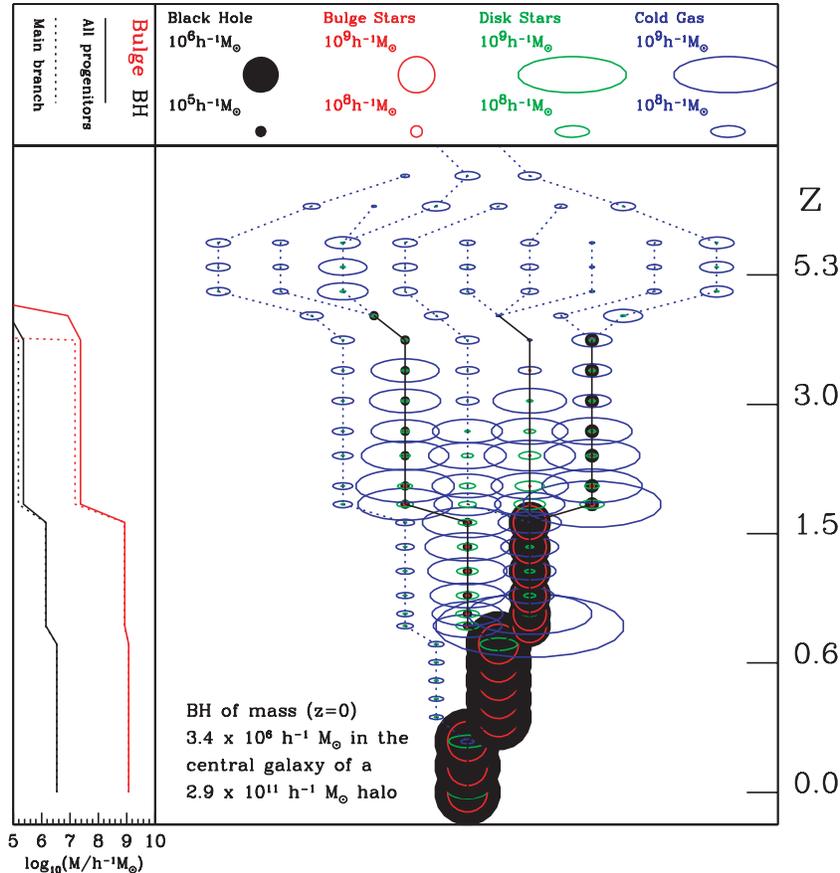
We present the bulk of our results in this section. The section is quite long, so we list the contents here to help the reader navigate through the various topics. First, in Section 4.1, we give illustrative examples of how BHs acquire mass, tracing the mass assembly history of two BHs. We then explore the demographics of the BH population: in Section 4.2, we present the predictions for the evolution of the mass function of BHs and in Section 4.3 we investigate how the BHs are distributed between dark haloes of different mass.

The next few sections deal with how BHs build up their mass. In Section 4.4, we show the distribution of progenitor masses of BHs, and, in Section 4.5, we address the issue of whether the accretion of gas or mergers is the main mechanism for accumulating BH mass. We present results for the formation redshift of BHs in Section 4.6 and for their merger rates in Section 4.7. Finally, in Section 4.8, we compare the amount of baryons locked up in BHs with other phases, such as cold gas and stars.

##### 4.1 Illustrations of black hole growth

Before concentrating on statistical descriptions, it is instructive to show some illustrations of how individual BHs grow in our simulations. These examples serve to provide a qualitative picture of the model, and to make clear certain definitions and results on BH formation histories that will be of use later on. Note that, although space limitations restrict us to only two examples, there is, in fact, a rich diversity in BH formation histories in the model.

The mass assembly history of two BHs is shown in Figs 4 and 5. Fig. 4 shows the central galaxy in a halo of mass  $2.9 \times 10^{11} h^{-1} M_\odot$  and Fig. 5 shows the central galaxy in a halo of mass  $8.2 \times 10^{11} h^{-1} M_\odot$ . The main part of each panel follows the mass assembly tree. Various components are plotted, as indicated by the key at the top of each plot: BH mass, bulge stars, disc stars and cold gas. The area of the symbols is proportional to the mass in a given component, with reference areas/masses provided at the top of each plot. Galaxies containing BHs are linked by solid lines, while galaxies not containing BHs are linked to their descendants with dotted lines. The redshifts plotted are the output redshifts of the simulation. The left–right positioning in the plot is schematic, and has no relevance to spatial positions of galaxies within the dark matter halo; the ‘main branch’ (i.e. the most massive progenitor at each merger) is always the rightmost branch of the merger tree.



**Figure 4.** A mass assembly tree of a BH and its host galaxy. Progenitor galaxies without BHs are connected by dotted lines. The trees show the relative amounts of cold gas, disc stars, bulge stars and BH mass, as indicated by the key. The area of the symbols is proportional to mass. The left-hand side panel shows the assembly of BH mass and bulge stars, adding all progenitors (solid line) and tracing back the main branch, which is usually the most massive progenitor (dotted line). The left–right positioning in the plot is purely schematic and has no relevance to the spatial positions of galaxies. The final galaxy is the central galaxy of a halo of mass  $2.9 \times 10^{11} h^{-1} M_{\odot}$ .

In some cases, the BH in the ‘main branch’, which we denote the ‘main progenitor’, may not actually be *the* most massive of *all* the progenitor BHs at a given epoch, particularly at higher redshifts. We have chosen to avoid jumping from one branch of the BH merger tree to another when following the ‘main progenitor’ backwards in time. Instead, we start from the present-day BH, find its most massive progenitor, and then build up a continuous branch by tracking the most massive progenitor at each of  $\sim 25$ – $30$  output redshifts.

In the side panel of each figure, we plot the cumulative masses of the BH and bulge stars as a function of time. The solid line shows the total mass in these components, adding together all of the progenitors. The dotted line shows the mass in the branch tracing back the most massive progenitor of the present-day BH (the ‘main branch’).

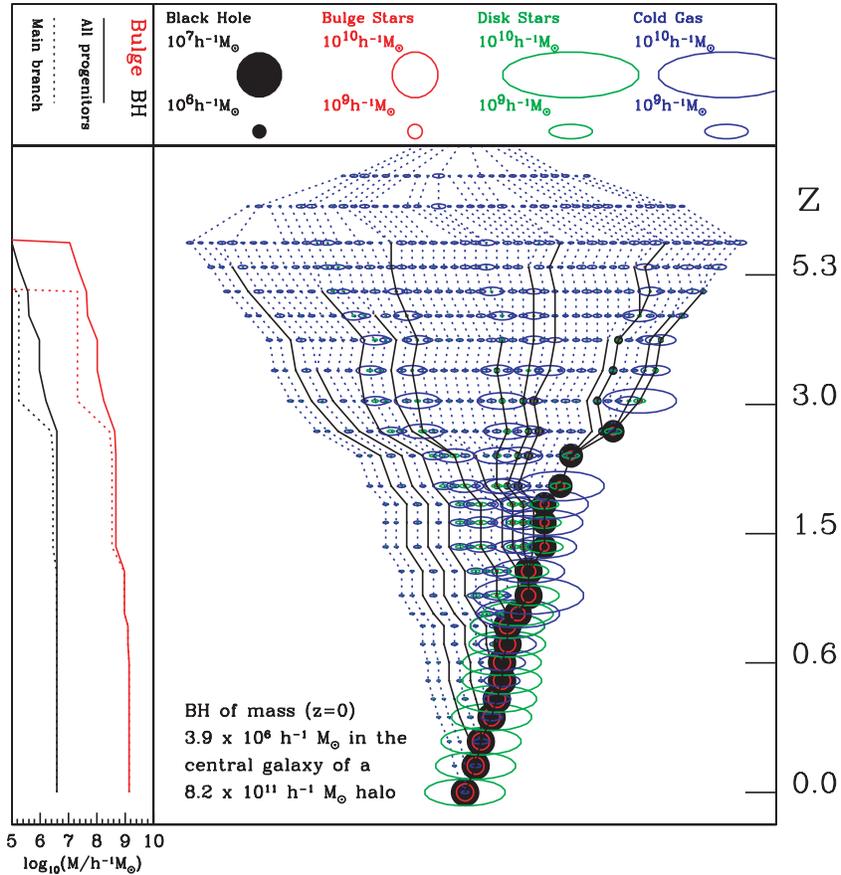
In general, we find a very wide variety of BH formation histories, and we have chosen the ones we plotted to be illustrative. The formation trees of the most massive BHs tend to be too large and complicated to plot effectively. Meanwhile, there is a high abundance of BH trees with just one burst in their history, which were not very interesting to plot. All merger trees are included, however, in the quantitative results we present later.

Inspection of the mass assembly trees, particularly the one for the more massive galaxy, reveals that there can be many branches to the BH merger trees at high redshifts. However, most of the BH mass is contained in one or two main branches, as shown by

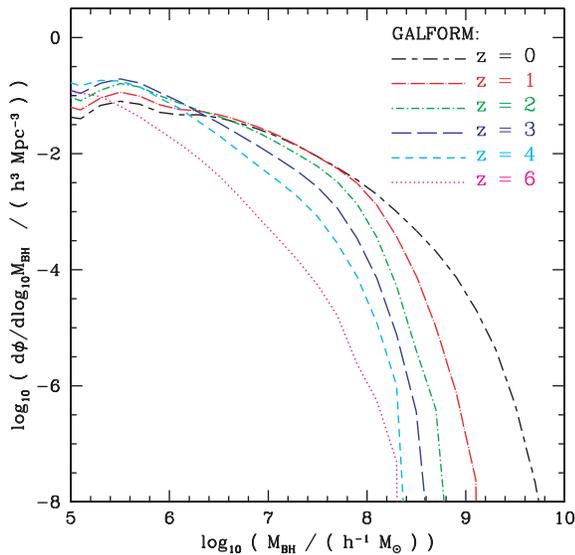
the closeness of the solid and dotted lines in the side panels. In the Baugh et al. (2005) model, the quiescent star formation time-scale is independent of the dynamical time. This results in discs which are gas-rich at early epochs (blue circles), with significant quantities of stars only forming at relatively recent epochs (green circles). At later times, it is also apparent that the ratio of the stellar mass of the bulge to the mass of the BH is increasing. We will present predictions for the evolution of the  $M_{\text{BH}}-M_{\text{bulge}}$  relations in a later section.

#### 4.2 Black hole mass function

The BH mass function at various redshifts is shown in Fig. 6. The high-mass end advances to higher masses at lower redshifts. This is unsurprising in a hierarchical galaxy formation model, and reflects the corresponding evolution of the dark matter halo mass function. The predicted evolution in the BH mass function is quite strong. This is in contrast with observational claims that the abundance of large BHs does not vary with redshift (e.g. McLure & Dunlop 2004). Such studies, however, typically include only optically selected quasars, and so can only probe accreting BHs. We examine the relationship of accreting BHs to the general BH population in a later section on downsizing (Section 6) and consider the implications of the rare, massive BHs at high redshift inferred from the observations of Fan et al. (2001) in the discussion (Section 7).



**Figure 5.** A mass assembly tree of a BH and its host. The final galaxy is the central galaxy of a halo of mass  $8.2 \times 10^{11} h^{-1} M_{\odot}$ .



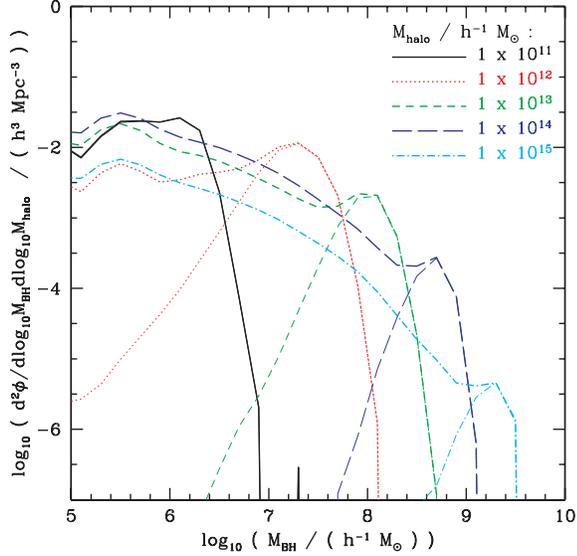
**Figure 6.** The evolution of the BH mass function with redshift, as indicated by the key.

At redshift zero, the break in the BH mass function occurs around  $10^8 h^{-1} M_{\odot}$ . This corresponds to the scale at which there is a transition between accretion-dominated growth and merger-dominated growth (as we demonstrate specifically in Section 4.5). In larger galaxies hosting more massive BHs, the cold gas has been sub-

stantially depleted, so the BH mass can only increase significantly through mergers. Gas depletion and suppression of further cooling by feedback processes is also the likely mechanism by which a break in the luminosity function of galaxies is produced (Benson et al. 2003b; Bower et al. 2006; Croton et al. 2006).

From the observed  $M_{\text{BH}}-M_{K,\text{bulge}}$  relation,  $M_{\text{BH}} = 10^8 h^{-1} M_{\odot}$  corresponds to  $M_{K,\text{vega}(\text{bulge})} - 5 \log_{10} h \sim -23.5$ . This is very close to the break in the  $K$ -band luminosity function,  $M_K^* - 5 \log_{10} h = -23.44 \pm 0.03$  (Cole et al. 2001). Similarly, from the observed  $M_{\text{BH}}-M_{\text{bulge}}$  relation,  $M_{\text{BH}} = 10^8 h^{-1} M_{\odot}$  corresponds to  $M_{\text{bulge}} \sim 3 \times 10^{10} M_{\odot}$ . This is the stellar mass at which Kauffmann et al. (2003) find a transition in galaxy properties. Although BH mass is related to bulge properties only, the identification of the knee in the BH mass function with a transition in the global properties of galaxies is reasonable since galaxies brighter and more massive than the transition mass tend to be bulge dominated. The conclusion is that galaxies (particularly galactic bulges) and BHs grow together (as demonstrated graphically in the side panels of Figs 4 and 5).

As time advances, the BH mass function becomes progressively flatter at the low-mass end. To a large extent, this is a generic feature of a hierarchical mass assembly model in which small objects merge into larger objects (at least when this effect is not exceeded by the production of new low-mass objects). A further contribution to the change in slope comes from less massive BHs accreting larger amounts of gas as a fraction of their mass than larger ones (i.e. downsizing, Section 6). The combination of these effects is greater than the effect of the formation of new, lower mass BHs; most BHs are seeded at high redshift, as discussed in Section 4.6.



**Figure 7.** The contribution to the BH mass function from BHs in dark matter haloes of various masses, as indicated by the key. We show the case for BHs contained within any galaxy (thick lines) and in central galaxies only (thin lines). The BH mass function for each halo mass is normalized to be the mass function per dex in dark matter halo mass.

### 4.3 Black hole demography: the conditional mass function

BHs of a given mass form in haloes with a broad range of masses. The contribution to the BH mass function from different ranges of dark matter halo mass are shown in Fig. 7. At the high-mass end of each of these conditional mass functions, there is a peak and a cut-off. The peak corresponds to the mass of the BH in the central galaxy, which increases as the mass of the central galaxy bulge which is strongly correlated with the mass of its host halo. This phenomenon is not restricted to BHs. Eke et al. (2004) find tentative evidence for a similar bump in the galaxy luminosity function of groups and clusters which they attribute to central galaxies, although this remains controversial (Yang et al. 2005).

In galaxy formation models, a bump is sometimes present in luminosity functions where only galaxies in a limited range of halo

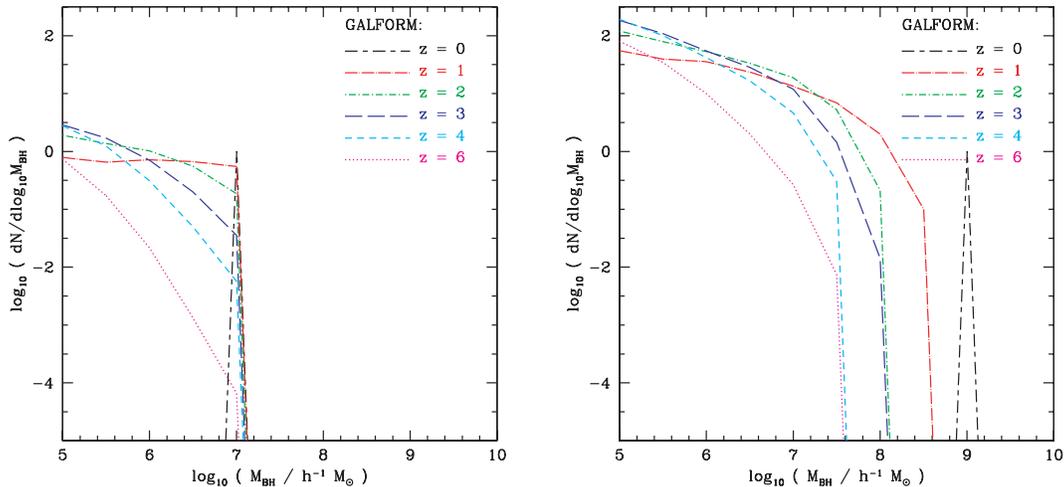
masses are selected – this is because of the contribution of central galaxies (Benson et al. 2003a). This reflects the different physical processes relevant to central and satellite galaxies: in the model, satellite–satellite mergers are not allowed, while all cooling gas is funnelled into the central galaxies. These simple assumptions, common in semi-analytic models, have been validated in gas-dynamic simulations (Zheng et al. 2004). Models with intense star formation in bursts, such as the Baugh et al. (2005) model used here, smear out the bumps somewhat (Eke et al. 2004), since the bursts introduce additional scatter in the properties of galaxies that form in haloes of a given mass.

### 4.4 Mass function of progenitor black holes

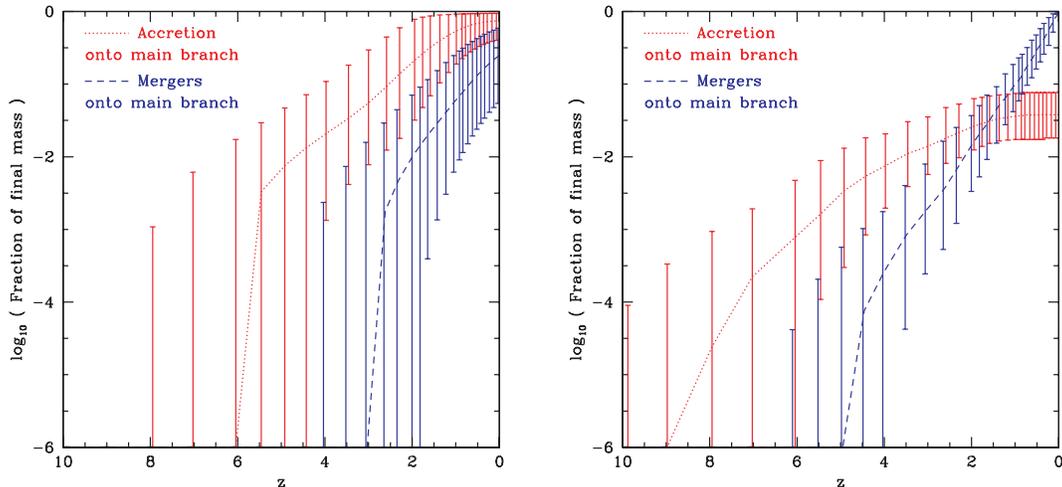
We now consider the distribution of the masses of BH progenitors at different epochs for present-day BHs. Fig. 8 shows the distribution of progenitor masses at different redshifts, for two ranges of BH mass measured at  $z = 0$ . The left-hand panel shows the progenitors of  $z = 0$  BHs with masses in the range  $10^7 - 10^{7.5} h^{-1} M_\odot$  and the right-hand panel shows the progenitors of  $z = 0$  BHs with masses in the range  $10^9 - 10^{9.5} h^{-1} M_\odot$ . The different line types in the plot show the progenitor mass distributions at different redshifts, as indicated by the key. The distributions plotted are averaged over large numbers of BHs with the appropriate present-day mass. In both panels, the  $z = 0$  distribution is naturally peaked around the present-day mass of the BH.

The evolution of these progenitor mass functions from  $z = 6$  to 1 looks remarkably similar to that of the universal BH mass function, albeit truncated at the final  $z = 0$  BH mass, and with an overall normalization which increases with increasing final BH mass.

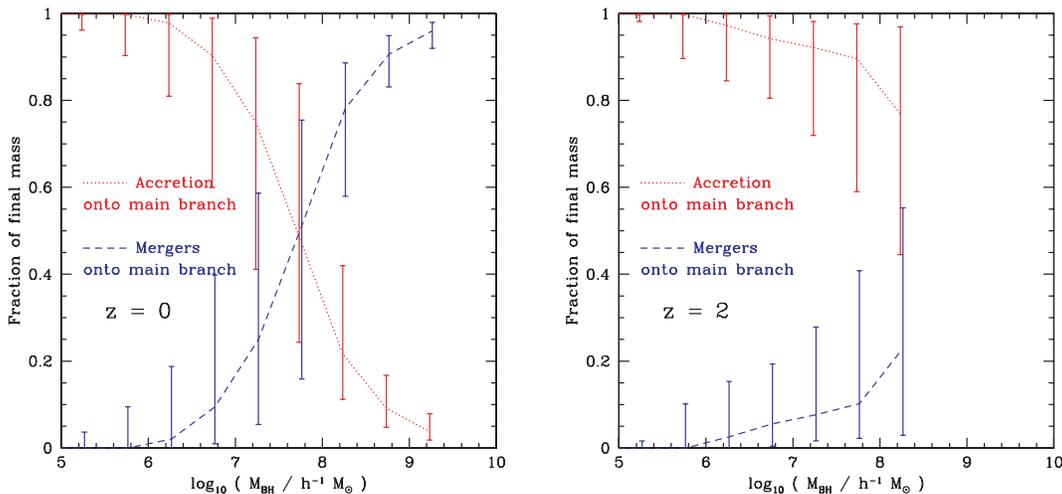
The similarity of the form and evolution of the progenitor mass functions with those of the universal mass function is remarkable. Only at the lowest progenitor redshift plotted ( $z = 1$ ) for BHs with present-day masses in the range  $10^7 - 10^{7.5} h^{-1} M_\odot$  do we see a significant deviation from the form of the overall mass function. The progenitor mass function in this case is rather flat, with fewer low-mass BHs and more high-mass BHs close in mass to the final BH. The amplitude of the progenitor mass functions is substantially larger for the BHs with present-day mass of  $10^9 - 10^{9.5} h^{-1} M_\odot$ : larger BHs have a significantly larger number of progenitor BHs. This fits in well with our later result (Section 4.5) that less mas-



**Figure 8.** The mass functions of progenitor BHs for present-day BHs with mass in the interval  $10^7 - 10^{7.5} h^{-1} M_\odot$  (left-hand panel) and  $10^9 - 10^{9.5} h^{-1} M_\odot$  (right-hand panel). The distribution of progenitor masses is plotted at different redshifts, as indicated by the key. The mass functions are generated by considering a large sample of BHs at  $z = 0$ , and the normalization is chosen so that each progenitor mass function is the mass function *per BH* at  $z = 0$ .



**Figure 9.** The cumulative growth with redshift of the BH mass in the ‘main branch’ divided into the contribution from mergers and accretion. We consider large samples of BHs with  $z = 0$  masses in the range  $10^7$ – $10^{7.5} h^{-1} M_{\odot}$  (left-hand panel) and  $10^9$ – $10^{9.5} h^{-1} M_{\odot}$  (right-hand panel). The dotted and dashed lines connect the medians of the distribution, while the 10–90 percentiles of the distribution are shown as error bars.



**Figure 10.** The cumulative fraction of the mass assembled by mergers and accretion, as a function of final BH mass at  $z = 0$  (left-hand panel) and  $z = 2$  (right-hand panel). The medians are connected by lines, and the 10–90 percentile spread of the distribution is shown as an error bar for each BH mass.

sive BHs grow primarily by accretion on to a single main branch, whereas BHs larger than  $5 \times 10^7 h^{-1} M_{\odot}$  grow primarily by mergers of pre-existing BHs.

#### 4.5 Black hole growth by mergers and accretion

We come now to one of the principal results of our paper, the manner in which BHs acquire their mass. There are two distinct modes of mass assembly in our model: ‘accretion’, in which cold gas is turned into BH mass during a starburst, and ‘mergers’, in which existing BHs merge to build a more massive BH. In the accretion mode, mass is being turned into BH mass for the first time, whereas in the merger mode, pre-existing BH mass is being rearranged or re-assembled into a more massive BH. In Fig. 9, we plot the fraction of the mass in the ‘main branch’ which is assembled by mergers or gas accretion as a function of redshift. We show results for BHs in two mass ranges at redshift zero:  $10^7$ – $10^{7.5} h^{-1} M_{\odot}$  (left-hand panel) and  $10^9$ – $10^{9.5} h^{-1} M_{\odot}$  (right-hand panel). Fig. 9 shows that at high redshifts, growth by accretion dominates over growth through mergers. Mergers become increasingly important as redshift decreases, but

for the  $10^7$ – $10^{7.5} h^{-1} M_{\odot}$  BHs, the cumulative growth by mergers never exceeds the cumulative growth by accretion, even at redshift zero. However, for BHs of mass  $10^9$ – $10^{9.5} h^{-1} M_{\odot}$  at  $z = 0$ , the cumulative growth of their main progenitors by mergers exceeds that by accretion around a redshift of 1.7, and growth by accretion almost halts after this.<sup>1</sup> By redshift zero, the cumulative mass assembled by mergers greatly exceeds that assembled by accretion. The declining importance of growth by accretion for BHs of mass  $>10^{7.5} h^{-1} M_{\odot}$  reflects the decline in the amount of gas available in mergers as more and more of the gas in collapsed haloes is consumed into stars.

In Fig. 10, we plot the fraction of the mass of BHs which, by  $z = 0$  (left-hand panel) and  $z = 2$  (right-hand panel), has been accumulated by mergers or accretion on to the ‘main branch’. This is shown as a function of BH mass. Fig. 10 (left-hand panel) shows that, by redshift zero, low-mass BHs have accumulated nearly all of their mass by direct accretion on to a single ‘main branch’, while the most massive

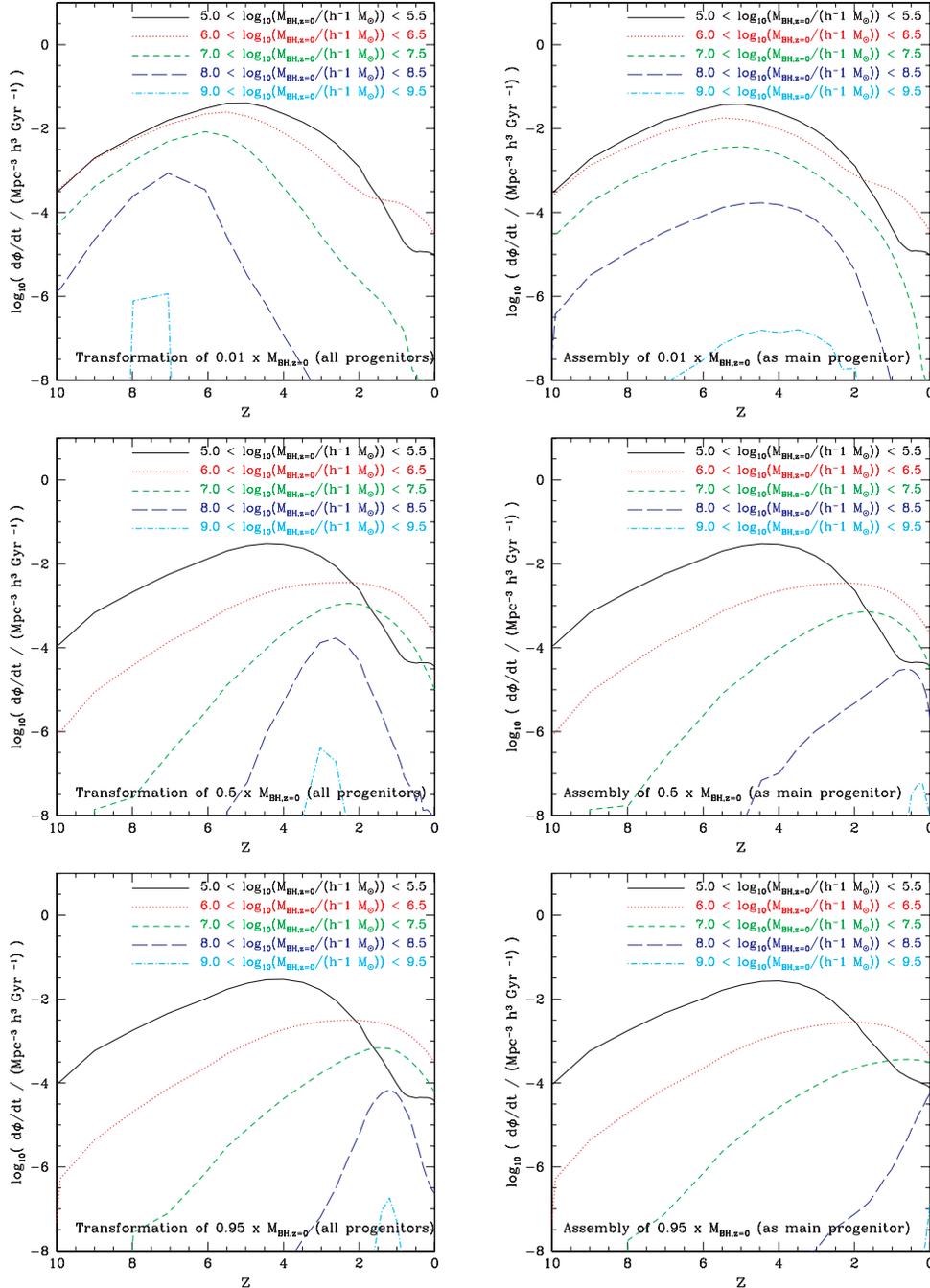
<sup>1</sup> This redshift can vary from BH to BH –  $z = 1.7$  is the redshift where the median growth by mergers exceeds the median growth by accretion.

BHs accumulate 80–90 per cent of their mass by mergers of less massive BHs on to the ‘main branch’. The transition from accretion-dominated growth to merger-dominated growth occurs at a  $z = 0$  mass of just over  $10^8 h^{-1} M_{\odot}$ . Fig. 10 (right-hand panel) shows that at  $z = 2$ , all BHs, even those more massive than  $10^8 h^{-1} M_{\odot}$ , grow predominantly by accretion, although there is a contribution from mergers which increases with BH mass. Comparison of the results in Fig. 10 for  $z = 0$  and 2 shows that for any given BH mass, growth by accretion is more significant for a BH at  $z = 2$  than at  $z = 0$ , and that this difference is greater for the more massive BHs. This is consistent with the idea that the luminous growth (i.e. growth by

direct accretion of gas) of higher mass BHs switches off towards lower redshifts (see Section 6).

#### 4.6 The redshift of black hole formation

In Fig. 11 we show the formation redshifts of BHs, binned by  $z = 0$  mass. Each of the six panels corresponds to a different definition of formation redshift. ‘Formation’ is defined as the time when either the main progenitor (right-hand panels) or the sum of all existing progenitor BHs (left-hand panels) first exceeds a given fraction of the final BH mass. Where the formation redshift is defined as the



**Figure 11.** The distribution of formation redshifts of BHs in five different bins of  $z = 0$  mass, as indicated by the key. The differing definitions of formation redshift used in each of the six plots are noted briefly on each plot and explained more fully in Section 4.6 of the text.

time when the *main progenitor* first exceeds a given fraction of the final mass, we refer to this as the *mass assembly* redshift, since this is the redshift where the stated fraction of the mass has been assembled into a single object. Where the formation redshift is defined as the time when the *sum of all progenitors* first exceeds a given fraction of the final mass, we refer to this as the *mass transformation* redshift. This distinction between the *mass transformation* time and *mass assembly* time for BHs is analogous to that between the star formation time and stellar mass assembly time for the stars in a galaxy. We consider three different mass fraction thresholds to define formation times: 0.01 (top), 0.5 (middle) and 0.95 (bottom).

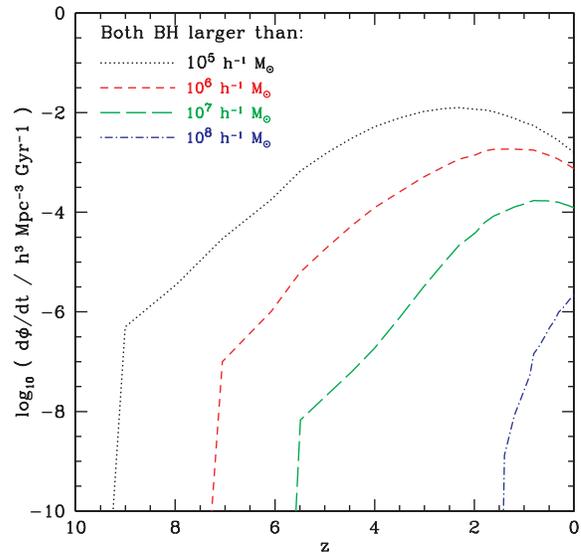
When we consider the assembly of 50 or 95 per cent of the final BH mass (Fig. 11, middle and bottom right-hand panels), we see clear hierarchical behaviour; the more massive BHs at redshift zero peak in their formation times at lower redshift than the less massive ones. This is evidence for the hierarchical *assembly* of BH mass into a single final object. However, when we consider the redshift at which 50 per cent of the final BH mass has *accreted* on to *any* BH in the merger tree (Fig. 11, middle left-hand panel), we see the opposite trend; in the mass range  $M_{\text{BH}} = 10^7 - 10^{9.5} h^{-1} M_{\odot}$ , the more massive BHs display a distribution of formation redshifts which peaks at higher redshift. When we consider the redshift at which 95 per cent of the final BH mass is *accreted* on to *any* BH in the merger tree (Fig. 11, bottom left-hand panel), we see further evidence of downsizing. Although the formation rate peaks at a similar redshift ( $z \sim 1.2$ ) for all BHs in the mass range  $M_{\text{BH}} = 10^7 - 10^{9.5} h^{-1} M_{\odot}$ , the decline in the fraction forming per unit time as redshift approaches zero is far steeper for more massive BHs within this mass range. The observational evidence for ‘downsizing’ refers to the accretion of mass on to a particular progenitor, which is accompanied by the release of energy. Hence, it is the latter trend which is relevant – as BH mass increases, the redshift when mass is *accreted* on to *any* progenitor increases. We return to this point in Section 6.

We consider now the early growth of the BHs. Fig. 11 (top left-hand panel) shows the redshift when the first 1 per cent of the final BH mass has collapsed into any of the branches of the merger tree. There is a clear trend for larger BHs to be seeded earlier. This is also a form of downsizing. All of the BHs in our largest mass bin ( $M_{\text{BH}} = 10^9 - 10^{9.5} h^{-1} M_{\odot}$ ) and many of those in the next mass bin,  $M_{\text{BH}} = 10^8 - 10^{8.5} h^{-1} M_{\odot}$ , are seeded before reionization occurs in the model at  $z = 6$ . Another interesting feature of Fig. 11 is that, for almost any definition of formation time, less massive BHs have a much wider spread in formation times than more massive BHs.

There is little difference in the distribution of formation times of BHs of mass  $M_{\text{BH}} = 10^5 - 10^{6.5} h^{-1} M_{\odot}$  regardless of whether we use a definition which relates to the ‘main branch’ or to ‘all progenitors’. This follows from our earlier result that BHs in this mass range formed almost exclusively by accretion on to a single object, with little contribution from mergers between BHs (Section 4.5, Fig. 10). The differentiation between the different definitions of formation time begins to become apparent for BHs of mass  $M_{\text{BH}} = 10^7 - 10^{7.5} h^{-1} M_{\odot}$  and is increasingly more significant as BH mass increases further. This relates to our earlier result that the contribution to the final BH mass from mergers of pre-formed BHs compared to the contribution from direct cold gas accretion on to the main branch increases strongly with increasing BH mass (Section 4.5, Fig. 10).

#### 4.7 Black hole merger rates

We show the merger rate per unit time of BHs as a function of redshift in Fig. 12. We show this for a number of mass thresholds



**Figure 12.** BH merger rate per unit time as a function of redshift. The merger rate is plotted for 5 different mass thresholds, as shown by the key, which the (pre-starburst) masses of both BHs must exceed.

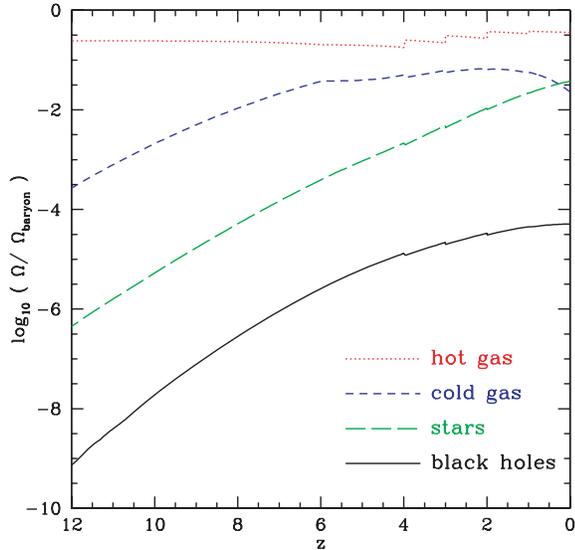
which must be exceeded by both of the BHs that take place in the merger. The merger rates peak at lower redshift for more massive BHs, with the merger rate for the most massive bin still rising at  $z = 0$ . This is consistent with the trend seen at  $z = 0$  that larger mass BHs grow primarily by mergers, while less massive BHs grow primarily by accretion (Section 4.5).

This behaviour in the growth and merging of BHs of varying mass is largely a reflection of the general hierarchical growth of structure, moderated in the case of galaxies and BHs by baryonic processes. The results presented in this subsection concern only mergers of BHs, not necessarily their total growth which can also involve accretion. There is no evidence for ‘antihierarchical’ behaviour in the evolution of BH mergers. However, as we show in Section 6, this is perfectly compatible with quasar downsizing – BH merging can be a ‘dark’ process in which no gas is present, whereas the observational evidence for downsizing refers to processes involving star formation or gas accretion.

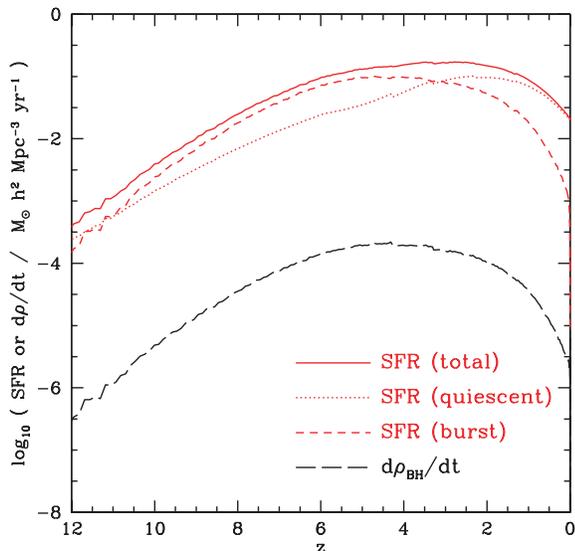
#### 4.8 The fraction of baryons in black holes

Having considered the formation of individual BHs, we now look at the global picture. In Fig. 13, we show the integrated cosmic density of all the baryonic components of the universe; hot gas, cold disc gas, stars and BHs. After  $z \sim 4$ , the growth of BH mass in the universe slows down in comparison to that of stars, as quiescent star formation begins to dominate over star formation in bursts. The decline in cold gas from redshift 2 to 0 goes a small way towards explaining the decline in quasar activity over this redshift interval. The decline in the galaxy merger rate and the transition from burst-dominated star formation to quiescent star formation also play a role. In Fig. 14, we show the SFR, divided into burst and quiescent modes, and the rate of BH growth. By construction in our model, BH growth is more strongly correlated with the SFR in bursts than with star formation in general. Very broadly, although perhaps less so at low redshifts, BH accretion tracks the overall star formation over cosmic time, as observed (Boyle & Terlevich 1998).

The cosmological mass density of BHs at  $z = 0$  is a quantity of interest. In our model, we find that  $\rho_{\text{BH}} = 2.83 \times 10^5 M_{\odot} \text{Mpc}^{-3}$ .



**Figure 13.** The evolution of the fraction of the baryons in the universe in hot gas, cold gas, stars (disc plus bulge) and BHs. The small abrupt changes in some of the lines are due to simulation runs that finish at different times.



**Figure 14.** The variation with redshift of the global SFR (starbursts, quiescent and total) and the global rate of BH growth.

Observationally,  $\rho_{\text{BH}}$  is determined by integrating the BH mass function which, in turn, is inferred from a combination of the velocity dispersion distribution of galaxies, the  $K$ -band luminosity function or the bulge stellar mass function, and the appropriate  $M_{\text{BH}}-M_{\text{bulge}}$  relation. Observed values of  $\rho_{\text{BH}}/(10^5 M_{\odot} \text{Mpc}^{-3})$ , converted to  $H_0 = 70 \text{ km s}^{-1} \text{Mpc}^{-1}$ , are:  $2.9 \pm 0.5$  (Yu & Tremaine 2002),  $2.4 \pm 0.8$  (Aller & Richstone 2002),  $2.8 \pm 0.4$  (McLure & Dunlop 2004),  $4.2 \pm 1.1$  (Shankar et al. 2004) and  $4.6_{-1.4}^{+1.9}$  (Marconi et al. 2004). Our estimate is towards the lower end of the broad range spanned by the observational estimates. We do not include any measurement errors in our estimate. A detailed comparison would need to take into account galaxy type (some estimates are based only on ellipticals), the flux limits of the observational samples and the treatment of the dispersion in the  $M_{\text{BH}}-M_{\text{bulge}}$  relations when converting from bulge properties to BH masses. Many observational estimates

assume that the scatter in  $\log(M_{\text{BH}})$ , at a given value of the bulge property under consideration, is symmetrical. This assumption then leads to larger values of  $\rho_{\text{BH}}$  for larger assumed values of the scatter (McLure & Dunlop 2004). However, it is not at all clear that the scatter in these relations is symmetrical.

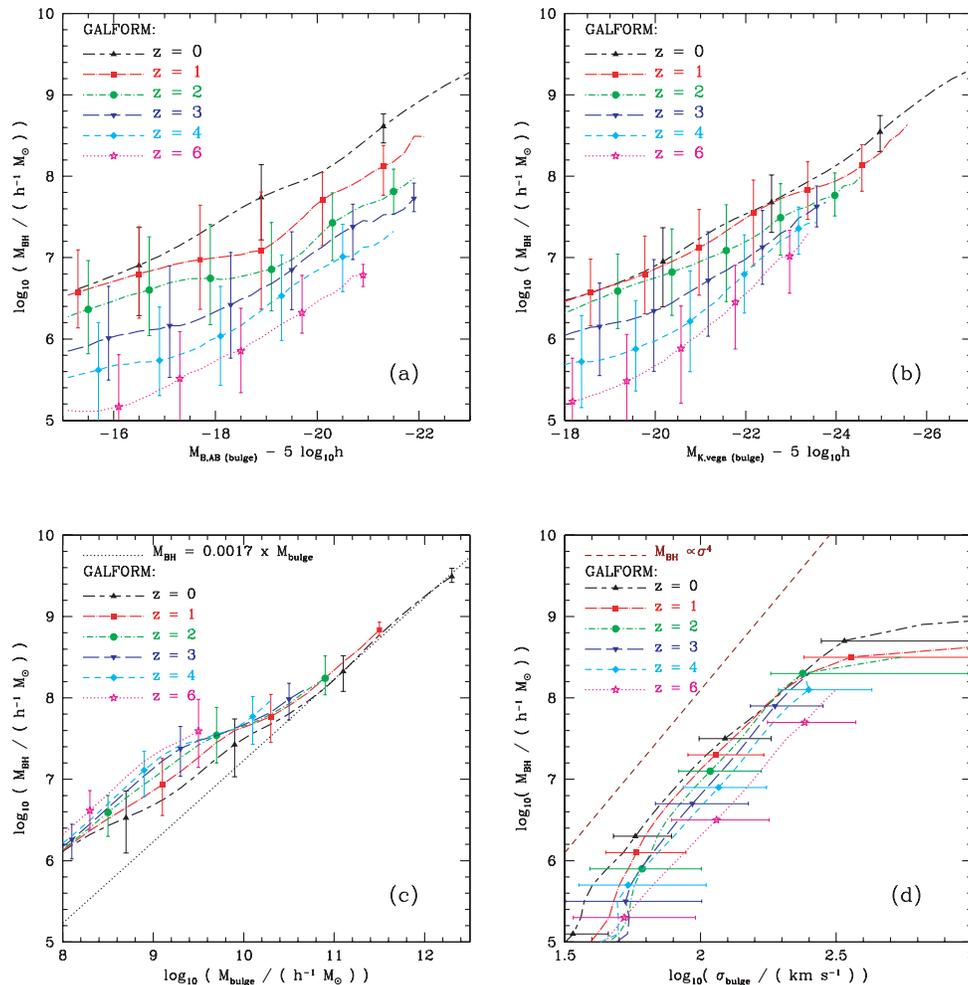
## 5 THE EVOLUTION OF THE RELATION BETWEEN BLACK HOLE MASS AND BULGE PROPERTIES

In this section, we discuss the evolution of the relationship between BH mass and various galaxy bulge properties:  $K$ - and  $B$ -band bulge magnitude, bulge stellar mass and bulge velocity dispersion. We show these relationships in Fig. 15, in each case plotting the model predictions for the  $M_{\text{BH}}-M_{\text{bulge}}$  relationships at  $z = 0, 1, 2, 3, 4$  and 6. We discuss each of these in turn, briefly referring to any relevant observational data. However, it is difficult to make rigorous comparisons to current data. While relationships between BH mass and bulge properties are fairly well determined at  $z = 0$ , this is currently not the case for  $z > 0$ , where observational samples are small and subject to selection effects. In particular, different surveys sample the population of galaxies and, where relevant, the AGN subpopulation, in ways that are not always straightforward to replicate in the models.

We show our model predictions for the  $M_{\text{BH}}-M_{\text{B,bulge}}$  relation in Fig. 15(a) and the  $M_{\text{BH}}-M_{K,\text{bulge}}$  relation in Fig. 15(b). In the model, these relationships shift towards brighter magnitudes at higher redshifts. This is a reflection of the evolving stellar populations. The stellar populations of bulges at low redshift are older and thus less luminous than their high-redshift counterparts. This effect more than compensates for any evolution in the opposite direction in the  $M_{\text{BH}}-M_{\text{bulge}}$  relation, which we discuss below. The redshift evolution in the  $M_{\text{BH}}-M_{\text{B,bulge}}$  relation is greater than that in the  $M_{\text{BH}}-M_{K,\text{bulge}}$  relation because stellar populations dim more strongly with time in the  $B$  band than in the  $K$  band. Observationally, however, Peng et al. (2006), selecting high-redshift quasars, find little trend in the  $M_{\text{BH}}-M_{R,\text{bulge,rest}}$  relation with redshift, which conflicts somewhat with our prediction of an evolution towards brighter magnitudes as redshift increases.

We show the  $M_{\text{BH}}-M_{\text{bulge}}$  relation in Fig. 15(c). There is no significant evolution in either the slope or scatter at large bulge masses. For  $M_{\text{bulge}} < 10^{10} h^{-1} M_{\odot}$ , the BH mass to bulge mass ratio increases with increasing redshift. Observationally, Peng et al. (2006) find that the ratio of  $M_{\text{BH}}/M_{\text{bulge}}$  was three to six times larger at  $z \gtrsim 2$  for AGN than for quiescent galaxies at  $z = 0$ . McLure et al. (2006), selecting radio galaxies at  $z > 0$  from the 3CRR catalogue, argue that  $M_{\text{BH}}/M_{\text{bulge}}$  increases with redshift, and is  $\sim 4$  times greater for radio galaxies at  $z = 2$  than for quiescent galaxies at  $z = 0$ . We find that  $M_{\text{BH}}/M_{\text{bulge}}$  was  $\sim 2$  times greater at  $z = 2$  than at  $z = 0$  for  $M_{\text{bulge}} < 10^{10} h^{-1} M_{\odot}$ . This evolution is in the same sense as and of comparable size to the observational trend, although the effect in the model is perhaps not as strong. As discussed in Section 3.1, the predicted variation in the  $M_{\text{BH}}/M_{\text{bulge}}$  ratio reflects the variation in the fraction of bulge stars which formed quiescently in discs. Mergers at higher redshift, when discs are more gas-rich and have fewer stars, deposit a lower fraction of (quiescently formed) disc stars in the bulge (e.g. Croton 2006).

Close inspection of Fig. 15(c) shows that a few objects at the highest redshifts have BH masses that exceed  $F_{\text{BH}} M_{\text{bulge}}$ . This would appear to be impossible given our definition of  $F_{\text{BH}}$  in Section 2.3. This apparent anomaly is due to our assumption that the mass of the BH increases instantaneously at the time of the starburst. In our



**Figure 15.** The redshift evolution of the relations between central BH mass,  $M_{\text{BH}}$ , and bulge properties. Each panel shows the relationship between  $M_{\text{BH}}$  and a different property of the host spheroid: (a) the bulge rest-frame  $B$ -band magnitude; (b) the bulge rest-frame  $K$ -band magnitude; (c) the stellar mass of the bulge; (d) the velocity dispersion of the bulge. The model predictions are shown by the symbols with error bars; the lines show the median relations and the error bars the 10–90 percentile spread of the distributions. Redshifts 0, 1, 2, 3, 4 and 6 are shown in different line types, as indicated by the key.

model, star formation in the bursts extends over  $\sim 50$  dynamical times, while quasars shine only over  $\sim 0.3$  dynamical times, so that the stellar mass builds up much more slowly than the BH mass. It seems likely, however, that a BH will still be growing towards its final mass towards the end of the starburst (Archibald et al. 2002; Alexander et al. 2005; Borys et al. 2005). We defer a study of the co-evolution of the stars and the BH mass to future work.

Finally, we show the  $M_{\text{BH}}-\sigma_{\text{bulge}}$  relation in Fig. 15(d). There is no evolution in the slope of the relation, but the zero-point does evolve and the scatter increases significantly towards higher redshift. For a given mass of BH, the velocity dispersion of the bulge is greater at higher redshift. To some extent, this evolution reflects the expected variation in the properties of dark matter haloes: at a given mass, the halo velocity dispersions scales as  $\sigma \propto (z_{\text{form}} + 1)^{1/2}$ . Alternatively, the evolution could be viewed as a reduction in the BH mass with increasing redshift, for a fixed bulge velocity dispersion.

Shields et al. (2003) have compared the relative amounts of BH mass in distant quasars and in galaxies in the local Universe. They find a large scatter and an increase of 0–0.5 dex in  $M_{\text{BH}}/\sigma_{\text{bulge}}$  between  $z = 0$  and  $\sim 3$ . Similarly, Woo et al. (2006) have compared Seyferts at  $z = 0.36$  with galaxies at  $z = 0$ . They too find an increase, of  $0.62 \pm 0.10$  dex, in BH mass at fixed  $\sigma_{\text{bulge}}$  at  $z = 0.36$

compared to  $z = 0$ . Thus, the observed trend in  $M_{\text{BH}}/\sigma_{\text{bulge}}$ , if any, is in the opposite direction to the trend we find in our simulations. It is possible that our model neglects effects that would cause BHs to be a larger fraction of the galactic bulge mass at higher redshifts. However, it must be remembered that  $\sigma_{\text{bulge}}$  is one of the more uncertain properties of the galaxies in our model and that dynamical effects which are not included could play a role in determining the properties of merger remnants (Dekel & Cox 2006; Robertson et al. 2006).

## 6 DOWNSIZING IN A HIERARCHICAL UNIVERSE

In cosmology, ‘downsizing’ is an ill-defined term which has been applied to describe the phenomenon whereby luminous activity (e.g. star formation or accretion on to BHs) appears to be occurring predominantly in progressively lower mass objects (galaxies or BHs) as the redshift decreases. Claims of downsizing were first made in connection with the population of star-forming galaxies (Cowie et al. 1996). More recently, the same trend has been inferred from the evolution of the X-ray luminosity function of quasars (Cowie et al. 2003; Steffen et al. 2003; Ueda et al. 2003; Barger et al. 2005;

Hasinger et al. 2005): the number of bright X-ray sources peaks at a higher redshift than the number of faint X-ray sources. The optical quasar luminosity function shows similar evolution, with more bright objects seen at increasing redshifts (e.g. Croom et al. 2004).

The apparent downsizing in the quasar X-ray luminosity function has been interpreted by some authors as implying that BHs acquire mass in an ‘*antihierarchical*’ manner (Marconi et al. 2004; Merloni 2004; Shankar et al. 2004; Hasinger et al. 2005). In this section, we demonstrate that the ‘downsizing’ of the *luminous* growth of BHs is actually a natural feature of our model, despite the fact that the overall assembly of mass into BHs is *hierarchical*. Downsizing in the galaxy population in hierarchical models is promoted by the earlier collapse and more active merging of objects in regions of high overdensity (Kauffmann 1995; Mouri & Taniguchi 2006; Neistein, van den Bosch & Dekel 2006). In recent models of galaxy formation, this natural trend is accentuated by the feedback processes associated with AGN activity in massive haloes (Bower et al. 2006; Croton et al. 2006). However, we wish to emphasize that AGN activity in low-redshift cooling flows is very far from being the only ingredient required for downsizing, and that we still find downsizing in our model. We now review some of the indirect evidence already presented in support of this conclusion (Section 6.1), and go on to present explicit predictions which reveal which BHs in our model are accreting mass most rapidly (Section 6.2).

### 6.1 Indirect evidence for downsizing in the model: the evolution of the optical luminosity function

The optical quasar luminosity function, as we have already remarked, reveals a dramatic increase in the space density of bright quasars with increasing redshift (Croom et al. 2004). In Section 3.2, we presented the model predictions for the optical luminosity function, which are in good agreement with this trend in the observations. Two features of our model are responsible for this success: the increase in the halo merger rate (and hence the galaxy merger rate) with increasing redshift and the increase in the gas content of discs with increasing redshift (see also Kauffmann & Haehnelt 2000). In combination, these phenomena lead to an increase in the frequency and strength of starbursts with redshift. In our model, a starburst results in a *luminous* phase of growth of the supermassive BH; a fraction  $F_{\text{BH}}$  of the cold gas which is turned into stars during the burst is accreted on to the BH.

Galaxy mergers are still an important way of building BH mass at low redshift. Our model predicts that BH–BH mergers are the most important channel for building BH mass for the most massive BHs at the present day. This *dark* growth process represents the assembly of mass which is already locked up in BHs into larger units. Galaxy mergers at low redshift tend to be gas-poor in our model simply because more time has elapsed to allow galactic discs to turn cold gas into stars quiescently. This effect is accentuated in the case of the most massive BHs which tend to reside in the more massive dark haloes. The process of galaxy formation starts earlier in the progenitors of massive haloes, since these objects collapse into bound structures earlier than is the case in less extreme environments.

### 6.2 Direct evidence for downsizing in the model: which black holes are accreting mass?

Our model allows us to separate the mass assembly of BHs into two contributions: accretion, in which cold gas is turned into BH mass in a starburst and mergers, in which existing BHs merge to build a more massive BH. Here we focus on the process of gas

accretion. Fig. 16 presents two views showing which mass of BHs are accreting material the most vigorously. The left-hand panels of Fig. 16 show the distribution of accretion rates, expressed in units of the Eddington mass accretion rate. Since the Eddington accretion rate scales with mass, this is easily scaled to give the distribution of fractional accretion rates. The right-hand panels compare the present accretion rate to the past average accretion rate (calculated as  $\langle \dot{M} \rangle_{t_{\text{age of Universe}}} / \langle M_{\text{BH}} \rangle$ , as a function of BH mass. Each row corresponds to a different redshift (top:  $z = 0$ , middle:  $z = 1$ , bottom:  $z = 2$ ). In these plots, we have *not* limited the mass accretion rate to be less than or equal to the Eddington limit.

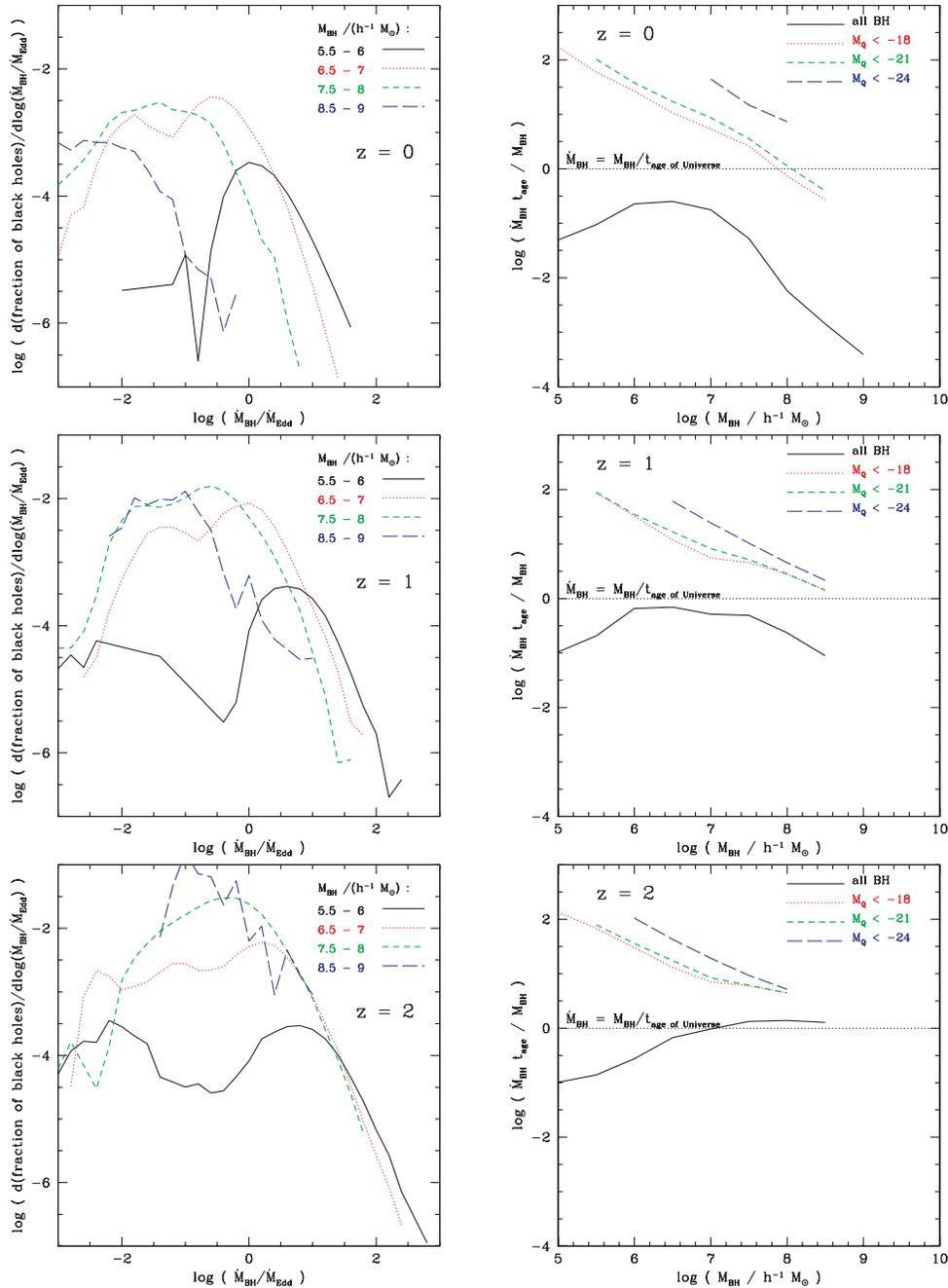
The left-hand column of Fig. 16 shows that, at all redshifts, there is a large spread in the Eddington ratios at which BHs are accreting. There is variation amongst mergers in gas supply, accretion time-scale and initial BH mass. Furthermore, the Eddington ratio evolves during any single accretion event. As expected, the mass accretion shifts towards higher fractions of the Eddington limit at higher redshift since there is more gas available in mergers. At  $z = 0$ , we see that as BH mass increases, accretion shifts to lower fractions of the Eddington ratio. This trend is less pronounced at  $z = 1$  and practically disappears by  $z = 2$ . Thus, more massive BHs were accreting mass more rapidly at  $z = 2$  than they are today. The predicted distribution of mass accretion rates at  $z = 0$  agree reasonably well with the observational results of Heckman et al. (2004). The distribution is normalized to unit area, but most BHs, particularly at lower redshifts, are not accreting at all (i.e. they are in a  $\delta$  function at  $\dot{M} = 0$ ).

The right-hand column of Fig. 16 shows the ratio of the present accretion rate to the past average accretion rate ( $\langle \dot{M} \rangle_{t_{\text{age}}} / \langle M_{\text{BH}} \rangle$ ) as a function of BH mass at  $z = 0, 1$  and  $2$ . If this ratio exceeds unity, then the current mass accretion rate exceeds the average rate at which the BH gained mass in the past (summed over all progenitors). The predictions for this ratio are sensitive to the BH selection, e.g. selection using a cut in quasar luminosity. We show results for all BHs (solid lines) and also for BHs selected as quasars brighter than a given luminosity. Note that the bulk of BHs in the model are not accreting material at any given time. The solid lines in each panel show that there is clear evidence for downsizing in the model. At  $z = 0$ , more massive BHs are growing less rapidly than less massive BHs. By  $z = 1$ , this trend is greatly diminished, and at  $z = 2$  it is reversed, i.e. the most massive BHs have the highest fractional accretion rate. When only quasars are selected, those with low-mass BHs show similar fractional accretion rates as redshift varies from 0 to 2, while quasars with massive BHs show a strong decline in fractional accretion rate towards the present day.

## 7 SUMMARY AND DISCUSSION

We have described an extension to the GALFORM semi-analytical model of galaxy formation in the  $\Lambda$ CDM cosmology to track the growth of BHs. Our model for BH growth has one free parameter,  $F_{\text{BH}}$ , the mass accreted on to the BH as a fraction of the stellar mass produced during a starburst. We set the value of  $F_{\text{BH}}$  so as to reproduce the zero-point of the present-day  $M_{\text{BH}}-M_{\text{bulge}}$  relations. The slope, scatter and evolution of the  $M_{\text{BH}}-M_{\text{bulge}}$  relations are model predictions.

In our model, BHs grow only during and following a galaxy merger. They grow through two distinct channels: mergers of pre-existing BHs and accretion of cold gas if a starburst is triggered by the merger. The importance of growth through BH mergers increases with the mass of the BH; at  $z = 0$  the growth of BHs less massive than  $5 \times 10^7 h^{-1} M_{\odot}$  is dominated by accretion, while the growth of



**Figure 16.** Left-hand panels: The distribution of accretion rate normalized by the Eddington mass accretion rate. Right-hand panels: the current mean mass accretion rate normalized by the past average mass growth rate, plotted against BH mass. In both cases, each row corresponds to a different redshift:  $z = 0$  (top),  $z = 1$  (middle) and  $z = 2$  (bottom). In the left-hand panels, each line shows the distribution of accretion rates for black holes in the mass interval shown by the key. In the right-hand panels, the lines correspond to different cuts on quasar luminosity, again as shown by the key.

more massive BHs is dominated by mergers. In general, the growth of BH mass by mergers becomes more important at low redshifts as the supply of gas available for accretion is consumed by star formation. Our model neglects BH growth from gas accreted directly in a cooling flow from a hot gas reservoir, as may be expected in massive haloes at late times. This is the ‘feedback mode’ of BH growth invoked by Bower et al. (2006) in their model that explains why there is an exponential cut-off at the bright end of the galaxy luminosity function. Apart from this new growth channel and an explicit treatment of disc instabilities, the calculation of BH growth

in the Bower et al. model is very similar to ours. However, around 20 per cent of the global mass in BHs in the Bower et al. study is due to the ‘feedback mode’ of growth. It is as important as mass assembly due to galaxy mergers for the most massive BHs, which accumulate  $\sim 50$  per cent of their mass via this channel (Richard Bower, private communication).

Essentially all current observational estimates of the accumulation of BH mass are sensitive to *luminous* growth, i.e. mass accretion. However, we predict that the importance of growth through BH–BH mergers grows with decreasing redshift and with increasing

BH mass. BH–BH mergers represent a *dark* mode of growth that is more difficult to observe and confirm. The most obvious way to detect BH–BH mergers is through the emission of gravitational waves (e.g. Haehnelt 1994). This may be possible in 10 yr with the planned LISA gravitational wave interferometer. When gas is present during a BH merger, a circumbinary accretion disc could form and the BH merger may produce high velocity gas outflows (Armitage & Natarajan 2002) followed by an X-ray afterglow which could be detected by the next generation of X-ray observatories (Milosavljević & Phinney 2005). Winged or X-shaped radio sources (Merriitt & Ekers 2002) and cores in elliptical galaxies (Faber et al. 1997; Milosavljević et al. 2002) may be indirect evidence of gas-poor mergers.

Our model predicts that the most important growth mechanism for the most massive BHs is the ‘dark’ mode or mass assembly through BH mergers. A testable prediction of our model is that a tail of BHs with masses above a few times  $10^9 M_\odot$  should be found at  $z = 0$  once high quality observations covering a large volume of the local Universe become available (Section 4.2). Furthermore, we expect that these will be more massive than any found in quasars at high redshift. To date, only BHs less massive than  $\sim 3 \times 10^9 M_\odot$  have been unambiguously observed in galaxies at  $z = 0$  (Tremaine et al. 2002) and in luminous, optically selected quasars over the redshift interval  $0 < z < 2$  (McLure & Dunlop 2004). However, this implied limit on BH mass is far from robust. The most massive BHs at  $z = 0$  tend to reside in massive and hence rare elliptical galaxies, which could easily have been missed in existing surveys. Larger volumes ( $\gtrsim$  a few times  $10^6 h^{-3} \text{Mpc}^3$ ) need to be surveyed to find such objects, which are therefore likely to lie at large distances. This, coupled with their expected low surface brightness (more massive ellipticals tend to have lower surface brightness cores), could make it difficult to measure their central mass using methods based on stellar dynamics (Kormendy & Gebhardt 2001). The high-redshift quasar data do not give a complete census of the BH populations, as quasar observations are only able to probe accreting BHs.

There is an important distinction to be made in our model between *mass transformation* and *mass assembly*. Mass transformation refers to the process of turning cold gas into BH mass; at any one time in the formation history of a BH, this phenomenon could be occurring across a number of progenitor BHs. Mass assembly refers to the accumulation of mass in a BH’s main progenitor, and may occur via both direct accretion of gas and merging of pre-existing BHs. BH mass *assembles* hierarchically; more massive BHs are assembled at lower redshifts than less massive BHs. However, if we choose to define the formation time of a BH in terms of the mass *transformation* redshift when some fraction of its mass has been *accreted* on to any progenitor, we find that, for  $M_{\text{BH}} > 10^7 h^{-1} M_\odot$ , more massive BHs form earlier. This dichotomy mirrors the growth of stellar mass in galactic spheroids in hierarchical models. In the semi-analytical models, galaxy mergers produce spheroids. At high redshift, the mergers tend to be gas-rich and new stars are produced as a result of the merger event. At low redshift, galactic discs tend to be gas-poor and consist mainly of stars, with the result that the merger simply rearranges the pre-existing stars (Baugh et al. 1996; Kauffmann 1996; Bell et al. 2006; De Lucia et al. 2006).

While we find that BH mass is assembled hierarchically, our model clearly exhibits a ‘downsizing’ in the mass of BHs which are undergoing luminous accretion. At the present day, we find that low-mass BHs are accreting material at a higher proportion of their Eddington luminosity than high-mass BHs. This distinction is less apparent at higher redshifts. Another way to demonstrate this down-

sizing is to examine the rate at which BHs are accreting mass, expressed as a fraction of the mass already in place:  $\langle \dot{M}_{\text{BH}} \rangle / \langle M_{\text{BH}} \rangle$ . At  $z = 0$ ,  $\dot{M}_{\text{BH}} / M_{\text{BH}}$  is largest for low-mass BHs and drops rapidly with increasing mass. This trend is removed with increasing redshift; accretion becomes an increasingly important mode of mass assembly for all masses of BH at earlier epochs in the universe.

A number of authors have claimed that BHs grow in an ‘anti-hierarchical’ fashion (Marconi et al. 2004; Merloni 2004; Shankar et al. 2004). This conclusion is reached by comparing an inferred present-day BH mass function with the BH mass function expected from AGN relics under the assumption that BHs grow exclusively by accretion. These calculations ignore any contribution to the mass of BHs arising from BH–BH mergers. Furthermore, the assumption that all BHs accrete at a constant fraction of their Eddington ratio (Marconi et al. 2004; Shankar et al. 2004), or the use by Merloni (2004) of the ‘fundamental plane of BH activity’ (Merloni, Heinz & Di Matteo 2003), which has a very large scatter, will introduce errors that may become cumulatively very large as the BH mass function is integrated backwards in time.

While the zero-points of the present-day  $M_{\text{BH}}-M_{\text{bulge}}$  relations are set by adjusting a single free parameter, the slope, scatter and evolution of these relations are genuine predictions of the model. We find little evolution with redshift in the slope of any of the  $M_{\text{BH}}-M_{\text{bulge}}$  relations, although our model predicts differing evolution in their zero-points, depending upon which particular bulge property is being considered. If we focus attention on a fixed BH mass, we find that with increasing redshift, the typical host bulge is more luminous in the rest-frame *B* and *K* bands, shows little change in stellar mass (except in the case of low-mass BHs, where the stellar mass is lower) and has a somewhat higher velocity dispersion.

Our model predicts the presence of massive BHs at high redshift. However, our simulations are not large enough to check if a population of sufficiently massive BHs has formed at high redshift to account for observations of quasars that have been interpreted as implying the presence of very massive BHs at early times (Fan et al. 2001, 2004). Fan et al. have discovered quasars of magnitude  $M_{1450} \sim -27$  at  $z \sim 6$ , albeit at a low space density,  $\phi \approx 1.6 \pm 0.5 \times 10^{-10} h^3 \text{Mpc}^{-3}$  (Fan et al. 2004). Assuming that these objects are radiating at the Eddington luminosity with an Elvis et al. (1994) spectrum, and that beaming and gravitational lensing are insignificant, Fan et al. (2001) inferred that these quasars host BHs masses of  $\sim 1-3 \times 10^9 h^{-1} M_\odot$ . In this paper, we probe the mass function of  $z = 6$  BHs only down to a space density of  $\phi \sim 1 \times 10^{-8} h^3 \text{Mpc}^{-3}$ , which is not sparse enough to compare with these data. We plan to address this problem by performing simulations of a larger volume than those analysed here, which will probe the high-mass end of the halo mass function in detail.

In summary, we have presented a new model for the concurrent growth of galaxies and BHs in the  $\Lambda$ CDM cosmology. We have previously shown that this model can successfully account for many observed properties of the galaxy population over a large range of wavelengths, from the local optical and infrared galaxy luminosity function to the number counts of submillimetre galaxies and the UV luminosity function of Lyman-break galaxies at redshift  $z \sim 3$  (Baugh et al. 2005). In this paper we have focused on the properties of the BH population that grows in unison with the spheroidal component of the galaxies. This model can account for a variety of observables that involve BHs, such as the relationship between the mass of the central BH in galaxies and the properties of the bulge, the quasar luminosity function and the apparent ‘antihierarchical’ growth of BHs. The model may be tested by future observations of the evolution of the  $M_{\text{BH}}-M_{\text{bulge}}$  relations and, perhaps, by the

detection of gravitational waves associated with the mergers of massive BHs that play a prominent role in our model.

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